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# 57 PRACTICAL PROGRAMS & GAMES IN BASIC

BY KEN TRACTON



Programs for Everything from Space War Games to Blackjack . . . from Craps to I Ching!

# 57 PRACTICAL PROGRAMS & GAMES IN BASIC

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DY KEN TRACTON



#### FIRST EDITION

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### **Preface**

These programs are intended for the computer hobbyist or user who has access to a computer system with standard BASIC language available.

The various programs are written in such a manner that they will operate even with a simplified subset of full BASIC. The advanced programmer, with full BASIC available, can easily modify the programs to take advantage of the functions and capabilities of the full instruction set.

The programs were chosen not just for their intrinsic qualities, but also for their role as teaching aids.

I would like to take this opportunity to thank the following people who helped to make this book possible. Alec Grynspan, who supplied the Bubble-Sort program; Tom McRoberts, who was able to read my notes and typed the manuscript; Laura Semple, who drew the final drafts of the flow charts; Jane, who said programming is simple; and David, who named my Iguana.

I would like to extend a special thank you to Construction Data Systems, who allowed me access to their time-sharing facility on an IBM 370-158 computer systems.

Ken Tracton

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#### **BASIC STATEMENTS**

BASIC (Beginners' All-purpose Symbolic Instruction Code) was invented and developed between 1963 and 1964 by John Kemeny and Thomas Kurtz of Dartmouth College. Since its first use in 1964, BASIC has steadily gained popularity as a high-level computer language which the user can easily master. The essential vocabulary is below:

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Statement	Example	Definition
CHANGE	CHANGE N\$ TO N	assigns to the elements of N the ASCII numeric value of the string N $\$$
DATA	DATA 15, -8, 76,	the DATA statement assigns appropriate values to the variables listed in the READ statement
DEF	DEF FNR $(X, Y) = (X 2 + Y 8)$	a single line function is defined by the DEF statement
DIM	DIM Z(3, 4)	dimensions the elements of X as a 3 by 4 matrix
END	END	ends program execution
FNEND	FNEND	a multiline DEF statement must end with a FNEND (function end) statement
FOR-TO	FOR X = 2 TO 66	defines the FOR, NEXT loop
GOTO	GOTO 100	transfers execution to line 100
GOSUB	GOSUB 100	transfers program control to a subroutine commencing at $100$
IF-THEN	IF A = X THEN 100	transfers program execution to 100 if the relational test is true
INPUT	INPUT X, Y,	assigns to the variable(s) the values presented by the user from a user defined device
LET	LET $A = V$	assigns the value of V to A
NEXT	NEXT X	returns control to the beginning of the FOR-TO loop
ON-GO TO	ON M GO TO 10, 20, 30	as M ranges in values from 1 up to 1st, 2nd,line number is transferred control, as follows to GO TO statement
PRINT	PRINT "LESLIE"	prints the alphanumeric string within quotation marks
RANDOMIZE	RANDOMIZE	assures each call to the RND produces a different order of random numbers
READ	READ L, K,	reads values from the DATA statement found in the same program
REM	REM AREA	remark is placed in the program to be used only during listing as a debugging aid

Statement	Example	Definition
RESTORE	RESTORE	restores the data pointer
RETURN	RETURN	returns program execution to the next instruction following the subroutine call
RND	RND	produced a random number
STOP	STOP	stops program execution

#### **LIBRARY FUNCTIONS**

ABS absolute value ATN arctangent

ASC converts a ASCII character to its numeric value

and assigns it

CHR\$ converts a numeric value to its ASCII character

and assigns it

COS cosine
COT cotangent
DET determinant

EXP raise e to the x power INT truncates to an integer

LOC determines the position of the pointer
LOF determines the last storage location in a file
returns the log (base e) of the argument

RND produces a random variable
SGN determines the sign of a variable

SIN sine

SQR square root

TAB positions printing head of a printer (CRT or LINE)

TAN tangent

#### **BASIC COMMAND FUNCTIONS**

BYE terminates time-sharing session CATALOG lists names of all files saved

GOOD-BYE same as BYE

LIST produced a listing of the current file
NEW specifies that a new file is being formed

OLD accesses an existing file

RENAME allows the name of a current file to be changed

RUN causes current program to be executed SAVE causes current program to be saved (stored)

SCRATCH deletes the current file

SYSTEM transfers control from BASIC to the system's

monitor

UNSAVE cancels storage of a file

exponential ↑ multiplication •

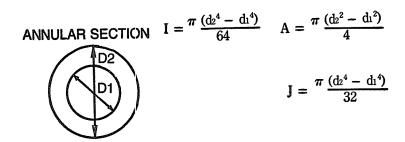
#### **PROGRAMS**

The programs appear in alphabetical order. Each one contains any applicable formulae, followed by an example of using the Program, the Flow Chart, and lastly, the Program itself.

#### **ANNULAR SECTIONS**

This program computes the various parameters; moment of inerta, polar moment of inertia and area; connected with an annular section.

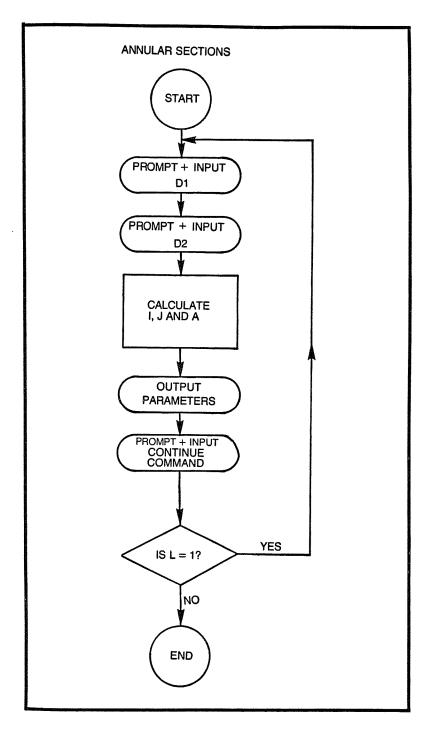
#### **FORMULAE**



where I and J is in (in.3) and A is in (in.2).

#### **EXAMPLE**

```
INSIDE DIAMETER (D1) =
?
3
OUTSIDE DIAMETER (D2) =
?
4.11
MOMENT OF INERTIA = 10
POLAR MOMENT OF INERTIA = 20
AREA OF SECTION = 6.18
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
* END
```



#### **ANNULAR SECTIONS**

- 10 REM THIS PROGRAM COMPUTES THE VARIOUS
- 20 REM PARAMETERS CONNECTED WITH AN ANNU-LAR
- 30 REM SECTION
- 40 PRINT "INSIDE DIAMETER (D1) = ";
- 50 INPUT D1
- 60 PRINT "OUTSIDE DIAMETER (D2) = ";
- 65 INPUT D2
- 70 LET P = 3.14159
- 80 LET  $I = (P^*((D2 \uparrow 4) (D1 \uparrow 4)))/64$
- 90 LET  $J = I^{*}2$
- 100 LET A =  $(P^*((D2 \uparrow 2) (D1 \uparrow 2)))/4$
- 110 PRINT "MOMENT OF INERTIA = ";I
- 120 PRINT "POLAR MOMENT OF INERTIA = ";J
- 130 PRINT "AREA OF SECTION = ";A
- 140 PRINT
- 150 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 160 INPUT L
- 170 IF L = 1 THEN 190
- 180 STOP
- 190 PRINT
- 200 GO TO 40
- 210 END

#### **ARITHMETIC MEAN**

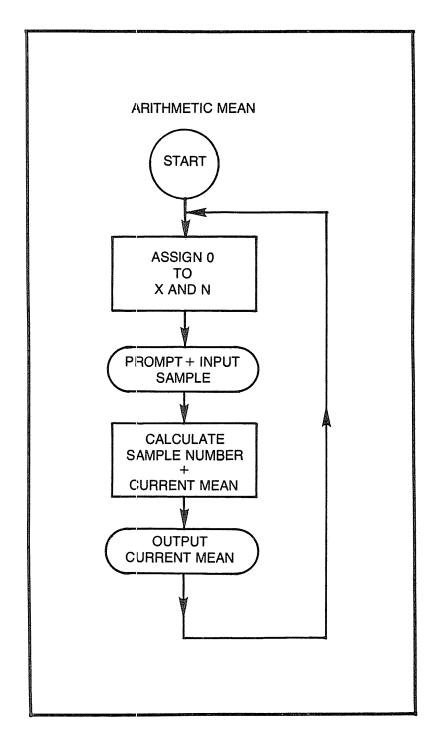
After each sample is entered the computer responds with sample number and the current mean. The program will continue to run until the operator types an exit or a break command.

#### **FORMULA**

$$\overline{A} = \frac{1}{N} \sum_{i=1}^{N} a_i$$

```
EXAMPLE
```

```
ENTER SAMPLE
5
   N = 1
          SAMPLE = 5 CURRENT MEAN = 5
ENTER SAMPLE
67
   N=2
            SAMPLE = 67 CURRENT MEAN = 36
ENTER SAMPLE
5
   N = 3
           SAMPLE = 5
                        CURRENT MEAN = 25.6666
ENTER SAMPLE
?
45
   N = 4
           SAMPLE = 45 CURRENT MEAN = 30.5
ENTER SAMPLE
?
12
   N = 5
          SAMPLE = 12
                        CURRENT MEAN = 26.8000
ENTER SAMPLE
123
   N = 6
          SAMPLE = 123
                        CURRENT MEAN = 42.8333
ENTER SAMPLE
?
0
   N = 7
          SAMPLE = 0
                       CURRENT MEAN = 36.7142
ENTER SAMPLE
*END
```



#### ARITHMETIC MEAN

- 10 REM THIS PROGRAM COMPUTES THE ARITHMETIC
- 20 REM MEAN
- $30 \qquad \text{LET X} = 0$
- 40 LET N = 0
- 50 PRINT "ENTER SAMPLE":
- 60 INPUT W
- 70 LET N = N + 1
- 80 LET X = X + W
- 90 LET A = X/N
- PRINT "N = "; N, "SAMPLE = "; W, "CURRENT MEAN = "; A
- 110 GOTO 50
- 120 END

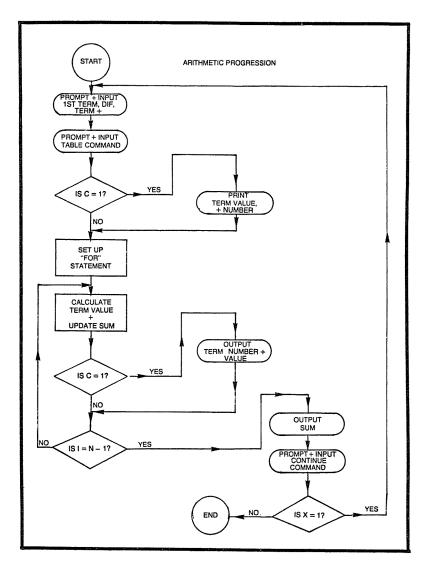
#### ARITHMETIC PROGRESSION

From the following information; first term, common difference and number of terms, this program computes the arithmetic progression.

#### **FORMULA**

```
A, A + D, A + 2D,...A + ((N-1)D)
```

EXAMPLE	
FIRST TERM =	
?	
10	
COMMON DIFFERENCE =	
?	
2	
NUMBER OF TERMS =	
?	
5	
FOR TABLE TYPE 1, IF NOT TYPE 0	
?	
1	
ARITHMETIC PROGRESSION	
TERM NUMBER	TERM PROGRESSION
1	10
2	12
3	14
4	16
5	18
SUM = 70	
TYPE 1 TO CONTINUE, 0 TO STOP	
?	
0	
*END	



#### **ARITHMETIC PROGRESSION**

- 10 REM THIS PROGRAM COMPUTES ARITHMETIC PROGRESSION
- 20 PRINT "FIRST TERM = ";
- 30 INPUT A
- 40 PRINT "COMMON DIFFERENCE = ";
- 50 INPUT D
- 60 PRINT "NUMBER OF TERMS = ";

- 70 INPUT N
- 80 PRINT "FOR TABLE TYPE 1, IF NOT TYPE 0";
- 90 INPUT C
- 100 IF C = 1 THEN 120
- 110 GOTO 140
- 120 PRINT "ARITHMETIC PROGRESSION"
- 130 PRINT "TERM NUMBER", "TERM VALUE"
- 140 LET J = 0
- 150 FOR I = 0 TO N 1
- 160 LET K = I + 1
- 170 LET  $L = A + (I^*D)$
- 180 LET J = J + L
- 190 IF C = 1 THEN 210
- 200 GOTO 220
- 210 PRINT K, L
- 220 NEXT I
- 230 PRINT "SUM = ";J
- 240 PRINT
- 250 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 260 INPUT X
- 270 IF X = 1 THEN 290
- 280 STOP
- 290 PRINT
- 300 GOTO 20
- 310 END

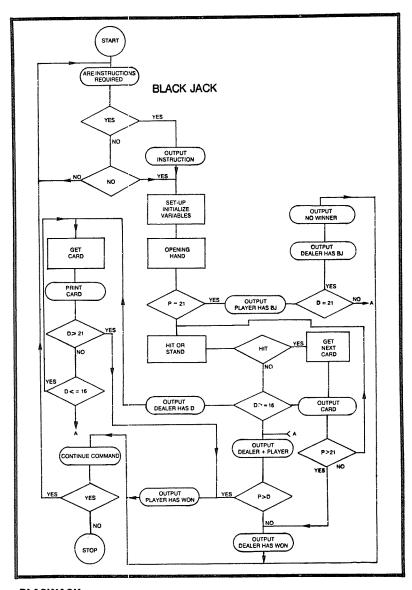
#### BLACKJACK

Blackjack, or the game of 21, is played against the computer, it being the dealer. Cards are dealt from a self-replenishing deck. Standard rules are as follows:

- Blackjack wins unless the dealer also gets blackjack, in which case there is no winning player.
- · The highest score below 21 wins.
- The dealer must draw a card if he is below 17, but must stand if he has 17 or greater.
- Aces count as 11 unless it would force a hand over 21, in which case the ace counts as 1.

#### **EXAMPLE**

```
RUN
IF INSTRUCTIONS ARE REQUIRED TYPE YES
IF NOT TYPE NO
?
NO
***GOOD-LUCK-----MAY THE BEST ONE WIN***
THE DEALER HAS A 9 SHOWING
YOU HAVE A 5 AND A 11
YOUR TOTAL IS 16
DO YOU WANT A HIT, OR DO YOU STAND
HIT
YOUR CARD IS 4
DO YOU WANT A HIT, OR DO YOU STAND
STAND
THE DEALER HAS 12
THE DEALER DRAWS A 5
HIS TOTAL IS 17
YOU HAVE 20
YOU HAVE WON!!!
DO YOU WISH TO PLAY AGAIN
TYPE YES OR NO
5
NO
BLACKIACK SAYS GOOD-BYE
*END
```



#### **BLACKJACK**

- 10 REM BLACKJACK
- 20 PRINT "IF INSTRUCTIONS ARE REQUIRED TYPE YES"
- 30 PRINT "IF NOT TYPE NO"
- 40 INPUT C\$
- 50 IF C\$ = "YES" THEN 90

- 60 IF C\$ = "NO" THEN 340
- 70 PRINT "INVALID RESPONSE"
- 80 GOTO 20
- 90 PRINT
- 100 PRINT"\*\*\*\*\*\*\*\*\*\*\*BLACKJACK\*\*\*\*\*\*\*\*\*\*\*\*
- 110 PRINT
- 120 PRINT "THE COMPUTER AS THE DEALER, DEALS TWO CARDS TO ITSELF"
- 130 PRINT "AND TWO CARDS TO THE PLAYER. THE PLAYER'S TWO CARDS"
- 140 PRINT "ARE SHOWN FACE UP, WHILE ONLY ONE OF THE DEALER'S"
- 150 PRINT "CARDS IS SHOWN. BOTH THE DEALER AND THE PLAYER"
- 160 PRINT "MAY DRAW ADDITIONAL CARDS."
- 170 PRINT "THE PLAYER'S GOAL IS TO REACH 21 OR LESS. BUT"
- 180 PRINT "BE CLOSER TO 21 THAN THE DEALER'S HAND."
- 190 PRINT "IF THE PLAYER'S OR THE DEALER'S HAND TOTALS"
- 200 PRINT "GREATER THAN 21 HE IS BUSTED! THE KING"
- 210 PRINT "THE QUEEN AND THE JACK ALL COUNT AS 10 POINTS."
- 220 PRINT "ALL OTHER CARDS EXCEPT THE ACE COUNT AS THEIR FACE"
- 230 PRINT "VALUE SHOWS. THE ACE COUNTS AS 11 UNLESS THIS"
- 240 PRINT "WOULD CAUSE THE HAND TO BE OVER 21, IN THAT"
- 250 PRINT "CASE THE ACE COUNTS AS 1."
- 260 PRINT "IF BOTH THE DEALER AND THE PLAYER GET BLACKJACK"
- 270 PRINT "WHICH IS A TWO CARD HAND TOTALING 21"
- 280 PRINT "NEITHER WINS, IT IS A PUSH"
- 290 PRINT "IF THE DEALER'S HAND IS BELOW OR EQUAL TO 16"
- 300 PRINT "HE MUST DRAW, AFTER 17 THE DEALER MUST STAND"
- 310 PRINT "TO RECEIVE A CARD YOU WANT A HIT-"
- 320 PRINT "TO STOP WHERE YOU ARE, YOU STAND-"
- 330 PRINT

```
340
      PRINT"***GOOD-LUCK-----MAY THE BEST ONE
             WIN***"
350
      REM 1ST HAND
355
      RANDOMIZE
360
      LET D = 0
370
      LET P = D
380
      GOSUB 820
390
      LET D1 = C
400
      GOSUB 820
410
      LET D2 = C
420
      GOSUB 890
430
      LET P1 = C
      GOSUB 890
440
      LET P2 = 3
450
      PRINT
460
      PRINT "THE DEALER HAS A ";D1;" SHOWING"
470
480
      PRINT "YOU HAVE A ";P1;" AND A ";P2
490
      PRINT "YOUR TOTAL IS":P1 + P2
500
      LET D = D1 + D2
510
      LET P = P1 + P2
520
      IF P = 21 THEN 640
530
      GOSUB 960
540
      IF L = 1 THEN 690
550
      IF D < = 16 THEN 740
560
      PRINT "THE DEALER HAS":D
570
      PRINT "YOU HAVE":P
580
      IF P > D THEN 620
590
      REM WIN OR LOSS STATEMENTS
600
      PRINT "THE DEALER HAS WON!!!"
610
      GOTO 1060
620
      PRINT "YOU HAVE WON!!!"
630
      GOTO 1060
      PRINT "***YOU HAVE BLACKJACK***"
640
650
      IF D = 21 THEN 670
660
      GOTO 560
670
      PRINT "THE DEALER ALSO HAS BLACKJACK.
      SORRY NO WINNER"
680
      GOTO 1060
690
      GOSUB 890
      PRINT "YOUR CARD IS ":C
700
710
      IF P > 21 THEN 600
      GOTO 530
730
740
      PRINT "THE DEALER HAS";D
```

```
750 GOSUB 820
```

760 LET 
$$D = D + C$$

- 770 PRINT "THE DEALER DRAWS A";C
- 780 PRINT "HIS TOTAL IS ";D
- 790 IF D > 21 THEN 620
- 800 IF D < = 16 THEN 750
- 810 GOTO 560
- 820 LET C = 1 + INT(11\*RND)
- 830 IF C = 11 THEN 850
- 840 GOTO 880
- 850 IF D + C > 21 THEN 870
- 860 GOTO 880
- 870 LET C = 1
- 880 RETURN
- 890 LET C = 1 + INT(11\*RND)
- 900 IF C = 11 THEN 920
- 910 GOTO 950
- 920 IF P + C> 21 THEN 940
- 930 GOTO 950
- 940 LET C = 1
- 950 RETURN
- 960 PRINT "DO YOU WANT A HIT, OR DO YOU STAND"
- 970 INPUT Q\$
- 980 IF Q\$ = "HIT" THEN 1020
- 990 IF Q\$ = "STAND" THEN 1040
- 1000 PRINT "INVALID RESPONSE"
- 1010 GOTO 960
- $1020 \qquad \text{LET L} = 1$
- 1030 GOTO 1050
- $1040 \qquad \text{LET L} = 0$
- 1050 RETURN
- 1060 PRINT
- 1070 PRINT "DO YOU WISH TO PLAY AGAIN"
- 1080 PRINT "TYPE YES OR NO"
- 1090 INPUT L\$
- 1100 IF L\$ = "YES" THEN 1130
- 1110 PRINT "BLACKJACK SAYS GOOD-BYE"
- 1120 STOP
- 1130 PRINT
- 1140 GOTO 20
- 1150 END

#### **BUBBLE SORT**

This program is actually a subroutine rather than a stand-alone program. It is intended to be used in conjunction with larger programs which require that data be placed in an array in ascending sequence.

#### **BUBBLE SORT**

- 10 REM THIS PROGRAM IS A BUBBLE SORT, WHICH PLACES THE
- 20 REM VALUES IN AN ARRAY IN ASCENDING SE-QUENCE
- 30 REM IT IS INTENDED TO BE AN EXAMPLE AND NOT A
- 40 REM SPECIFIC CASE.
- 50 REM THIS PROGRAM MAY BE CONVERTED INTO A SUBROUTINE
- 60 REM FOR USE IN A LARGER PROGRAM
- 70 REM THE ARRAY IS Z OF LENGTH N
- 80 REM Z IS ASSUMED TO HAVE BEEN DECLARED IN A DIM
- 90 REM STATEMENT AND N SET AHEAD OF TIME
- $100 \qquad \text{LET I} = N 1$
- 110 FOR J = 1 TO I
- 120 LET K = J + 1
- 130 FOR L = N TO K STEP 1
- 140 IF Z(L) > Z(J) THEN 210
- 150 REM SAVE FIRST VALUE
- 160 LET T = Z(L)
- 170 LET Z(L) = Z(J)
- 180 LET Z(J) = T
- 190 REM IF Z IS THE KEY FOR SORTING MULTIPLE
- 200 REM ARRAYS AND EXTRA CODE HERE
- 210 NEXT L
- 220 NEXT J
- 230 RETURN

#### **CHI-SQUARE EVALUATION**

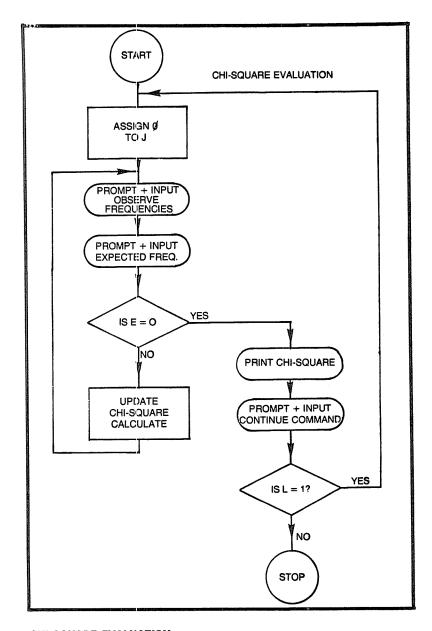
This program computes the chi-square evaluation from the inputed observed and expected frequencies. To terminate the evaluation the use simply inputs a 0 for the last expected frequency.

#### **FORMULA**

$$X^{2} = \sum_{i=1}^{N} \frac{(O_{1} - E_{i})^{2}}{E_{i}}$$

```
EXAMPLE
```

```
OBSERVED FREQUENCIES =
?
10
EXPECTED FREQUENCIES =
10
OBSERVED FREQUENCIES =
0
OBSERVED FREQUENCIES =
0
CHI-SQUARE = 0
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



#### **CHI-SQUARE EVALUATION**

- 10 REM THIS PROGRAM COMPUTES CHI-SQUARE
- 20 REM EVALUATION ON THE OBSERVED TO
- 30 REM EXPECTED FREQUENCIES
- 40 LET J = 0

- 50 PRINT "OBSERVED FREQUENCIES = "
- 60 INPUT D
- 70 PRINT "EXPECTED FREQUENCIES = "
- 80 INPUT E
- 90 IF E = 0 THEN 130
- 100 LET K = ((D E)/2)/E
- 110 LET J = J + K
- 120 GOTO 50
- 130 PRINT "CHI-SQUARE = ":J
- 140 PRINT "\*\*\*\*\*\*\*\*\*\*\*\*\*\*
- 150 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 160 INPUT L
- 170 IF L = 1 THEN 190
- 180 STOP
- 190 PRINT
- 200 GOTO 40
- 210 END

#### CIRCLE DETERMINED BY THREE POINTS

The user inputs three noncolinear points, and the program responds with the center and the radius of the circle thus generated.

#### **FORMULAE**

$$y_0 = \frac{K_2 - K_1}{N_2 - N_1} \qquad X_0 = K_2 - N_2 Y_0$$

$$r = (X_3 - X_0)^2 + (Y_3 - Y_0)^2$$

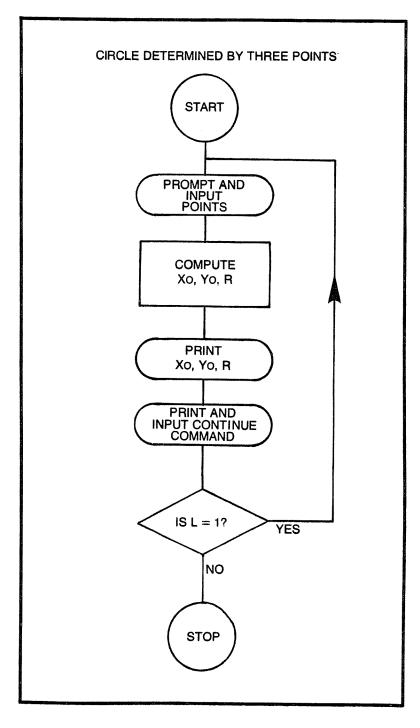
$$K_1 = \underbrace{(X_2 - X_1)(X_2 + X_1) + (Y_2 - Y_1)(Y_2 + Y_1)}_{2(X_2 - X_1)}$$

$$K_2 = \underbrace{(X_3 - X_1)(X_3 + X_1) + (Y_3 - Y_1)(Y_3 + Y_1)}_{2(X_3 - X_1)}$$

$$N_1 = \frac{Y_2 - Y_1}{X_2 - X_1} \qquad N_2 = \frac{Y_3 - Y_1}{X_3 - X_1}$$

#### **EXAMPLES**

```
INPUT X1,Y1
?
2,3
INPUT X2,Y2
?
5,4
INPUT X3,Y3
?
6,4.5
CENTER X0,Y0 = - 1.25,17.25
RADIUS = 15.10
TO CONTINUE TYPE 1, IF NOT TYPE 0
?
0
*END
```



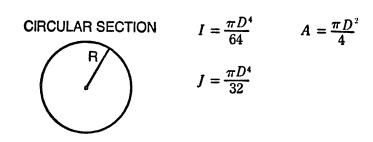
#### CIRCLE DETERMINED BY THREE POINTS

- 10 REM THIS PROGRAM COMPUTES THE CENTER AND RADIUS
- 20 REM OF A CIRCLE FROM 3 NON-COLINEAR POINTS
- 30 PRINT "INPUT X1, Y1";
- 40 INPUT X1, Y1
- 50 PRINT "INPUT X2, Y2";
- 60 INPUT X2, Y2
- 70 PRINT "INPUT X3, Y3";
- 80 INPUT X3, Y3
- 90 LET A = (Y2 Y1)/(X2 X1)
- 100 LET B = (Y3 Y1)/(X3 X1)
- 110 LET C =  $((X2 X1)^*(X2 + X1))^*$ +  $((Y2 - Y1)^*(Y2 + Y1))$
- 120 LET D = C/(2\*(X2 X1))
- 130 LET E = ((X3 X1)\*(X3 + X1)) + ((Y3 Y1)\*(Y3 + Y1))
- 140 LET F = E/(2\*(X3 X1))
- 150 LET YO = (F D)/(B A)
- 160 LET XO = F (B\*YO)
- 170 LET R =  $SQR((X3 X0)\uparrow 2 + (Y3 Y0)\uparrow 2)$
- 180 PRINT "CENTER X0, Y0 = ";X0;",";Y0
- 190 PRINT "RADIUS = ";R
- 200 PRINT
- 210 PRINT "TO CONTINUE TYPE 1, IF NOT TYPE 0"
- 220 INPUT L
- 230 IF L = 1 THEN 250
- 240 STOP
- 250 PRINT
- 260 GOTO 30
- 270 END

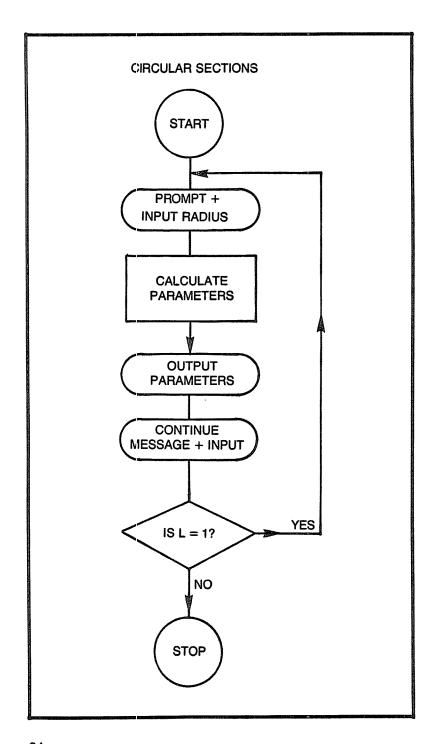
#### **CIRCULAR SECTIONS**

This program computes the various parameters: moment of inertia, polar moment of inertia and area connected within a circular section.

#### **FORMULAE**



where I & J are in in<sup>4</sup> and  $A = in^2$ 



#### CIRCULAR SECTION

- 10 REM THIS PROGRAM COMPUTES THE PARA-METERS
- 20 REM CONNECTED WITH A CIRCULAR SECTION
- 30 PRINT "RADIUS"
- 40 INPUT R
- 50 LET P = 3.14159
- 60 LET D = 2\*R
- 70 LET  $I = (P^*(D^{\dagger}4))/64$
- 80 LET  $J = I^{*}2$
- 90 LET A =  $(P^*(D_1^2))/4$
- 100 PRINT "MOMENT OF INERTIA =":I
- 110 PRINT "POLAR MOMENT OF INERTIA = ":J
- 120 PRINT "AREA OF SECTION = ":A
- 140 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 150 INPUT L
- 160 IF L = 1 THEN 180
- i70 STOP
- 180 PRINT
- 190 GOTO 30
- 200 END

#### **COMPOUNDED AMOUNTS**

This program applies to an amount of principle placed into an account and compounded periodically, with no further deposits.

#### **FORMULAE**

$$X = Y(1+I)^{N}$$
  $N = \frac{\ln(X/Y)}{\ln(1+I)}$   $Y = X(1+I)^{-N}$   $L = Y((1+I)^{N} - 1)$ 

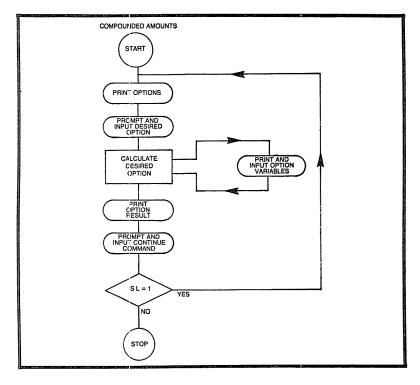
```
where N = number of Time periods
I = interest \ rate \ (decimal) \quad L = interest
Y = present \ value
X = future \ value
```

```
FUTURE VALUE(1)
PRESENT VALUE (2)
INTEREST (3)
PERIODIC INTEREST RATE (4)
NUMBER OF TIME PERIODS (5)
ENTER 1 TO 5
?
PRESENT VALUE =
100
INTEREST RATE =
10
NUMBER OF TIME PERIODS =
?
4
FUTURE VALUE = 146.41
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
ENTER 1 TO 5
2
```

```
FUTURE VALUE =
?
200
INTEREST RATE =
?
.1
NUMBER OF TIME PERIODS =
5
PRESENT VALUE =124.18
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
ENTER 1 TO 5
3
PRESENT VALUE =
300
INTEREST RATE =
.2
NUMBER OF TIME PERIODS =
6
INTEREST = 595.80
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
ENTER 1 TO 5
4
PRESENT VALUE =
100
FUTURE VALUE =
200
NUMBER OF TIME PERIODS =
?
5
INTEREST RATE = .15
```

```
TYPE 1 TO CONTINUE, 0 TO STOP

?
1
ENTER 1 TO 5
?
5
FUTURE VALUE ==
?
500
PRESENT VALUE ==
?
250
INTEREST RATE ==
?
.2
NUMBER OF TIME PERIODS =3.8
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



#### **COMPOUNDED AMOUNTS**

- 10 REM COMPOUNDED AMOUNTS
- 20 PRINT "FUTURE VALUE (1)"
- 30 PRINT "PRESENT VALUE (2)"
- 40 PRINT "INTEREST (3)"
- 50 PRINT "PERIODIC INTEREST RATE (4)"
- 60 PRINT "NUMBER OF TIME PERIODS (5)"
- 70 PRINT "ENTER 1 TO 5":
- 80 INPUT A
- 90 ON A GOTO 100,160,220,280,340
- 100 GOSUB 410
- 110 GOSUB 440
- 120 GOSUB 470
- 130 LET  $X = Y^*((1 + I) \uparrow N)$
- 140 PRINT "FUTURE VALUE = ":X
- 150 GOTO 390
- 160 GOSUB 500
- 170 GOSUB 440
- 180 GOSUB 470
- 190 LET  $Y = X^*((1 + I)\uparrow N)$
- 200 PRINT "PRESENT VALUE = ":Y
- 210 GOTO 390
- 220 GOSUB 410
- 230 GOSUB 440
- 240 GOSUB 470
- 250 LET L =  $Y^*((1 + I \uparrow N) 1)$
- 260 PRINT "INTEREST = ":L
- 270 GOTO 390
- 280 GOSUB 410
- 290 GOSUB 500
- 300 GOSUB 470
- 310 LET  $I = ((X/Y) \uparrow (1/N)) 1$
- 320 PRINT "INTEREST RATE = ":I
- 330 GOTO 390
- 340 GOSUB 500
- 350 GOSUB 410
- 360 GOSUB 440
- 370 LET N = (LOG(X/Y))/(LOG(1 + I))
- 380 PRINT "NUMBER OF TIME PERIODS = ";N
- 390 PRINT
- 400 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 401 INPUT L

IF L = 1 THEN 404 402 STOP 403 404 **PRINT** 405 **GOTO 70** PRINT "PRESENT VALUE = "; 410 420 INPUT Y 430 RETURN PRINT "INTEREST RATE = ": 440 450 INPUT I RETURN 460 PRINT "NUMBER OF TIME PERIODS = "; 470 480 INPUT N 490 RETURN 500 PRINT "FUTURE VALUE = "; INPUT X 510 520 RETURN

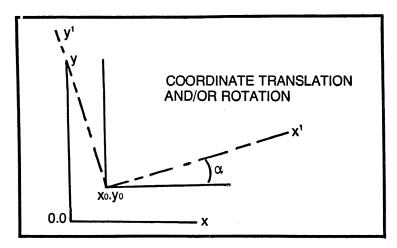
530

**END** 

#### COORDINATE TRANSLATION AND/OR ROTATION

This program will compute rectangular-coordinate translation and/or rotation. The origin is translated from (0,0) to a new point (X,Y) and the X,Y axes are rotated to an angle A to give new axes  $X^1,Y^1$ .

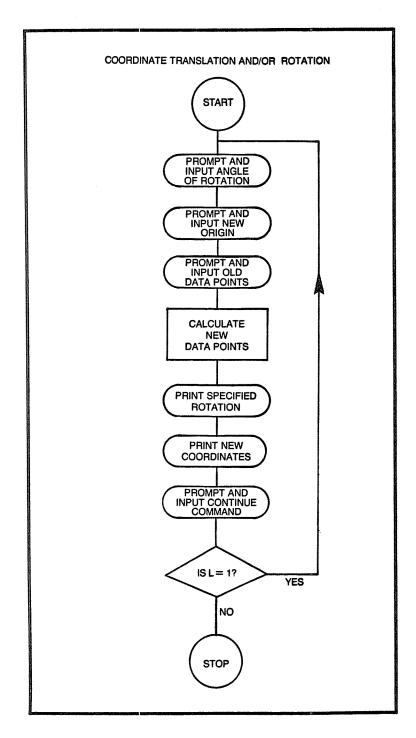
#### **FORMULAE**



$$X^{1} = (X - Xo)Cos \alpha + (Y - Yo)Sin \alpha$$
  

$$Y^{1} = -(X - Xo)Sin \alpha + (Y - Yo)Cos \alpha$$

```
ANGLE OF ROTATION IN DEGREES=
?
45
COORDINATES OF NEW ORIGIN (X0,Y0)=
?
5,6
OLD COORDINATES OF DATA POINT (X1, Y1)=
?
8,9
SPECIFIED ROTATION = 45
NEW COORDINATES OF DATA POINT
X2 =4.24
Y2 = 0
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



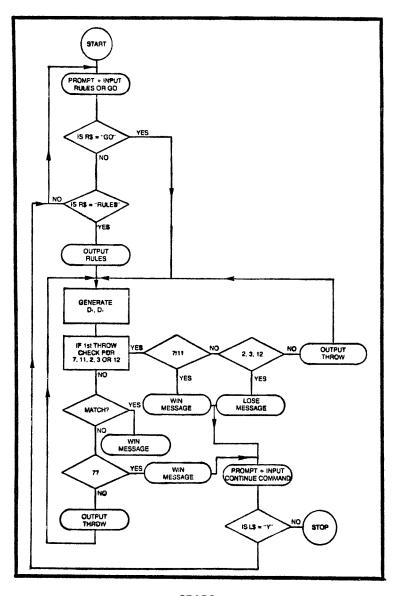
#### COORDINATE TRANSLATION AND/OR ROTATION

- 10 REM THIS PROGRAM COMPUTES RECTANGULAR COORDINATE
- 20 REM TRANSLATION AND/OR ROTATION
- 30 PRINT "ANGLE OF ROTATION IN DEGREES = ";
- 40 INPUT A
- 50 LET B = (A\*3.14159)/180
- PRINT "COORDINATES OF NEW ORIGIN (X0, Y0) =';
- 70 INPUT X.Y
- 80 PRINT "OLD COORDINATES OF DATA POINT (X1, Y1)
  =":
- 90 INPUT F,C
- 100 LET Z = F X
- 110 LET W = C Y
- 120 LET D = (Z\*COS(B)) + (W\*SIN(B))
- 130 LET E = -(Z\*SIN(B)) + (W\*COS(B))
- 140 PRINT
- 150 PRINT "SPECIFIED ROTATION =";A
- 160 PRINT "NEW COORDINATES OF DATA POINT"
- 170 PRINT "X2 = ";D
- 180 PRINT "Y2 = ";E
- 190 PRINT
- 200 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 210 INPUT L
- 220 IF L = 1 THEN 240
- 230 STOP
- 240 PRINT
- 250 GOTO 30
- 260 END

#### **CRAPS**

The following game-simulation is that of craps. Craps is a game that is played with two dice. The object of the game is to either win by throwing a 7 or an 11 on the first throw, or by matching your throw on the following throws. If on the first throw a 2, 3, or a 12 comes up you lose automatically; also, if you throw a 7 when looking for a match you lose too.

```
RUN
FOR RULES, TYPE RULES, OTHERWISE TYPE GO
?
GO
6
8
4
YOU THROW A 6 YOU WIN BY MATCHING
TO CONTINUE TYPE Y, IF NOT TYPE N
Y
FOR RULES, TYPE RULES, OTHERWISE TYPE GO
GO
YOU THROW A 7 YOU WIN
TO CONTINUE TYPE Y, IF NOT TYPE N
N
*END
```



## **CRAPS**

- 10 REM THIS PROGRAM SIMULATES THE GAME OF CRAPS
- 20 RANDOMIZE
- 30 PRINT " FOR RULES, TYPE RULES, OTHERWISE TYPE GO"
- 40 INPUT R\$

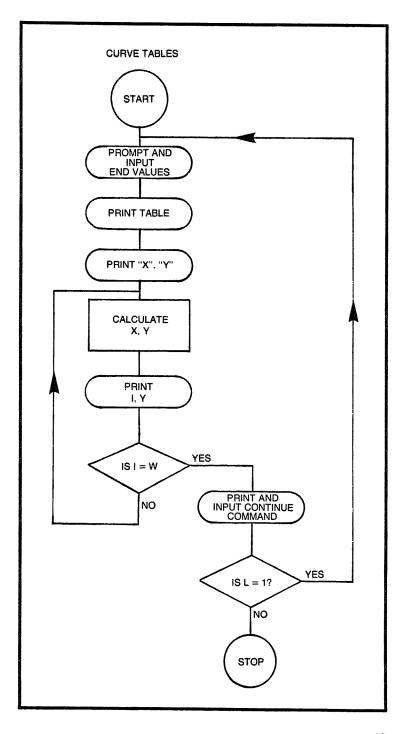
- IF R\$ = "RULES" THEN 90
- 60 IF R\$ = "GO" THEN 140
- 70 PRINT "INVALID COMMAND"
- 80 GOTO 30
- 90 PRINT "A 7 OR 11 ON THE FIRST THROW WINS"
- 100 PRINT "YOU CAN ALSO WIN BY THROWING A 4.5.6.8.9.10"
- 110 PRINT " AND MATCHING IT BEFORE THROWING A 7. IF ON"
- 120 PRINT "THE FIRST THROW A 2,3 OR A 12 COMES UP"
- 130 PRINT "YOU LOSE AUTOMATICALLY"
- 140 LET J = 0
- 150 GOSUB 460
- 160 LET D1 =N
- 170 GOSUB 460
- 180 LET D2 = N
- 190 LET D3 = D1 + D2
- 200 LET J = J + 1
- 210 IF J = 1 THEN 260
- 220 IF D3 = D4 THEN 420
- 230 IF D3 = 7 THEN 440
- 240 PRINT "YOU THROW A";D3
- 250 GOTO 150
- 260 IF D3 = 7 THEN 320
- 270 IF D3 = 2 THEN 340
- 280 IF D3 = 3 THEN 340
- 290 IF D3 = 12 THEN 340
- 300 IF D3 = 11 THEN 320
- 310 LET D4 = D3
- 315 GOTO 240
- 320 PRINT "YOU THROW A ":D3;" YOU WIN"
- 330 GOTO 350
- 340 PRINT "YOU THROW A ";D3;" YOU LOSE"
- 350 PRINT
- 360 PRINT "TO CONTINUE TYPE Y. IF NOT TYPE N"
- 370 INPUT L\$
- 380 IF L\$ = "Y" THEN 400
- 390 STOP
- 400 PRINT
- 410 GOTO 30
- PRINT "YOU THROW A ";D3;" YOU WIN BY MATCH-ING"
- 430 GOTO 350

440	PRINT "YOU THROW A ";D3;" SORRY YOU LOSE"
450	GOTO 350
460	LET N = 1 + INT(6*RND)
470	RETURN
480	END

## **CURVE TABLES (PLOTTING)**

This program generates a series of data points, with which the user can plot curves. The data points generated lie between the values given for the starting value and the end point of X. Step size may be changed by using a step statement in conjunction with the FOR statement. The user must supply the equation of the curve in line 140.

```
(ASSUMING THE EQUATION IS (2*X) + 6)
STARTING VALUE OF X =
5
END VALUE OF X =
10
TABLE
X
     Y
5
    16
6
    18
7
    20
    22
8
9
     24
     26
10
TYPE 1 TO CONTINUE,0 TO STOP
0
*END
```



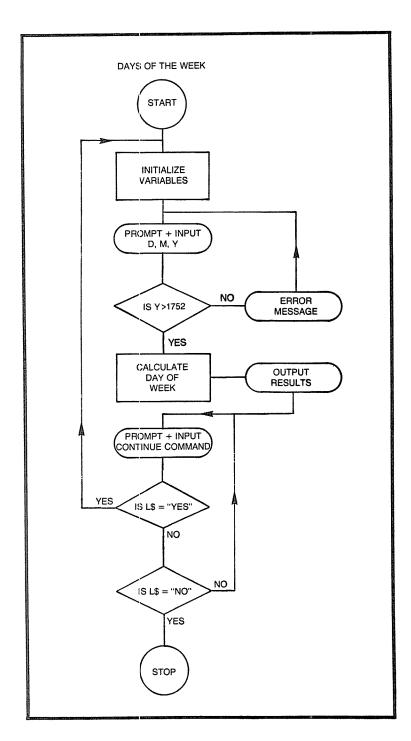
#### **CURVE TABLES**

- 10 REM THIS PROGRAM GENERATES A SERIES OF
- 20 REM DATA POINTS, WITH WHICH THE USER CAN
- 30 REM PLOT CURVES. THE DATA POINTS GENE-RATED
- 40 REM LIE BETWEEN THE VALUES GIVEN FOR X
- 50 REM IF A STEP SIZE OTHER THAN 1 IS DERIVED
- 60 REM USE A STEP STATEMENT WITH THE FOR STATEMENTS
- 70 PRINT "STARTING VALUE OF X = ";
- 80 INPUT X
- 90 PRINT "END VALUE OF X =";
- 100 INPUT W
- 110 PRINT "TABLE"
- 120 PRINT "X", "Y"
- 130 FOR I = X TO W
- 140 LET Y =
- 150 PRINT I, Y
- 160 NEXT I
- 170 PRINT
- 180 PRINT "TYPE 1 TO CONTINUE,0 TO STOP"
- 190 INPUT L
- 200 IF L = 1 THEN 220
- 210 STOP
- 220 PRINT
- 230 GOTO 70
- 240 END

## DAY OF THE WEEK

This computer program computes the day of the week (e.g., Monday) from the date entered. The date entered must not be prior 1753, this is due to changes involving the switch-over from the Julian to the Gregorian Calandar.

```
RUN
ENTER DAY(D), MONTH(M) AND YEAR(Y)
?
16,02,1977
THE DAY OF THE WEEK IS WEDNESDAY
FOR NEXT DATE IN YES, IF NOT
TYPE NO
?
NO
DAY OF THE WEEK SAYS GOOD-BYE
*END
```



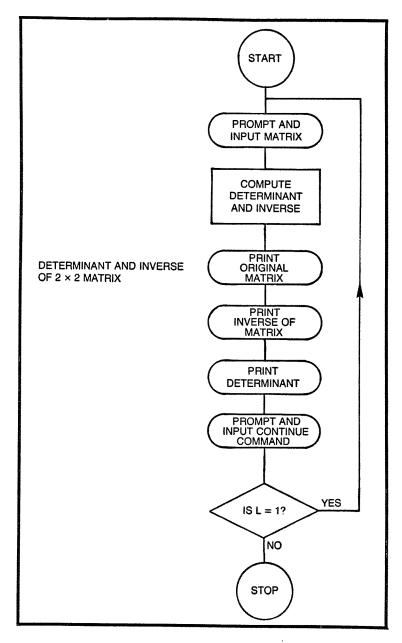
#### DAY OF THE WEEK

- 10 REM THIS PROGRAM COMPUTES THE DAY OF THE WEEK
- 20 REM RESTRICTION: THE DATE MUST BE AFTER 1752
- 30 LET J\$(1) = "SUNDAY"
- 40 LET J\$(2) = "MONDAY"
- 50 LET J\$(3) = "TUESDAY"
- 60 LET J\$(4) = "WEDNESDAY"
- 70 LET J\$(5) = "THURSDAY"
- 80 LET J\$(6) = "FRIDAY"
- 90 LET J\$(7) = "SATURDAY"
- 100 PRINT "ENTER DAY(D), MONTH(M) and YEAR(Y)"
- 110 INPUT D, M, Y
- 120 IF Y > 1752 THEN 150
- 130 PRINT "YEAR MUST NOT BE PRIOR TO 1753"
- 140 GOTO 100
- 150 LET K = INT(0.6 + (1/M))
- 160 LET L = Y K
- 170 LET O = M + 12\*K
- 180 LET P = L/100
- 190 LET Z1 = INT(P/4)
- 200 LET Z2 = INT(P)
- 210 LET Z3 = INT((5\*L)/4)
- 220 LET Z4 = INT (13\*(O + 1)/5)
- 230 LET Z = Z4 + Z3 Z2 + Z1 + D 1
- 240 LET Z=Z (7\*INT(Z/7)) + 1
- 250 PRINT "THE DAY OF THE WEEK IS"; J\$(Z)
- 260 PRINT
- 270 PRINT "FOR NEXT DATE TYPE IN YES, IF NOT"
- 280 PRINT "TYPE NO"
- 290 INPUT L\$
- 300 IF L\$ = "YES" THEN 340
- 310 IF L\$ = "NO" THEN 360
- 320 PRINT "INVALID COMMAND"
- 330 GOTO 270
- 340 PRINT
- 350 GOTO 30
- 360 PRINT "DAY OF THE WEEK SAYS GOOD-BYE"
- 370 END

# DETERMINANT AND INVERSE OF A 2 $\times$ 2 MATRIX

The computer computes the inverse and determinant of a  $2 \times 2$  matrix supplied by the user.

```
ENTER A11,A12
5,3
ENTER A21,A22
2,1
ORIGINAL MATRIX
5
    3
2
    1
INVERSE OF MATRIX
-1 4
 2 - 5
DETERMINANT = -1
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



## DETERMINANT AND INVERSE OF $2 \times 2$ MATRIX

- 10 REM THIS PROGRAM COMPUTES THE DETER-MINANT AND
- 20 REM INVERSE OF A  $2 \times 2$  MATRIX

- PRINT "ENTER A11, A12"; 30
- INPUT A,B 40
- PRINT "A21, A22"; 50
- INPUT C,D 60
- LET  $E = (D^*A) (B^*C)$ 70
- LET F = D/E80
- LET G = B/E90
- LET H = C/E100
- LET I = A/E110
- PRINT "ORIGINAL MATRIX" 120
- PRINT A,B 130
- PRINT C,D 140
- **PRINT** 150
- PRINT "INVERSE OF MATRIX" 160
- PRINT F, G 170
- PRINT H,I 180
- **PRINT** 190
- PRINT "DETERMINANT = ";E 200
- **PRINT** 210
- PRINT "TYPE 1 TO CONTINUE, 0 TO STOP" 220
- INPUT L 230
- IF L = 1 THEN 30 240
- STOP 250
- **PRINT** 260
- **GOTO 30** 270
- **END** 280

# DETERMINATE INVERSE OF A 3 imes 3 MATRIX

The user inputs his original matrix, and the computer responds with the determinate and the inverse.

#### **FORMULAE**

MATRIX = 
$$\begin{pmatrix} A_1 & B_1 & C_1 \\ A_2 & B_2 & C_2 \\ A_3 & B_3 & C_3 \end{pmatrix}$$
 DET A =  $A_1B_2C_3 + B_1C_2A_3 + C_1B_3A_2 - C_1B_2A_3 - C_2B_3A_1 - C_3A_2B_1$   
INVERSE OF MATRIX A =  $\begin{pmatrix} \alpha_1 & \beta_1 & \gamma_1 \\ \alpha_2 & \beta_2 & \gamma_2 \\ \alpha_3 & \beta_3 & \gamma_3 \end{pmatrix}$   
 $\alpha_1 = (B_2C_3 - B_3C_2)/DET A$ 

 $\alpha_2 = (A_3C_2 - A_2C_3)/DET A$ 

 $\alpha_3 = (A_2B_3 - A_3B_2)/DET A$  $\beta_1 = (B_3C_1 - B_1C_3)/DET A$ 

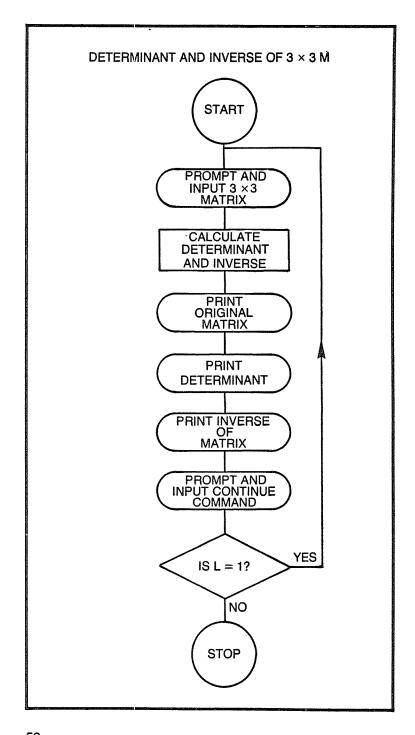
 $\beta_2 = (A_1C_3 - A_3C_1)/DET A$  $\beta_3 = (A_3B_1 - A_1B_3)/DET A$ 

 $\gamma_1 = (B_1C_2 - B_2C_1)/DET A$ 

 $\gamma_2 = (A_2C_1 - A_1C_2)/DET A$ 

 $\gamma_3 = (A_1B_2 - A_2B_1)/DET A$ 

```
ENTER 3X3 MATRIX
1,4,2,2,4,2,3,5,1
ORIGINAL MATRIX
142
242
351
DETERMINANT = 6
INVERSE OF MATRIX
-110
.67 - .83 .33
-.331.17 - .67
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



## DETERMINANT AND INVERSE OF 3 × 3 MATRIX

- 10 REM THIS PROGRAM COMPUTES 3 × 3 MATRIX OPERATIONS
- 20 PRINT "ENTER  $3 \times 3$  MATRIX"
- 30 INPUT A,B,C,D,E,F,G,H,I
- 40 REM COMPUTE DETERMINANT OF 3\*3
- 50 LET M = (A\*E\*I) + (B\*F\*G) + (C\*H\*D)
- 60 LET  $N = M (C^*E^*G) (F^*H^*A) (I^*D^*B)$
- 70 REM COMPUTE INVERSE
- 80 LET O = ((E\*I) (H\*F))/N
- 90 LET P = ((G\*F) (D\*I))/N
- 100 LET  $Q = ((D^*H) (G^*E))/N$
- 110 LET R = ((H\*C) (B\*I))/N
- 120 LET S = ((A\*I) (G\*C))/N
- 130 LET T = ((G\*B) (A\*H))/N
- 140 LET U = ((B\*F) (E\*C))/N
- 150 LET V = ((D\*C) (A\*F))/N
- 160 LET W = ((A\*E) (D\*B))/N
- 170 PRINT "ORIGINAL MATRIX"
- 180 PRINT A,B,C
- 190 PRINT D, E, F
- 200 PRINT G,H,I
- 210 PRINT
- 220 PRINT "DETERMINANT = ":N
- 230 PRINT
- 240 PRINT "INVERSE OF MATRIX"
- 250 PRINT O.R.U
- 260 PRINT P,S,V
- 270 PRINT Q,T,W
- 280 PRINT
- 290 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 300 INPUT L
- 310 IF L = 1 THEN 20
- 320 STOP
- 330 END

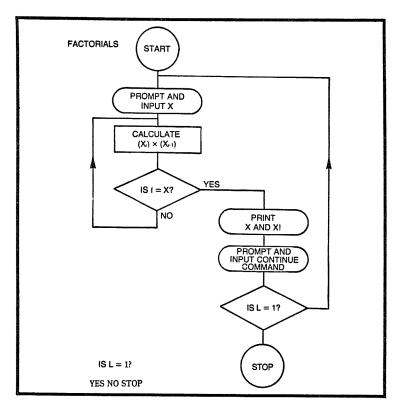
## **FACTORIALS**

This program computes by iterative multiplication of the factorial of X.

## **FORMULA**

$$(X)(X-1)(X-2)...(X-X+1)$$

```
X = ?
5
X = 5 X! = 120
TYPE 1 TO CONTINUE,0 TO STOP
?
1
X = ?
7
X = 7 X! = 5040
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
X = ?
1
X = ?
1
X = ?
18
X = 18 X! = 6.40237E15
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



## **FACTORIALS**

- 10 REM THIS PROGRAM COMPUTES THE FACTORIALS OF X
- 20 REM BY ITERATIVE MULTIPLICATIONS
- 30 PRINT "X =";
- 40 INPUT X
- 50 LET Z = 1
- FOR I = 1 TO X
- 70 LET Z = Z\*I
- 80 NEXT I
- 90 PRINT "X = "; X, "X! = "; Z
- 100 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 110 INPUT L
- 120 IF L = 1 THEN 140
- 130 STOP
- 140 PRINT
- 150 GOTO 30
- 160 END

#### FIBONACCI NUMBERS

This program computes a table of Fibonacci numbers from the first two terms entered by the user, who may also specify the maximum number of terms.

#### **FORMULA**

 $F_I = i^{th}$  term in the sequence;

For any two terms the

first term =  $f_i - 2$ ,

second term =  $f_i - 1$  $f_i = f_{i-1} + f_{i-2}$ 

## EXAMPLE

ENTER 1ST TERM

1

ENTER 2ND TERM

MAXIMUM NUMBER OF TERMS =

10

TABLE OF FIBONACCI NUMBERS

TERM NO.	
1	
2	
3	
4	
5	
6	
7	
8	
9	

FIBONACCI NUMBERS

13 21

34

55

MAXIMUM NUMBER OF TERMS REACHED

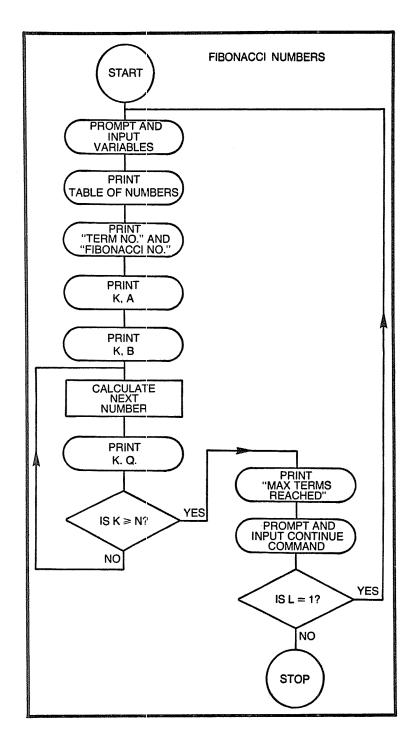
TYPE 1 TO CONTINUE, 0 TO STOP

10

ENTER FIRST TERM

27

```
ENTER SECOND TERM
963
MAXIMUM NUMBER OF TERMS =
TABLE OF FIBONACCI NUMBERS
                   FIBONACCI NUMBERS
   TERM NO.
    1
                   27
    2
                   963
    3
                   990
    4
                   1953
    5
MAXIMUM NUMBER OF TERMS REACHED
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



## FIBONACCI NUMBERS

- 10 REM THIS PROGRAM COMPUTES A TABLE OF FIBONACCI NUMBERS
- 20 PRINT "ENTER FIRST TERM"
- 30 INPUT A
- 40 PRINT "ENTER SECOND TERM"
- 50 INPUT B
- 60 PRINT "MAXIMUM NUMBER OF TERMS = "
- 70 INPUT N
- 80 PRINT
- 90 PRINT "TABLE OF FIBONACCI NUMBERS"
- 100 PRINT "TERM NO.", "FIBONACCI NUMBER"
- 110 LET K = 1
- 120 PRINT K.A
- 130 LET K = 2
- 140 PRINT K.B
- 150 LET K = K + 1
- 160 LET Q = A + B
- 170 PRINT K.Q
- 180 LET A = B
- 190 LET B = Q
- 200 IF K > = N THEN 220
- 210 GOTO 150
- 220 PRINT "MAXIMUM NUMBER OF TERMS REACHED"
- 230 PRINT
- 240 PRINT "TYPE 1 TO CONTINUE. 0 TO STOP"
- 250 INPUT L
- 260 IF L = 1 THEN 280
- 270 STOP
- 280 PRINT
- 290 GOTO 20
- 300 END

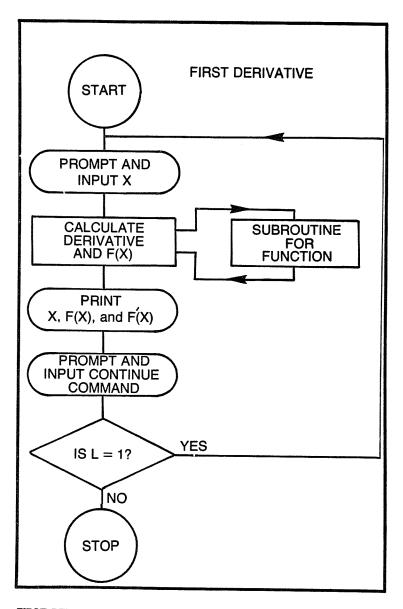
#### FIRST DERIVATIVE

The user must supply the expression to complete the assignment statement in line 280. The computer will then derive the first derivative of the supplied equation.

### **FORMULA**

$$f^{1}(x) = \frac{f(x + \Delta x/2) - f(x - \Delta x/2)}{\Delta x}$$

```
(ASSUMING THE EQUATION IS X<sup>†</sup>2)
VALUE OF X =
?
10
IF X = 10 THEN F(X) = 100
AND F'(X) = 20
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
VALUE OF X =
?
20
IF X = 20 THEN F(X) = 400
AND F'(X) = 40
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



## FIRST DERIVATIVE

- 10 REM THIS PROGRAM COMPUTES THE FIRST DE-RIVATIVE
- 20 REM OF A FUNCTION ENTERED BY THE USER
- 30 PRINT "VALUE OF X =":
- 40 INPUT y

- 50 LET Y = X
- 60 LET Z = (X\*(1E 04))/2
- 70 LET W = X + Z
- 80 LET V = X Z
- 90 LET X = W
- 100 GOSUB 280
- 110 LET A = P
- 120 LET X =V
- 130 GOSUB 280
- 140 LET B = P
- 150 LET X = Y
- 160 GOSUB 280
- 170 LET C = P
- 180 LET F = (A B)/2\*Z
- 190 PRINT "IF X = "; Y, "THEN F(X) = "; C
- 200 PRINT "AND F' (X) = ";F
- 210 PRINT
- 220 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 230 INPUT L
- 240 IF L = 1 THEN 260
- 250 STOP
- 260 PRINT
- 270 GOTO 40
- 280 LET P =
- 290 RETURN
- 300 END

## **GAMMA FUNCTION AND GENERALIZED FACTORIAL**

This program computes both the gamma function and the generalized factorial via polynomial approximation.

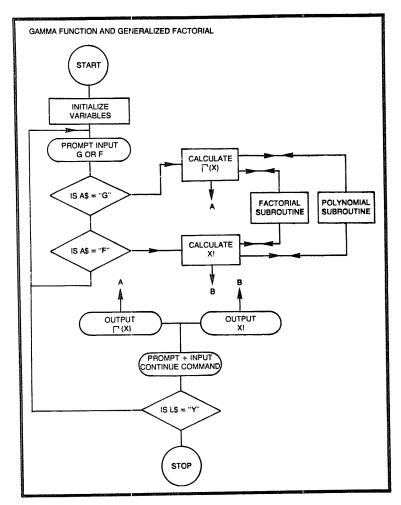
#### **FORMULAE**

$$\Gamma(X) = \int_{0}^{\infty} t^{x-1} e^{-t} dt$$

$$\Gamma(X) \cong (1 + A_1(Y) + A_2(Y)^2 \dots A_8(Y)^8) Z$$

```
where Y = \text{fractional part of } X
where Z = (X - 1)(X - 2)....(X - N)
and X - N = 1 + Y
```

```
RIIN
TYPE G FOR THE GAMMA FUNCTION OR
TYPE F FOR THE GENERALIZED FACTORIAL
?
G
ENTER VALUE OF X
5
GAMMA (5) = 24
TO CONTINUE TYPE Y. IF NOT TYPE N
Y
TYPE G FOR THE GAMMA FUNCTION OR
TYPE F FOR THE GENERALIZED FACTORIAL
?
F
ENTER VALUE OF X
?
5
5! = 120
TO CONTINUE TYPE Y. IF NOT TYPE N
Ş
N
*END
```



## **GAMMA FUNCTION AND GENERALIZED FACTORIAL**

- 10 REM THIS PROGRAM GENERATES VIA POLY-NOMIAL
- 20 REM APPROXIMATION THE GAMMA FUNCTION
- 30 REM AND THE GENERALIZED FACTORIALS
- 40 LET A = 0.57717
- 50 LET B = 0.98821
- 60 LET C = 0.89706
- 70 LET D = 0.91821
- 80 LET E = 0.7567
- 90 LET F = 0.4822
- 100 LET G = 0.19353

```
110 LET H = 0.03587
```

- 120 PRINT "TYPE G FOR THE GAMMA FUNCTION OR"
- 130 PRINT "TYPE F FOR THE GENERALIZED FACTORIAL"
- 140 INPUT A\$
- 150 IF A\$ = "G" THEN 190
- 160 IF A\$ = "F" THEN 300
- 170 PRINT "INVALID RESPONSE"
- 180 GOTO 120
- 190 PRINT "ENTER VALUE OF X"
- 200 INPUT X
- 210 LET K = X
- 220 LET K = K 1
- 230 IF K > = 0 THEN 260
- 240 PRINT "X MUST BE EQUAL TO OR GREATER THAN 1"
- 250 GOTO 190
- 260 GOSUB 490
- 270 IF (X 1) = INT(X 1) THEN 410
- 280 GOSUB 570
- 290 GOTO 410
- 300 PRINT "ENTER VALUE OF X"
- 310 INPUT X
- $320 \qquad \text{LET K} = X$
- 330 IF K > = 0 THEN 360
- 340 PRINT "X MUST BE GREATER THAN OR EQUAL TO 0"
- 350 GOTO 300
- 360 GOSUB 490
- 370 IF X = INT(X) THEN 390
- 380 GOSUB 570
- 390 PRINT X;"! = ";K
- 400 GOTO 420
- 410 PRINT "GAMMA ("; X;") = "; K
- 420 PRINT
- 430 PRINT "TO CONTINUE TYPE Y. IF NOT TYPE N"
- 440 INPUT L\$
- 450 IF L\$ = "Y" THEN 470
- 460 STOP
- 470 PRINT
- 480 GOTO 120
- 490 LET J = 1
- LET J = J\*K

```
LET K = K - 1
510
       IF K < 1 THEN 540
520
530
       GOTO 500
       LET L = K
540
       LET K = J
550
       RETURN
560
       LET A1 = 1 + (A*L) + (B*(L\uparrow2)) + (C*(L\uparrow3))
570
       LET A1 = A1 + (D^*(L^4)) + (E^*(L^5)) + (F^*(L^6))
580
       LET A1 = A1 + (G^*(L\uparrow 7)) + (H^*(L\uparrow 8))
590
       LET K = A1*K
600
       RETURN
610
620
       END
```

## **GAUSSIAN PROBABILITY FUNCTION**

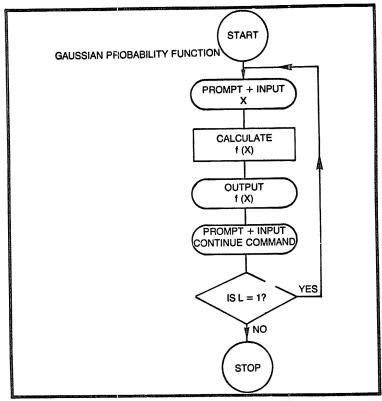
This program computes the Gaussian probability function of X.

# FORMULA

$$f(X) = \frac{1}{\sqrt{2\pi}} \quad e^{-\frac{X^2}{2}}$$

## **EXAMPLES**

```
X =
?
3.2
F(X) = .00238
TO CONTINUE TYPE 1, 0 TO STOP
1
X =
?
4
F(X) = .000133
TO CONTINUE TYPE 1, 0 TO STOP
1
X =
?
1.2
F(X) = .19418
TO CONTINUE TYPE 1, 0 TO STOP
0
*END
```



# **GAUSSIAN PROBABILITY FUNCTION**

- 10 REM THIS PROGRAM COMPUTES THE GAUSSIAN PROBABILITY
- 20 REM FUNCTION OF X
- 30 PRINT "X =";
- 40 INPUT X
- 50 LET A = EXP $(-(X \uparrow 2)/2)$
- 60 LET B = .398942
- 70 LET C = B\*A
- 80 PRINT "F(X) = ";C
- 90 PRINT
- 100 PRINT "TO CONTINUE TYPE 1, 0 TO STOP"
- 110 INPUT L
- 120 IF L = 1 THEN 140
- 130 STOP
- 140 PRINT
- 150 GOTO 30
- 160 END

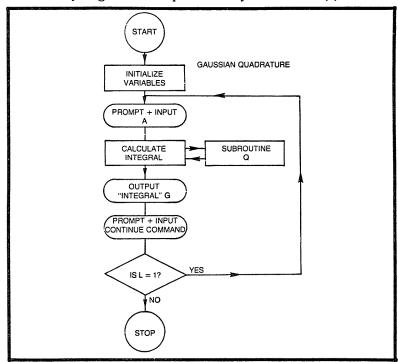
#### **GAUSSIAN QUADRATURE**

This program computes the integral f(x)dx for a finite A by the 6-point Gaussian-Legendre quadrature formula. It should be noted that f(x) must be a single-valued function.

#### **FORMULA**

$$\int_{A}^{\infty} f(x)dx = \frac{1}{2} \sum_{i=1}^{6} \frac{4D_{i}}{(I+C_{i})^{2}} f\left(\frac{2}{1+C_{i}}+A-1\right)$$
**EXAMPLE**
ENDPOINT A =
?
0
INTEGRAL = 0.92
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
\*END

The LET Q statement in line 470 must be completed by the user. Any single-valued expression may be used for f(x).



## **GAUSSIAN QUADRATURE**

- 10 REM THIS PROGRAM COMPUTES THE INTEGRAL BETWEEN A
- 20 REM AND INFINITY BY GAUSSIAN QUADRATURE
- 30 LET C1 = .238619
- 40 LET C2 = -C1
- 50 LET C3 = .661209
- 60 LET C4 = -C3
- 70 LET C5 = .932470
- 80 LET C6 = -C5
- 90 LET D1 = .467914
- $100 \quad LET D2 = .360762$
- $110 \quad \text{LET D3} = .171324$
- 120 LET I = 0
- 130 PRINT "ENDPOINT A =";
- 140 INPUT A
- 150 LET X = (2/(1 + C1)) + (A 1)
- 160 GOSUB 470
- 170 LET N =  $((4*D1)/(1 + C1)^2)*Q$
- 180 LET J = J + N
- 190 LET X = (2/(1 + C2)) + (A 1)
- 200 GOSUB 470
- 210 LET N =  $((4*D1)/(1 + C2)^2)$
- $220 \qquad \text{LET } J = J + N$
- 230 LET X = (2/(1 + C3)) + (A 1)
- 240 GOSUB 470
- 250 LET N =  $((4*D2)/(1 + C3)^2)$
- 260 LET J = J + N
- 270 LET X = (2/(1 + C4)) + (A 1)
- 280 GOSUB 470
- 290 LET N = ((4\*D2)/(1 + C4)/(2)\*Q
- $300 \quad \text{LET J} = \text{J} + \text{N}$
- 310 LET X = (2/(1 + C5)) + (A 1)
- 320 GOSUB 470
- 330 LET N =  $((4*D3)/(1 + C5)^2)^2Q$
- 340 LET J = J + N
- 350 LET X = (2/(1 + C6)) + (A 1)
- 360 GOSUB 470
- 370 LET N =  $((4*D3)/(1 + C6)^2)^2$
- $380 \qquad \text{LET J} = \text{J} + \text{N}$
- 390 LET G = J/2
- 400 PRINT "INTEGRAL = ";G

410	DDING WENDE 1 TO COMMINTIN A TO COOP!
410	PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
420	INPUT L
430	IF L = 1 THEN 450
440	STOP
450	PRINT
460	GOTO 120
470	LET Q =
480	RETURN
490	END

### **GENERALIZED MEAN**

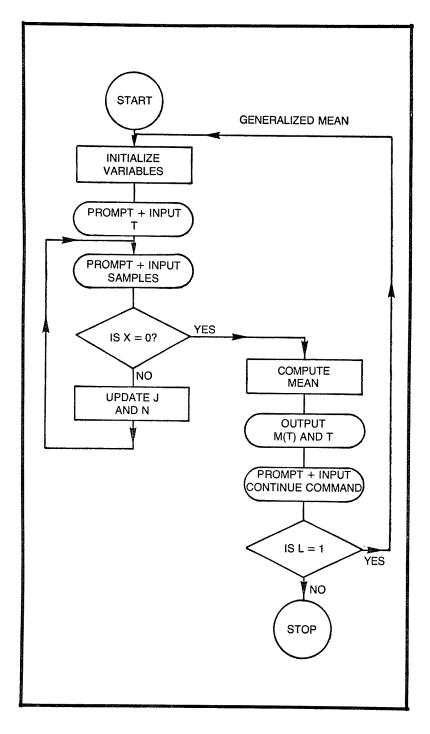
This program computes the generalized mean, which becomes equal to the arithmetic mean if the T entered by the user is 1, and equal to the harmonic mean if the user enters -1.

#### **FORMULA**

$$M(T) = \left( \begin{array}{cc} \frac{1}{N} \sum\limits_{K=1}^{N} \times {}_{K}^{T} \right)^{\frac{1}{T}} & \text{where } X > 0 \\ \end{array}$$

### **EXAMPLE**

```
T =
?
4
INPUT SAMPLE
?
5
GENERALIZED MEAN
M(T) = 5 WHERE T = 4
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



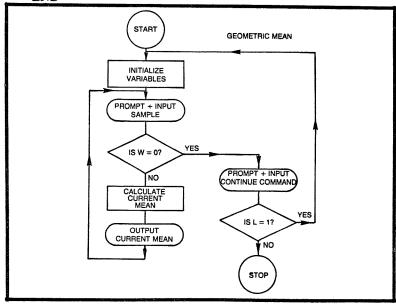
# GENERALIZED MEAN

- 10 REM THIS PROGRAM COMPUTES THE GENER-ALIZED MEAN
- 20 REM IF T = 1, THEN THE GENERALIZED MEAN M(T)
- 30 REM IS EQUAL TO THE ARITHMETIC MEAN. IF T = -1
- 40 REM THEN M(T) IS EQUAL TO THE HARMONIC MEAN
- 50 LET J = 0
- 60 LET N = 0
- 70 PRINT "T =";
- 80 INPUT T
- 90 PRINT "INPUT SAMPLE";
- 100 INPUT X
- 110 IF X = 0 THEN 150
- 120 LET  $J = J + (X \uparrow T)$
- 130 LET N = N + 1
- 140 GOTO 90
- 150 LET  $G = (J/N) \uparrow (1/T)$
- 160 PRINT "GENERALIZED MEAN"
- 170 PRINT "M(T) = "; G, "WHERE T = "; T
- 180 PRINT
- 190 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 200 INPUT L
- 210 IF L = 1 THEN 230
- 220 STOP
- 230 PRINT
- 240 GOTO 50
- 250 END

### **GEOMETRIC MEAN**

This program computes the geometric mean of the sample entered by the user until a 0 is entered for the sample.

```
FORMULA
                G = \sqrt[n]{(a_1)(a_2).....(a_n)}
EXAMPLE
SAMPLE =
2
NUMBER OF SAMPLES = 1 CURRENT SAMPLE = 2
CURRENT MEAN = 2
SAMPLE =
5
NUMBER OF SAMPLES = 2 CURRENT SAMPLE = 5
CURRENT MEAN = 3.1623
SAMPLE =
0
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



# **GEOMETRIC MEAN**

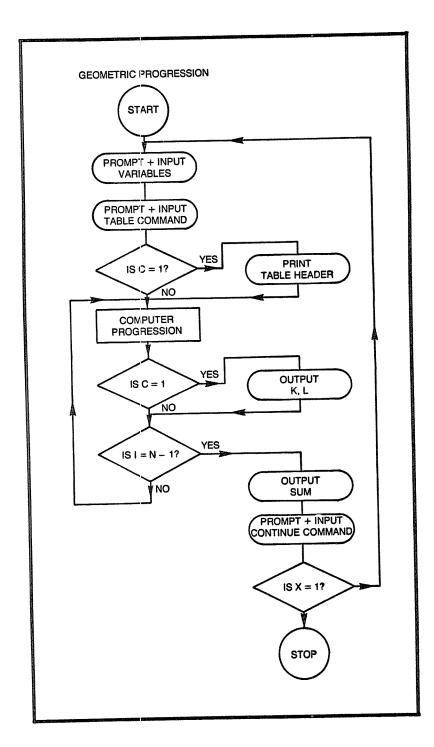
- 10 REM THIS PROGRAM COMPUTES THE GEOMETRIC MEAN
- 20 REM AFTER EACH SAMPLE IS ENTERED, THE NUMBER OF
- 30 REM SAMPLES, THE CURRENT SAMPLE AND CUR-RENT MEAN
- 40 REM IS PRINTED.
- 50 LET Y = 1
- 60 LET N = 0
- 70 PRINT "SAMPLE = ":
- 80 INPUT W
- 90 IF W = 0 THEN 160
- 100 LET N = N + 1
- 110 LET  $Y = Y^*W$
- 120 LET G = Y / (1/N)
- PRINT "NUMBER OF SAMPLES = ";N,"CURRENT SAMPLE = ";W
- 140 PRINT "CURRENT MEAN = ";G
- 150 GOTO 70
- 160 PRINT
- 170 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 180 INPUT L
- 190 IF L = 1 THEN 210
- 200 STOP
- 210 PRINT
- 220 GOTO 50
- 230 END

# **GEOMETRIC PROGRESSION**

From the following information: first term, ratio of terms, and number of terms, this program computes the geometric progression.

### **FORMULA**

```
A,AR,AR^2...AR^{N-1}
EXAMPLE
FIRST TERM =
10
RATIO OF TERMS =
2
NUMBER OF TERMS =
FOR TABLE, TYPE 1, IF NOT TYPE 0
1
GEOMETRIC PROGRESSION
TERM NUMBER
                 TERM VALUE
1
                       10
2
                       20
3
                       40
4
                       80
                       160
SUM = 310
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



## **GEOMETRIC PROGRESSION**

320

330

**GOTO 30** 

**END** 

```
10
       REM THIS PROGRAM COMPUTES THE VALUES AND
         THEIR SUM
       REM OF A GEOMETRIC PROGRESSION
 20
 30
       PRINT "FIRST TERM = ":
 40
       INPUT A
       PRINT "RATIO OF TERMS = ";
 50
 60
       INPUT R
 70
      PRINT "NUMBER OF TERMS = ":
       INPUT N
 80
      PRINT "FOR TABLE TYPE 1, IF NOT TYPE 0"
 90
100
      INPUT C
      IF C = 1 THEN 130
110
120
      GOTO 160
130
      PRINT
140
      PRINT "GEOMETRIC PROGRESSION"
150
      PRINT "TERM NUMBER";, "TERM VALUE";
160
      LET I = 0
      FOR I = 0 TO N - 1
170
180
      LET K = I + 1
      LET L = A^*(R^{\dagger}I)
190
200
      LET J = J + L
210
      IF C = 1 THEN 230
220
      GOTO 240
230
      PRINT K.L
240
      NEXT I
250
      PRINT "SUM = ":I
260
      PRINT
      PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
270
280
      INPUT X
290
      IF X = 1 THEN 310
300
      STOP
310
      PRINT
```

#### HARMONIC MEAN

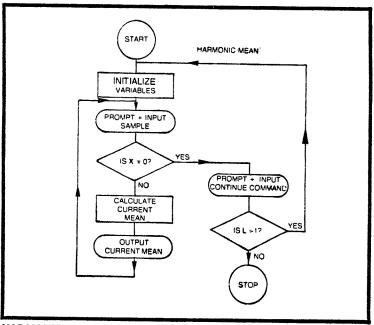
This program computes the harmonic mean of the samples entered by the user, until a 0 is entered for the sample.

#### **FORMULA**

$$H = \frac{N}{\sum_{i=1}^{N} \frac{1}{a_i}}$$

```
EXAMPLE
```

```
SAMPLE = ?
2
N = 1 SAMPLE = 2 CURRENT MEAN = 2
SAMPLE = ?
5
N = 2 SAMPLE = 5 CURRENT MEAN = 2.86
SAMPLE = ?
7
N = 3 SAMPLE = 7 CURRENT MEAN = 3.56
SAMPLE = ?
0
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



#### HARMONIC MEAN

- 10 REM THIS PROGRAM COMPUTES THE HARMONIC MEAN
- 20 REM OF THE SAMPLES ENTERED BY THE USER
- $30 \qquad \text{LET } Z = 0$
- 40 LET N = 0
- 50 PRINT "SAMPLE = ";
- 60 INPUT X
- 70 IF X = 0 THEN 130
- 80 LET N = N + 1
- 90 LET Z = Z + (1/X)
- 100 LET H = N/Z
- PRINT "N = ";N,"SAMPLE = ";X,"CURRENT MEAN = ";H
- 120 GOTO 50
- 130 PRINT
- 140 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 150 INPUT L
- 160 IF L = 1 THEN 180
- 170 STOP
- 180 PRINT
- 190 GOTO 30
- 200 END

# HARMONIC NUMBERS

This program computes the first N harmonic numbers where N is entered by the user.

# **FORMULA**

$$1, 1 + 1/2, 1 + 1/2 + 1/3, 1 + 1/2 + 1/3 + 1/4, \dots$$

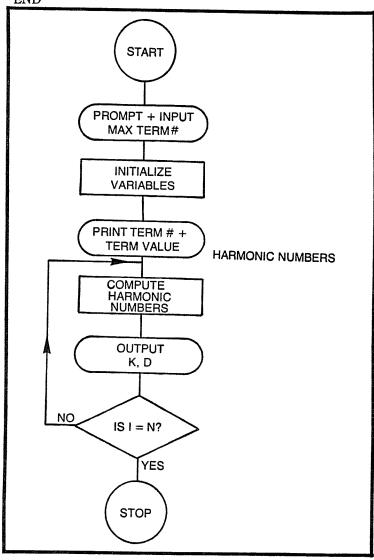
# EXAMPLE

## MAXIMUM TERM NUMBER

•	
35	
TERM NUMBER	TERM VALUE
1	1
2	1.5
3	1.83333
4	2.08333
5	2.28333
6	2.45
7	2.59285
8	2.71785
9	2.82896
10	2.92896
11	3.01987
12	3.10321
13	3.18013
14	3.25156
15	3.31822
16	3.38072
17	3.43955
18	3.49510
19	3.54774
20	3.59773
21	3.64535
22	3.69081
23	3.73429
24	3.77595
25	3.81595
26	3.85442
27	3.89145
28	3.92717
29	3.96165
30	3.99498

TERM NUMBER	TERM VALUE
31	4.02724
32	4.05849
33	4.08879
34	4.11821
35	4.14678
36	4.17456





# HARMONIC NUMBERS

- 10 REM THIS PROGRAM COMPUTES HARMONIC NUMBERS
- 20 PRINT "MAXIMUM TERM NUMBER"
- 30 INPUT N
- 40 LET K = 0
- 50 LET D = 0
- 60 PRINT "TERM NUMBER", "TERM VALUE"
- 70 FOR I = 0 TO N
- 80 LET K = I + 1
- 90 LET C = 1/K
- 100 LET D = D + C
- 110 PRINT K,D
- 120 NEXT I
- 130 PRINT
- 140 END

#### HARMONIC PROGRESSIONS

This program computes from the following information the values of A and B, the difference and the number of terms desired. At the user's option a table of progressions may be generated. In either case the sum of the number of terms is produced.

#### **FORMULA**

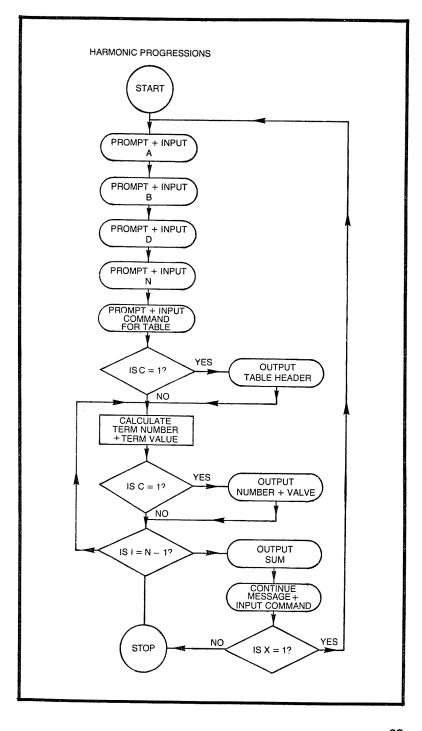
12

$$\frac{A}{B}$$
,  $\frac{A}{B+D}$ ,  $\frac{A}{B+2D,...}$   $\frac{A}{B+(N-1)D}$ 

```
EXAMPLE
VALUE OF A =
10
VALUE OF B =
2
DIFFERENCE =
3
NUMBER OF TERMS =
20
FOR TABLE TYPE 1, IF NOT TYPE 0
1
HARMONIC PROGRESSION
TERM NUMBER TERM VALUE
1
                  5
2
                  2
3
                  1.25
4
                  .90901
5
                  .714286
6
                  .588235
7
                  .5
8
                  .434783
9
                 .384615
10
                 .344828
                 .3125
11
```

.285714

```
TERM VALUE
TERM NUMBER
                    .263158
13
                    .243802
14
                    .227273
15
                    .212766
16
17
                    .2
                    .188679
18
                    .178571
19
                    .169492
20
SUM = 14.4078
**********
TYPE 1 TO CONTINUE, 0 TO STOP
7
0
*END
```



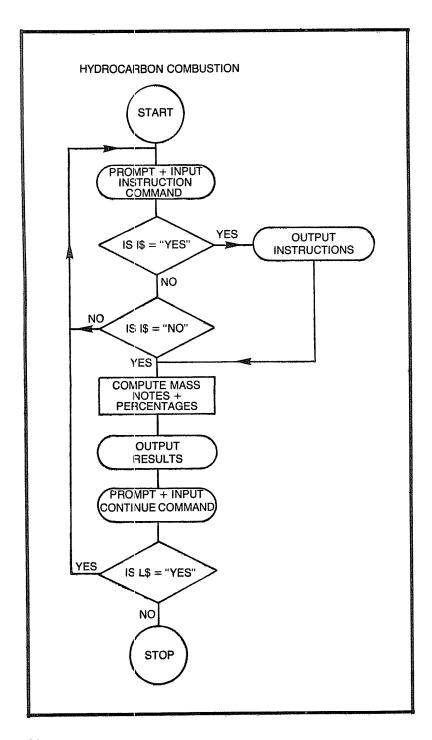
# HARMONIC PROGRESSIONS

- REM THIS PROGRAM COMPUTES A SERIES OF 10 HARMONIC
- REM PROGRESSIONS 20
- PRINT "VALUE OF A = " 30
- INPUT A 40
- PRINT "VALUE OF B = " 50
- INPUT B 60
- PRINT "DIFFERENCE = " 70
- INPUT D 80
- PRINT "NUMBER OF TERMS = " 90
- INPUT N 100
- PRINT "FOR TABLE TYPE 1, IF NOT TYPE 0" 110
- INPUT C 120
- IF C = 1 THEN 150 130
- **GOTO 170** 140
- PRINT "HARMONIC PROGRESSION" 150
- PRINT "TERM NUMBER", "TERM VALUE" 160
- 170 LETI = 0
- FOR I = 0 to N 1180
- LET K = I + 1190
- LET L = A/(B + (I\*D))200
- LET I = I + L210
- IF C = 1 THEN 240 220
- GOTO 250 230
- PRINT K,L 240
- NEXT I 250
- PRINT "SUM = ";J260
- 270
- PRINT "TYPE 1 TO CONTINUE, 0 TO STOP" 280
- INPUT X 290
- IF X = 0 THEN 320 300
- 310 STOP
- 320 **PRINT**
- GOTO 30 330
- **END** 340

#### HYDROCARBON COMBUSTION

This program simulates the burning of a hydrocarbon compound; complete combustion is assumed, and the option of excess air is available.

```
FORMULAE
AIR = 1 + \% EXCESS AIR/100
O_2 = C + S + H/4 - O/2
AF(MOLES) = O_2(4.762)AIR
AF(MASS) = 1.8094(AF MOLES)/.7507C + 0.063H
+ 2.004S + 0.875N + O
TOTAL MOLES = O_2(4.762 \text{ AIR}) + H/4 + O/2 + N/2
VOLUME % CO_2 = 100C/M
VOLUME % SO_2 = 100S/M
VOLUME % H_2O = 100H/2M
VOLUME % O_2 = 100(AIR - 1)O_2/M
VOLUME % N_2 = (100((3.762)AIR(02) + N/2)/M
EXAMPLE
RUN
FOR INSTRUCTIONS TYPE YES, IF NOT TYPE NO
NO
ENTER CARBON(C), HYDROGEN(H), OXYGEN(O), SUL-
PHUR(S), NITROGEN(N) IN THAT ORDER
1,4,0,0,0
ENTER PERCENTAGE EXCESS AIR, IF ZERO
ENTER 0, EXAMPLE: - 34% ENTER AS 34
AIR-FUEL RATIO WITH RESPECT TO MOLES = 9.52
AIR-FUEL RATIO WITH RESPECT TO MASS = 17.19
TOTAL MOLES OF PRODUCTION = 10.52
******PERCENTAGE OF VOLUME OF PRODUCETS*****
CARBON DIOXIDE = 9.50\%
SULPHUR DIOXIDE = 0.0\%
WATER = 19.0\%
OXYGEN = 0.0\%
NITROGEN = 71.49\%
*******COMPLETE COMBUSTION ASSUMED******
TO TRY NEXT COMPOUND TYPE YES
TO STOP TYPE NO
NO
COMBUSTION SAYS GOOD-BYE
*END
```



### HYDROCARBON COMBUSTION

- 10 REM THIS PROGRAM COMPUTES THE PERCENT-AGES OF THE
- 20 REM PRODUCTS PRODUCED BY HYDROCARBON COMBUSTION
- 30 PRINT "FOR INSTRUCTIONS TYPE YES, IF NOT TYPE NO"
- 40 INPUT IS
- 50 IF I\$ = "YES" THEN 90
- 60 IF I\$ = "NO" THEN 130
- 70 PRINT "INVALID COMMAND"
- 80 GOTO 30
- 90 PRINT "THE AMOUNTS OF EACH ELEMENT MUST BE"
- 100 PRINT "ENTERED, EVEN IF THE AMOUNT IS ZERO"
- 110 PRINT "EXAMPLE: METHANE (CH4) MUST BE ENTERED AS"
- 120 PRINT "C;1, H;4, O;0, S;0, N;0"
- 130 PRINT
- PRINT "ENTER CARBON(C), HYDROGEN(H), OXY-GEN(O)"
- 150 PRINT "SULPHUR(S), NITROGEN(N) IN THAT ORDER"
- 160 INPUT C,H,O,S,N
- 170 PRINT "ENTER PERCENTAGE EXCESS AIR, IF ZERO"
- 180 PRINT "ENTER 0, EXAMPLE: 34% ENTER AS 34"
- 190 INPUT E
- 200 LET E = 1 + (E/100)
- 210 LET O2 = C + S + (H/4) (O/2)
- 220 LET A = O2\*E\*4.762
- 230 LET A1 = 1.8094\*A
- 240 LET F = (0.7507\*C) + (0.063\*H) + (2.004\*S)
- 250 LET F = (0.875\*N) + O + F
- 260 LET A1 = A1/F
- 270 LET M = A + (HP4) + (O/2) + (N/2)
- 280 LET C2 = (C\*100)/M
- 290 LET S2 = (S\*100)/M
- 300 LET H2 = (H\*100)/(2\*M)
- 310 LET O3 = (100\*(E-1)\*02)/M
- 320 LET N2 = (100\*((3.762\*E\*02) + (N/2)))/M
- 330 PRINT

PRINT "AIR-FUEL RATIO WITH RESPECT TO 340 MOLES = ":APRINT "AIR-FUEL RATIO WITH RESPECT TO 350 MASS = ":A1PRINT "TOTAL MOLES OF PRODUCT = ":M 360 PRINT "\*\*\*\*\*PERCENTAGE VOLUME OF PRO-370 DUCTS\*\*\*\*\*\*" PRINT "CARBON DIOXIDE = ";C2;" % " 380 PRINT "SULPHUR DIOXIDE = ";S2;" % " 390 PRINT "WATER = ";H2;" % " 400 PRINT "OXYGEN = ":03;" % " 410 PRINT "NITROGEN = ";N2;" % " 420 PRINT "\*"\*\*\*\*COMPLETE COMBUSTION AS-430 SUMED\*\*\*\*\*\* PRINT 440 PRINT "TO TRY NEXT COMPOUND TYPE YES" 450 PRINT "TO STOP TYPE NO" 460 470 INPUT L\$ IF L\$ = "YES" THEN 510 480 PRINT "COMBUSTION SAYS GOOD-BYE" 490 500 STOP **PRINT** 510 520 GOTO 30

530

END

## HYPERBOLIC FUNCTIONS

This program computes the following hyperbolic trigonometric functions: sinH, cosH, tanH, cscH, secH, cotH.

## **FORMULAE**

$$sinHx = \frac{e^{x} - e^{-x}}{2} \qquad cscHx = \frac{1}{sinHx}$$

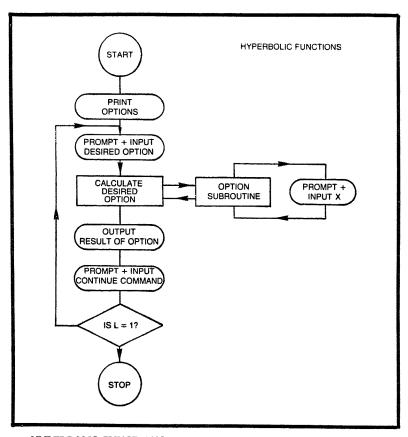
$$cosH x = \frac{e^{x} + e^{-x}}{2} \qquad secH x = \frac{1}{cosHx}$$

$$tanH x = \frac{e^{x} - e^{-x}}{e^{x} + e^{-x}} \qquad cotH x = \frac{1}{tanHx}$$

## **EXAMPLE**

```
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
1
X =
SINH 4 = 27.2899
TYPE 1 TO CONTINUE, 0 TO STOP
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
2
X =
COSH 5 = 74.2099
TYPE 1 TO CONTINUE, 0 TO STOP
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
X =
.02
TANH .02 = .019997
```

```
TYPE 1 TO CONTINUE, 0 TO STOP
1
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
4
X =
3.5
CSCH 3.5 = .060449
TYPE 1 TO CONTINUE, 0 TO STOP
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
5
X =
12
SECH 12 = .000012
TYPE 1 TO CONTINUE, 0 TO STOP
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
6
X =
.3
COTH .3 = 3.43273
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



### HYPERBOLIC FUNCTIONS

- 10 REM THIS PROGRAM COMPUTES HYPERBOLIC FUNCTIONS
- 20 PRINT "SINH (1)"
- 30 PRINT "COSH (2)"
- 40 PRINT "TANH (3)"
- 50 PRINT "CSCH (4)"
- 60 PRINT "SECH (5)"
- 70 PRINT "COTH (6)"
- 80 PRINT "TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED"
- 90 INPUT C
- 100 ON C GOTO 110,160,200,270,320,370
- 110 GOSUB 490
- 120 GOSUB 520
- 130 LET Z = Y/2

```
PRINT "SINH"; X; ="; Z
140
150
      GOTO 420
160
      GOSUB 490
      GOSUB 540
170
      LET Z = B/2
180
      PRINT "COSH";X;" = ";Z
190
200
      GOTO 420
      GOSUB 490
210
      GOSUB 520
220
      GOSUB 540
230
      LET Z = Y/B
240
      PRINT "TANH";X;" = ";Z
250
      GOTO 420
260
      GOSUB 490
270
      GOSUB 520
280
290
      LET Z = 1/(Y/2)
      PRINT "CSCH";X;" = ";Z
300
      GOTO 420
310
      GOSUB 490
320
      GOSUB 540
330
      LET Z = 1/(B/2)
340
      PRINT "SECH";X;" = ";Z
350
       GOTO 420
360
      GOSUB 490
370
       GOSUB 520
380
       GOSUB 540
390
       LET Z = 1/(Y/B)
400
       PRINT "COTH";X;" = ";Z
410
420
       PRINT
       PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
430
       INPUT L
440
       IF L = 1 THEN 470
 450
       STOP
 460
 470
       PRINT
 480
       GOTO 80
       PRINT "X = "
 490
       INPUT X
 500
 510
       RETURN
       LET Y = EXP(X) - EXP(-X)
 520
 530
       RETURN
       LET B = \mathbb{E}XP(X) + EXP(-X)
 540
 550
       RETURN
```

560

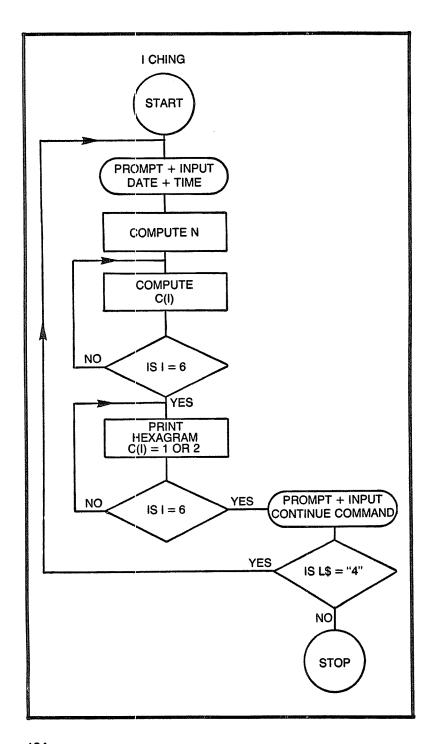
**END** 

# I CHING (THE CHINESE BOOK OF CHANGES)

The I Ching is a collection of 64 hexagrams used to determine possible future events. It was inspired by the ancient Chinese. Each hexagram consists of six lines which may be broken (--) or unbroken(---). The user of the I Ching may throw coins or sticks to produce the six lines. This program computes the six lines randomly on an algorithm using the date and time. The meanings of each of the possible 64 hexagrams may be looked up in the Chinese Book of Changes (The I Ching).

#### **EXAMPLE**

```
RUN
ENTER DATE AS M,D,Y
?
8,28,1977
ENTER TIME AS H,M(24 HOUR CLOCK)
?
9,56
--
--
--
TO CONTINUE TYPE Y, IF NOT TYPE N
?
N
THE I CHING SAYS GOOD-BYE
*END
```



## I CHING

- 10 REM THIS PROGRAM SIMULATES THE I CHING
- 20 RANDOMIZE
- 30 PRINT "ENTER DATE AS M.D.Y"
- 40 INPUT M, D, Y
- 50 PRINT "ENTER TIME AS H,M(24 HOUR CLOCK)"
- 60 INPUT H.M1
- 70 LET N = M + (D/30) + (Y/100) + H + (M1/60)
- 80 FOR I = 1 TO 6
- 90 LET K = N\*RND(0)
- 100 LET K = K INT(K)
- 110 LET C(I) = 1 + INT(2\*K)
- 120 NEXT I
- 130 FOR I = 1 TO 6
- 140 IF C(I) = 1 THEN 170
- 150 PRINT "---"
- 160 GOTO 180
- 170 PRINT "--"
- 180 NEXT I
- 190 PRINT
- 200 PRINT "TO CONTINUE TYPE Y, IF NOT TYPE N"
- 210 INPUT L\$
- 220 IF L\$ = "Y" THEN 250
- 230 PRINT "THE I CHING SAYS GOOD-BYE"
- 240 STOP
- 250 PRINT
- 260 GOTO 30
- 270 END

### INTEGRAL BETWEEN TWO LIMITS

This program computes the integral between the limits of finite points A and B for single-valued function f(x) by the six-point Gauss-Legendre quadrature formula.

#### **FORMULA**

$$\int_{a}^{b} f(x)dx = \frac{b-a}{2} \sum_{i=1}^{b} D_{i} f_{i} \frac{(C_{i}(b-a)+b+a)}{2}$$

### **EXAMPLE**

```
Where f(x) = 13*X^2 - 6*X^2 + SIN(X) + 1/X)

ENTER ENDPOINTS A,B

?

- 1,1

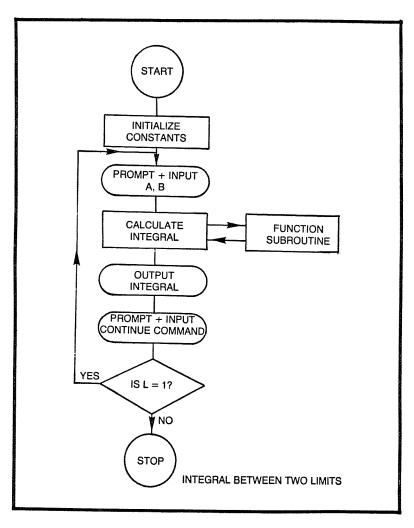
INTEGRAL = 4.28786

TYPE 1 TO CONTINUE, 0 TO STOP

?

0

*END
```



# INTEGRAL BETWEEN TWO LIMITS

- 10 REM THIS PROGRAM COMPUTES THE INTEGRAL BETWEEN
- 20 REM THE LIMITS A AND B OF F(X)
- 30 LET C1 = .238619
- 40 LET C2 = C1
- 50 LET C3 = .661209
- 60 LET C4 = C3
- 70 LET C5 = .932470
- 80 LET C6 = C5
- 90 LET D1 = .467914

```
100
      LET D2 = .360762
110
      LET D3 = .171324
      LET J = 0
120
      PRINT "ENTER ENDPOINTS A,B"
130
      INPUT A.B
140
      LET Y = B - A
150
```

LET Z = B + A160

170 LET X = ((C1\*Y) + Z)/2

180 GOSUB 500

LET N = D1\*Q190

200 LET I = I + N

LET X = ((C2\*Y) + Z)/2210

220 GOSUB 500

LET N = D1\*Q230

LET J = J + N240

LET X = ((C3\*Y) + Z)/2250 GOSUB 500

260 LET N = D2\*Q270

LET J = J + N280

LET X = ((C4\*Y) + Z)/2290

GOSUB 500 300

LET N = D2\*Q310

LET J = J + N320

LET X = ((C5\*Y) + Z)/2330

340 GOSUB 500

LET N = D3\*Q350

LET J = J + N360

LET X = ((C6\*Y) + Z)/2370

GOSUB 500 380

390 LET N = D3\*Y

LET J = J + N400

LET G = (Y/2)\*J410

PRINT "INTEGRAL = ";G420

430 **PRINT** 

PRINT "TYPE 1 TO CONTINUE, 0 TO STOP" 440

INPUT L 450

IF L = 1 THEN 480 460

**STOP** 470

480 **PRINT** 

490 GOTO 120

LET Q =  $13*X^2 - 6*X^2 + SIN(X) + 1/X$ 500

RETURN 510

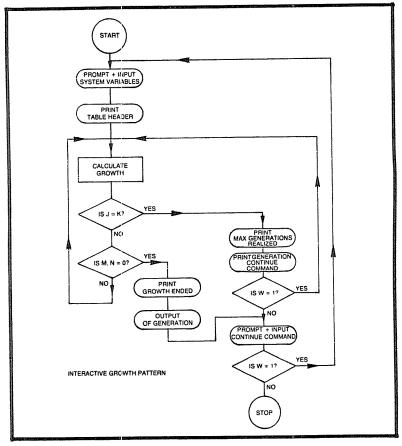
520 END

### INTERACTIVE GROWTH PATTERN

This program computes a growth pattern between two quantities called X and Y, where the existence of Y depends on the destruction of an X, but to be just, X can propagate.

```
NUMBER OF DESTROYERS (Y) =
201
NUMBER OF CREATORS (X) =
347
PROPAGATION RATE OF X =
CHANCE OF MEETING BETWEEN X AND Y =
.01
TIME BETWEEN SAMPLE DISPLAYED =
.5
MAXIMUM GENERATIONS =
10
INTERACTIVE GROWTH PATTERN
CREATOR
                  DESTROYER
1039
                   449
1822
                   2558
0
                  24600
0
                  12300
0
                  6150
0
                  3075
0
                  1537
0
                  768
0
                  384
                  192
MAXIMUM NUMBER OF GENERATIONS REACHED
FOR FURTHER GENERATIONS, TYPE 1, IF NOT 0
?
MAXIMUM GENERATIONS =
```

```
10
0
                   96
0
                   48
0
                   24
0
                   12
0
                   6
                   3
0
0
0
ALL GROWTH ENDED
NUMBER OF GENERATIONS = 18
FOR NEXT PATTERN TYPE 1, 0 TO STOP
0
*END
```



#### INTERACTIVE GROWTH PATTERN

- 10 REM THIS PROGRAM COMPUTES THE GROWTH PATTERN BETWEEN
- 20 REM A QUANTITY Y THE DESTROYER AND A QUANTITY X
- 30 REM THE CREATOR, X CAN PROPAGATE, AND ON A
- 40 REM CHANCE METTING BETWEEN X AND Y, X IS DESTROYED.
- 50 REM THUS INCREASING THE NUMBER OF YS.
- 60 PRINT "NUMBER OF DESTROYERS (Y) = ":
- 70 INPUT Y
- 80 PRINT "NUMBER OF CREATORS (X) = ":
- 90 INPUT X
- 100 PRINT "PROPAGATION RATE OF X = ":
- 110 INPUT Z
- PRINT "CHANCE OF METTING BETWEEN X AND Y = ":
- 130 INPUT A
- 140 PRINT "TIME BETWEEN SAMPLES = ":
- 150 INPUT H
- 160 PRINT "MAXIMUM GENERATIONS = ":
- 170 INPUT K
- $180 \qquad \text{LET J} = 0$
- 190 PRINT
- 200 PRINT "INTERACTIVE GROWTH PATTERN"
- 210 PRINT
- 220 PRINT "CREATOR", "DESTROYER"
- 230 IF J = K THEN 470
- 240 LET J = J + 1
- 250 LET B = A\*X\*Y
- 260 LET C = ((Y B)\*H) + Y
- 270 IF C < 0 THEN 390
- $280 \qquad \text{LET Y} = C$
- 290 LET D = (((X\*Z) B)\*H) + X
- 300 IF D < 0 THEN 140
- 310 LET X = D
- 320 LET M = INT(X)
- 330 LET N = INT(Y)
- 340 PRINT M,N
- 350 IF M = 0 THEN 370
- 360 GOTO 230
- 370 IF N = 0 THEN 430
- 380 GOTO 230

LET Y = 0390 **GOTO 290** 400 LET X = 0410 420 **GOTO 320** PRINT "ALL GROWTH ENDED" 430 PRINT "NUMBER OF GENERATIONS = ":J 440 PRINT 450 **GOTO 560** 460 PRINT "MAXIMUM NUMBER OF GENERATIONS 470 REACHED" **PRINT** 480 PRINT "FOR FURTHER GENERATIONS TYPE 1, IF 490 NOT 0" INPUT W 500 IF W = 1 THEN 530 510 520 **GOTO 560** PRINT "MAXIMUM GENERATIONS = ": 530 540 INPUT K **GOTO 230** 550 **PRINT** 560 PRINT "FOR NEXT PATTERN TYPE 1, 0 TO STOP" 570 INPUT W 580 IF W = 1 THEN 610 590 **STOP** 600 PRINT

610 620

630

**GOTO 60** 

END

### **INVERSE HYPERBOLIC FUNCTIONS**

This program computes the following hyperbolic trigonometric functions:  $sinH^{-1}$ ,  $cosH^{-1}$ ,  $tanH^{-1}$ ,  $cosH^{-1}$ ,  $secH^{-1}$   $cotH^{-1}$ 

#### **FORMULAE**

$$\sin H^{-1}x = \ln(X + (x^{2} + 1)^{.5})$$

$$\cos H^{-1}x = \ln(x + (x^{2} - 1)^{.5})$$

$$\tan H^{-1}x = \frac{1}{2}\ln\left(\frac{1+x}{1-x}\right)$$

$$\csc H^{-1}x = \sin H^{-1}\left(\frac{1}{x}\right)$$

$$\sec H^{-1}x = \cos H^{-1}\left(\frac{1}{x}\right)$$

$$\cot H^{-1}x = \tan H^{-1}\left(\frac{1}{x}\right)$$

```
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED

1

X =

?

12

SINH - 1 12 = 3.17979

TYPE 1 TO CONTINUE, 0 TO STOP

?

1

TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED

?

2

X =

?

45

COSH - 1 45 = 4.49969

TYPE 1 TO CONTINUE, 0 TO STOP

?

1

TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED

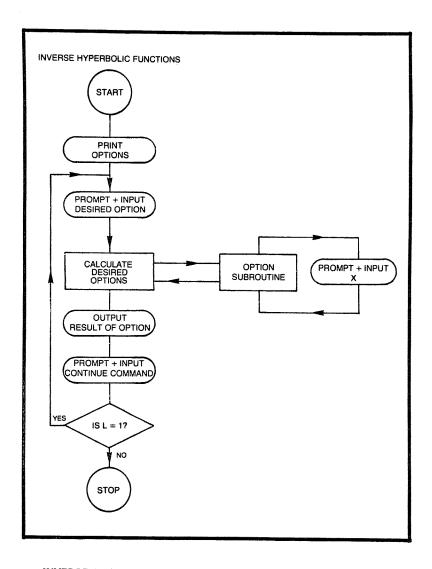
?

1

TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED

?
```

```
X =
?
.00055
TANH - 1.00055 = .00055
TYPE 1 TO CONTINUE, 0 TO STOP
1
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
4
X =
?
23
CSCH - 123 = .04346
TYPE 1 TO CONTINUE, 0 TO STOP
1
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
5
X =
.125
SECH - 1.125 = 2.76866
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
TYPE A NUMBER 1 TO 6 FOR FUNCTION DESIRED
5
6
X =
COTH - 18 = .12566
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



### **INVERSE HYPERBOLIC FUNCTIONS**

- 10 REM THIS PROGRAM COMPUTES INVERSE HYPER-BOLIC FUNCTIONS
- 20 PRINT "SINH -1 (1)"
- 30 PRINT "COSH 1 (2)"
- 40 PRINT "TANH 1 (3)"
- 50 PRINT "CSCH 1 (4)"
- 60 PRINT "SECH 1 (5)"
- 70 PRINT "COTH 1 (6)"

```
PRINT "TYPE A NUMBER 1 TO 6 FOR FUNCTION
80
        DESIRED"
      INPUT C
90
      ON C GOTO 110,150,190,230,280,330
100
      GOSUB 440
110
      GOSUB 470
120
      PRINT "SINH -1"; X;" = ":Z
130
      GOTO 370
140
      GOSUB 440
150
      GOSUB 490
160
      PRINT "COSH -1";X;" = ";Z
170
180
      GOTO 370
      GOSUB 440
190
      GOSUB 510
200
      PRINT "TANH -1"; X; = "; Z
210
220
       GOTO 370
       GOSUB 530
230
       GOSUB 470
240
       LET X = A
250
      PRINT "CSCH -1";X;" = ";Z
260
270
       GOTO 370
       GOSUB 530
280
       GOSUB 490
290
       LET X = A
300
       PRINT "SECH -1"; X;" = "; Z
310
320
       GOTO 370
       GOSUB 530
330
340
       GOSUB 510
       LET X = A
350
       PRINT "COTH -1";X:" = ":Z
360
       PRINT
370
       PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
380
       INPUT L
 390
       IF L = 1 THEN 420
 400
       STOP
 410
       PRINT
 420
       GOTO 80
 430
       PRINT "X = ";
 440
       INPUT X
 450
       RETURN
 460
       LET Z = LOG(X + SQR((X^{\dagger}2) + 1))
 470
       RETURN
 480
       LET Z = LOG(X + SQR((X^{\bullet}2) - 1))
 490
```

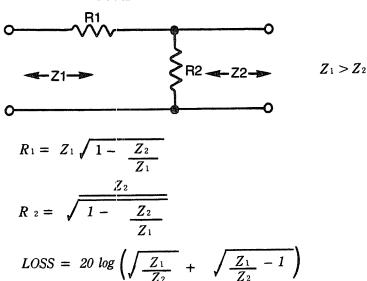
- 500 RETURN
- 510 LET Z = (LOG((1 + X/(1 X)))/2
- 520 RETURN
- 530 PRINT "X = ";
- 540 INPUT X
- 550 LET A = X
- 560 LET X = 1/X
- 570 RETURN
- 580 END

### L-PAD MINIMUM LOSS SYSTEM

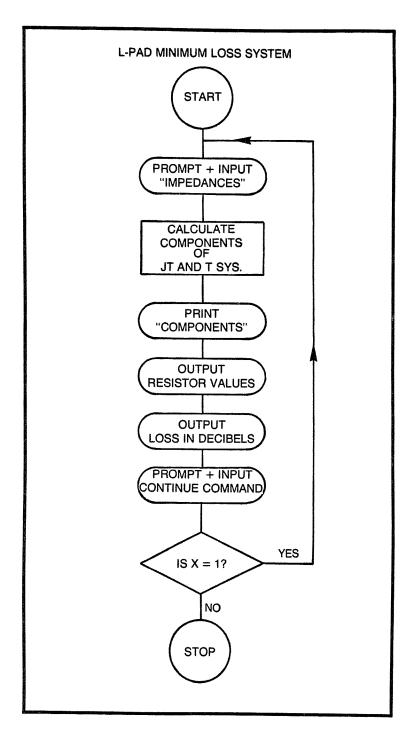
In systems where two resistive stages must be coupled, a minimum loss L-pad can be used for matching. A typical application for this pad would be to couple inputs and outputs of audio circuits. The user inputs the two impedances  $Z_1$  and  $Z_2$ ; the program responds with the L-pad resistors  $R_1$  and  $R_2$ , and also the system loss in decibels.

### **FORMULAE**





```
1ST IMPEDANCE
?
300
2ND IMPEDANCE
?
75
COMPONENTS OF THE L-PAD
RESISTOR 1 = 259.807
RESISTOR 2 = 86.6025
LOSS IN DECIBELS = 11.4389
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



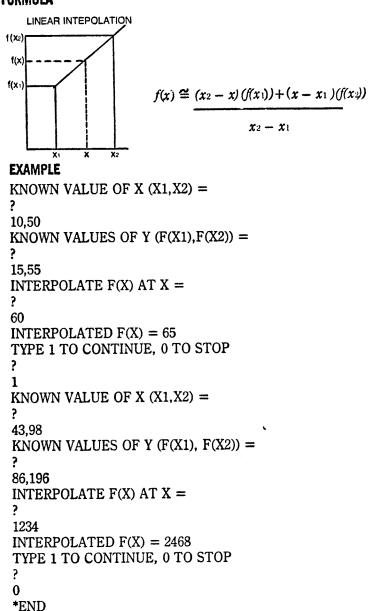
## L-PAD MINUMUM LOSS SYSTEM

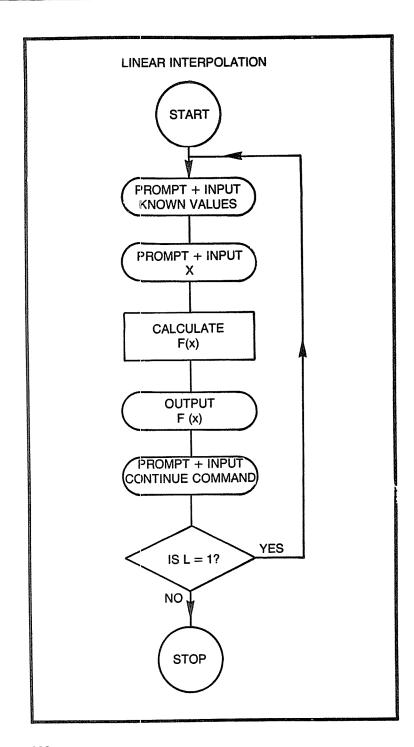
- 10 REM THIS PROGRAM COMPUTES THE VALUES OF
- 20 REM THE TWO RESISTANCES REQUIRED TO CON-STRUCT A
- 30 REM L-PAD OF MINIMUM LOSS
- 40 PRINT "1ST IMPEDANCE"
- 50 INPUT Z1
- 60 PRINT "2ND IMPEDANCE"
- 70 INPUT Z2
- 80 LET R1 = Z1\*SQR(1 (Z2/Z1))
- 90 LET R2 = Z2/SQR(1 (Z2/Z1))
- 100 LET M = SQR(Z1/Z2) + SQR((Z1/Z2) 1)
- 110 LET L =  $20^{\circ}(LOG(M)/LOG(10))$
- 120 PRINT "COMPONENTS OF THE L-PAD"
- 130 PRINT "RESISTOR 1 = ";R1
- 140 PRINT "RESISTOR 2 = ";R2
- 150 PRINT "LOSS IN DECIBELS = ";L
- 160 PRINT
- 170 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 180 INPUT X
- 190 IF X = 1 THEN 210
- 200 STOP
- 210 PRINT
- 220 GOTO 40
- 230 END

#### LINEAR INTERPOLATION

If Y is a function of X, and  $Y_1 - Y_2$  are the values of the function at  $X_1 - X_2$ , respectively, Y may be computed for any value of X.

## **FORMULA**





## LINEAR INTERPOLATION

- 10 REM THIS PROGRAM COMPUTES LINEAR INTER-POLATION
- PRINT "KNOWN VALUE OF X (X1,X2) = ";
- 30 INPUT X1, X2
- 40 PRINT "KNOWN VALUES OF Y (F(X1), F(X2)) = ";
- 50 INPUT Y1, Y2
- 60 PRINT "INTERPOLATE F(X) AT X = ";
- 70 INPUT X
- 80 LET G = ((X2 X)\*Y1) + ((X X1)\*Y2)
- 90 LET F = G/(X2 X1)
- 100 PRINT "INTERPOLATED F(X) = ";F
- 110 PRINT
- 120 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 130 INPUT L
- 140 IF L = 1 THEN 160
- 150 STOP
- 160 PRINT
- 170 GOTO 20
- 180 END

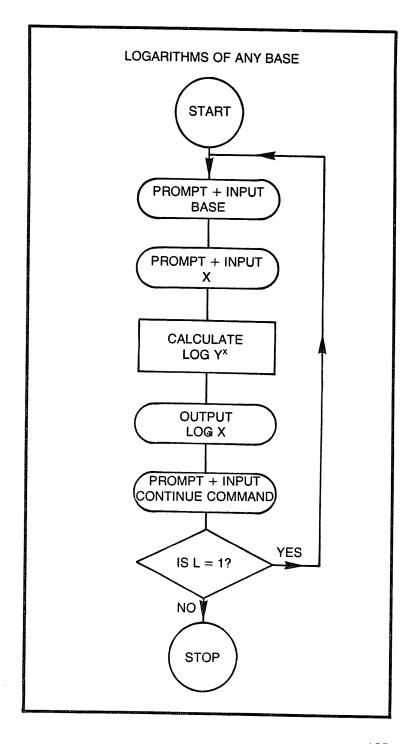
## LOGARITHMS OF ANY BASE

This simple program allows the user to compute the value of a logarithm to any base. The number X and the base Y must both be positive if machine error is not to occur.

## **FORMULA**

$$\log_{x} x = \frac{\ln x}{\ln y}$$

```
BASE =
16
X =
54
LOG 54 = 1.43872
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
BASE =
567
X =
23
LOG 23 = .494529
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



# LOGARITHMS OF ANY BASE

- 10 REM THIS PROGRAM WILL COMPUTE THE LOG
- REM OF ANY POSITIVE NUMBER X, TO ANY POSITIVE
- 30 REM BASE Y
- 40 PRINT "BASE = "
- 50 INPUT Y
- 60 PRINT "X ="
- 70 INPUT X
- 80 LET J = LOG(X)/LOG(Y)
- 90 PRINT "LOG";X;" = ";J
- 100 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 110 INPUT L
- 120 IF L = 1 THEN 140
- 130 STOP
- 140 PRINT
- 150 GOTO 40
- 160 END

## MEAN, STANDARD DEVIATION, STANDARD ERROR FOR GROUPED DATA

This program generates the mean, standard deviation and standard error for grouped data until the user enters a 0 for the value of the frequency.

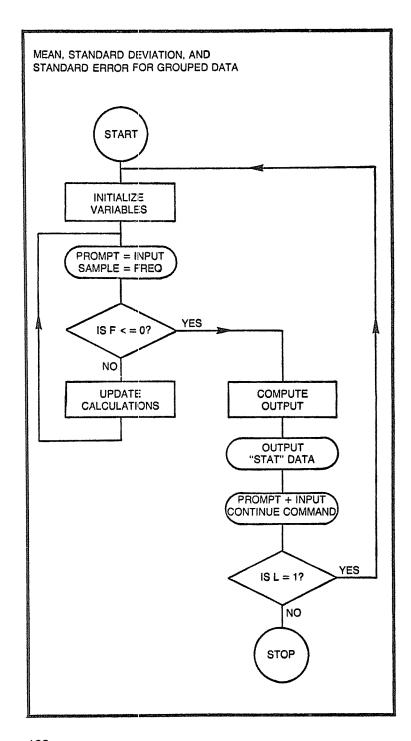
## **FORMULAE**

$$Mean \ \overline{x} = \frac{\sum f_i x_i}{\sum f_i}$$

Standard error 
$$S\overline{x} = \frac{S}{\sqrt{\sum f_i}}$$

Standard deviation 
$$S = \frac{\sqrt{\sum f_i \ x_i^2 - (\sum f_i) \ \overline{x}^2}}{\sum f_i - 1}$$

```
ENTER SAMPLE VALUE AND FREQUENCY
?
5.2
ENTER SAMPLE VALUE AND FREQUENCY
10.3
ENTER SAMPLE VALUE AND FREQUENCY
6.1
ENTER SAMPLE VALUE AND FREQUENCY
?
0.0
NUMBER OF SAMPLES ENTERED = 3
MEAN = 7.67
STANDARD DEVIATION = 5.77
STANDARD ERROR = 2.36
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



## MEAN, STANDARD DEVIATION, AND

## STANDARD ERROR FOR GROUPED DATA

- 10 REM THIS PROGRAM COMPUTES THE MEAN, STANDARD
- 20 REM DEVIATION AND STANDARD ERROR FOR GROUPED DATA
- $30 \qquad \text{LET A} = 0$
- $40 \qquad \text{LET B} = 0$
- 50 LET C = 0
- 60 LET D = 0
- 70 PRINT "ENTER SAMPLE VALUE AND FREQUENCY";
- 80 INPUT X.F
- 90 IF F < = 0 THEN 170
- 100 LET A = A + 1
- 110 LET B = B + F
- 120 LET G = X\*F
- 130 LET C = C + G
- 140 LET E =  $(X^{\dagger}2)^*F$
- 150 LET D = D + E
- 160 GOTO 70
- 170 LET H = C/B
- 180 LET I =  $SQR(D (B^*(H^{\dagger}2)))$
- 190 LET J = I/SQR(B)
- 200 PRINT
- 210 PRINT "NUMBER OF SAMPLES ENTERED = ";A
- PRINT "MEAN = ";H
- 230 PRINT "STANDARD DEVIATION = ";I
- 240 PRINT "STANDARD ERROR = ";J
- 250 PRINT
- 260 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 270 INPUT L
- 280 IF L = 1 THEN 300
- 290 STOP
- 300 PRINT
- 310 GOTO 30
- 320 END

## MOMENTS, SKEWNESS AND KURTOSIS

This program computes the first four moments where the first moment is the mean of the distribution and the second moment is the variance. Skewness is the departure of a frequency distribution from symmetry, and kurtosis is a property of distribution that expresses its relative peakedness.

### **FORMULAE**

$$I^{ST}M = \overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

$$2^{ND} M = M_2 = \frac{1}{n} \sum_{i} x_{i^2} - \overline{x}^2$$

$$3^{RD}M = M_3 = \frac{1}{n} \sum_{x} x^{3} - \frac{3}{n} \sum_{x} x^{2} + 2x^{3}$$

$$4^{TH}M = M_4 = \frac{1}{n} \sum_{i} x_i^4 - \frac{4}{n} \overline{x} \sum_{i} x_i^3 + \frac{6}{n} \overline{x}^2 \sum_{i} x_i^2 - 3\overline{x}$$

$$SKEWNESS = \gamma_1 = \frac{M_3}{M_2^{3/2}}$$

$$KURTOSIS \gamma_2 = \frac{M_4}{M_2^2}$$

## **EXAMPLE**

NUMBER OF SAMPLES =

? 5

SAMPLE =

?

12

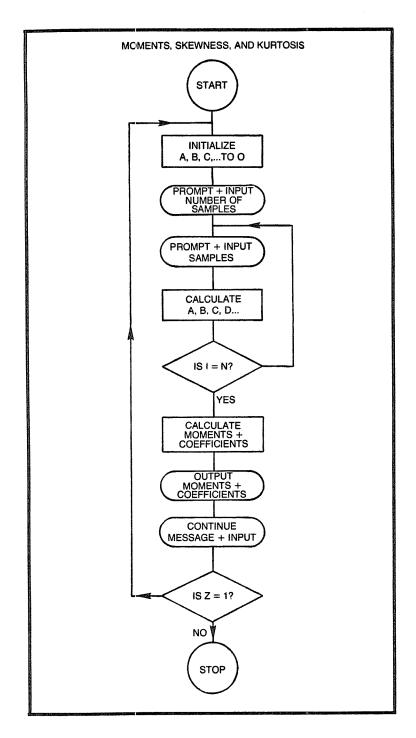
SAMPLE =

?

SAMPLE =

?

4



### MOMENTS, SKEWNESS, AND KURTOSIS

- 10 REM THIS PROGRAM COMPUTES THE VALUES OF THE
- 20 REM FIRST 4 MOMENTS, SKEWNESS AND KURTOSIS
- $30 \quad \text{LET A} = 0$
- $40 \qquad \text{LET B} = 0$
- 50 LET C = 0
- $60 \quad \text{LET D} = 0$
- 70 PRINT "NUMBER OF SAMPLES = "
- 80 INPUT N
- 90 FOR I = 1 TO N
- 100 PRINT "SAMPLE = "
- 110 INPUT X
- $120 \quad \text{LET A} = A + X$
- 130 LET B = B +  $(X^{\uparrow}2)$
- 140 LET  $C = C + (X^{\uparrow}3)$
- 150 LET D = D +  $(X^4)$
- 160 NEXT I
- 170 LET J = A/N
- 180 LET E =  $(B/N) (J^2)$
- 190 LET  $F = (C/N) ((3*J*B)/N) + (2*(J^3))$
- 200 LET G = (D/N) ((4\*J\*C)/N)
- 210 LET H = G +  $((6*(J^2)*B)/N) (3*(J^4))$
- 220 LET  $K = F/(E \uparrow (3/2))$
- 230 LET L =  $H/(E\uparrow 2)$
- 240 PRINT "1ST MOMENT = ";J
- 250 PRINT "2ND MOMENT = ";E
- 260 PRINT "3RD MOMENT = ":F
- 270 PRINT "4TH MOMENT = ":H
- 280 PRINT "MOMENT COEFFICIENTS"
- 290 PRINT "SKEWNESS = ";K, "KURTOSIS = ";L
- 310 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 320 INPUT Z
- 330 IF Z = 1 THEN 350
- 340 STOP
- 350 PRINT
- 360 GOTO 30
- 370 END

### NO REPETITIONS PROBABILITY

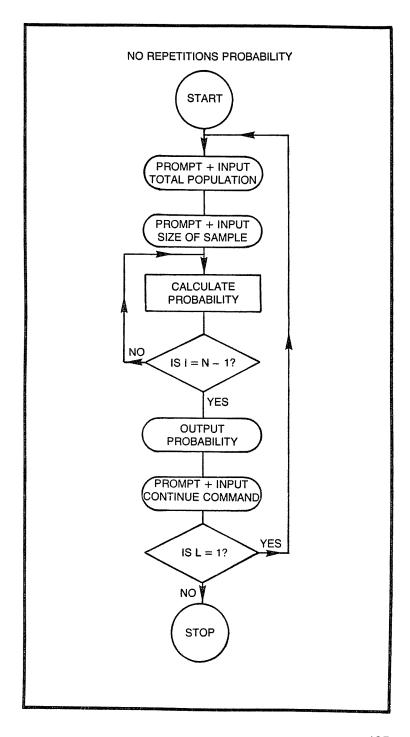
The user dictates the size of a population to be determined for a "No Repetitions" probability.

### **FORMULA**

$$P = \left(1 - \frac{1}{M}\right) \left(1 - \frac{2}{M}\right) \cdots \left(1 - \frac{N-1}{M}\right)$$

where  $M \ge N \ge 1$ 

```
EXAMPLE
**************
TOTAL POPULATION
?
56
SIZE OF SAMPLE
2
PROBABILITY = .982143
TYPE 1 TO CONTINUE, 0 TO STOP
1
*********
TOTAL POPULATION
9
SIZE OF SAMPLE
PROBABILITY = .460905
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



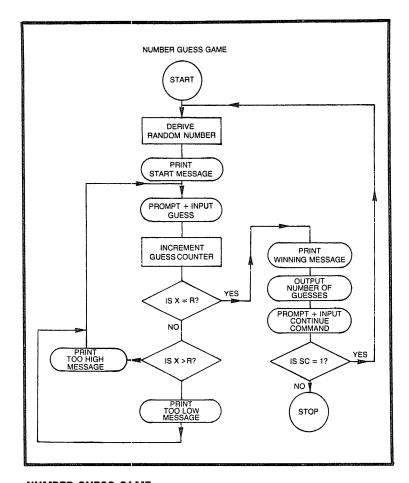
## **NO-REPETITIONS PROBABILITY**

- 10 REM THIS PROGRAM COMPUTES THE "NO REPETITIONS"
- 20 REM PROBABILITY OF A SAMPLE
- 35 PRINT "TOTAL POPULATION"
- 40 INPUT M
- 50 PRINT "SIZE OF SAMPLE"
- 60 INPUT N
- $70 \quad \text{LET J} = 1$
- 80 FOR I = 1 TO N 1
- 90 LET K = 1 (I/M)
- 100 LET J = J\*K
- 110 NEXT I
- 120 PRINT "PROBABILITY = ";J
- 130 PRINT
- 140 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 150 INPUT L
- 160 IF L = 1 THEN 30
- 170 STOP
- 180 END

### **NUMBER GUESS GAME**

The object of this game is to guess in as few tries as possible the number chosen at random by the computer. (Hint: Use a binary search pattern.)

```
A RANDOM NUMBER HAS BEEN PICKED
TRY GUESSING IT, HINT THE NUMBER
IS FROM 1 TO 100
GOOD LUCK!!!
YOUR GUESS IS =
?
50
TOO HIGH, TRY AGAIN
YOUR GUESS IS =
?
25
TOO HIGH, TRY AGAIN
YOUR GUESS IS =
?
12
TOO LOW, TRY AGAIN
YOUR GUESS IS =
?
18
TOO LOW, TRY AGAIN
YOUR GUESS IS =
?
20
NOT BAD!!!-YOU GOT IT!!!
YOUR NUMBER OF TRIES WERE 5
IF YOU WANT TO TRY AGAIN TYPE 1
IF NOT TYPE 0
?
0
*END
```



#### NUMBER GUESS GAME

- 10 REM THE COMPUTER CHOOSES A NUMBER FROM
- 20 REM 1 TO 100 AT RANDOM, THE OBJECT OF
- 30 REM THE GAME IS TO GUESS THE CHOSEN
- 40 REM NUMBER IN AS FEW GUESSES AS POSSIBLE
- 50 LET R = 1 + INT(100\*RND)
- 60 LET Y = 0
- 70 PRINT "A RANDOM NUMBER HAS BEEN PICKED"
- 80 PRINT "TRY GUESSING IT, HINT THE NUMBER"
- 90 PRINT "IS FROM 1 TO 100"
- 100 PRINT "GOOD LUCK!!!"
- 110 PRINT
- 120 PRINT "YOUR GUESS IS = ";
- 130 INPUT X

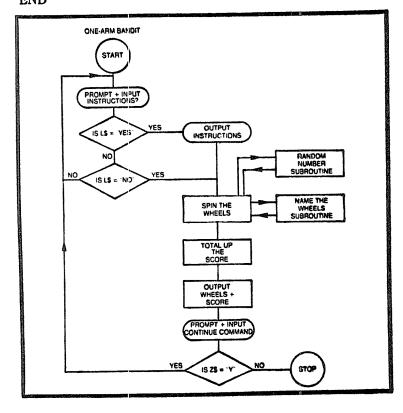
- 140 LET Y = Y + 1
- 150 IF X = R THEN 180
- 160 IF X > R THEN 280
- 170 GOTO 300
- 180 PRINT "NOT BAD!!!-YOU GOT IT!!!"
- 190 PRINT "YOUR NUMBER OF TRIES WERE";Y
- 200 PRINT
- 210 PRINT "IF YOU WANT TO TRY AGAIN, TYPE 1"
- 220 PRINT "IF NOT TYPE 0"
- 230 INPUT L
- 240 IF L = 1 THEN 260
- 250 STOP
- 260 PRINT
- 270 GOTO 50
- 280 PRINT "TOO HIGH, TRY AGAIN"
- 290 GOTO 120
- 300 PRINT "TOO LOW, TRY AGAIN"
- 310 GOTO 120
- 320 END

## **ONE-ARM BANDIT**

This computer program simulates the one-arm bandits that use three mechanical wheels. For detailed instructions, type yes to the instruction question in the program.

### **EXAMPLE**

RUN
ARE INSTRUCTIONS REQUIRED
TYPE EITHER YES OR NO
?
NO
CHERRY CHERRY CHERRY
YOUR TOTAL EARNINGS ARE NOW \$89
TO CONTINUE TYPE Y, IF NOT TYPE N
?
N
ONE-ARM BANDIT SAYS GOOD-BYE
\*END



#### **ONE-ARM BANDIT**

- 10 REM THIS PROGRAM SIMULATES THE MECHANI-CAL
- 20 REM THREE WHEEL ONE-ARM BANDIT
- 30 PRINT "ARE INSTRUCTIONS REQUIRED"
- 40 PRINT "TYPE EITHER YES OR NO"
- 50 INPUT L\$
- 60 IF L\$ = "YES" THEN 100
- 70 IF L\$ = "NO" THEN 170
- 80 PRINT "INVALID COMMAND"
- 90 GOTO 30
- 100 PRINT "SCORING IS SIMPLE; 3 ORANGES, LEM-ONS OR"
- PRINT "BANANAS EARN \$10. 3 CHERRIES EARN \$90."
- 120 PRINT "IF THE FIRST FRUIT IS AN APPLE YOU EARN \$2"
- PRINT "IF THE 1ST AND 2ND ARE APPLES YOU EARN \$3"
- 140 PRINT "IF THE LAST FRUIT IS A CHERRY AND THE"
- 150 PRINT "OTHER TWO ARE THE SAME BUT NOT APPLES YOU"
- 160 PRINT "EARN \$10. EACH TURN COSTS \$1. GOOD-LUCK"
- 170 LET J = 0
- 180 PRINT
- 190 GOSUB 590 ~
- 200 LET S1 = S
- 210 GOSUB 590
- 220 LET S2 = S
- 230 GOSUB 590
- $\frac{230}{240}$  LET S3 = S
- 250 LET S = S1
- 260 GOSUB 610
- 270 LET S1\$ = S\$
- $280 \qquad \text{LET S} = S2$
- 290 GOSUB 610
- 300 LET S2\$ = S\$
- 310 LET S = S3
- 320 GOSUB 610
- 330 LET S3\$ = S\$
- 340 IF S1\$ = "CHERRY" THEN 380
- 350 IF S1\$ = "APPLE" THEN 420

```
360
      IF S1\$ = S2\$ THEN 440
370
      GOTO 460
      IF S1\$ = S2\$ THEN 400
380
      GOTO 460
390
      IF S2\$ = S3\$ THEN 480
400
      GOTO 460
410
420
      IF S1\$ = S2\$ THEN 500
430
      GOTO 520
      IS S2\$ = S3\$ THEN 540
440
      IF S3$ = "CHERRY" THEN 540
450
460
      LET J = J - 1
470
      GOTO 550
      LET J = J + 89
480
490
      GOTO 550
500
      LET J = J + 2
510
      GOTO 550
520
      LET J = J + 1
530
      GOTO 550
540
      LET J = J + 9
550
      PRINT
      PRINT S1$;" ";S2$;" ";S3$
560
      PRINT "YOUR TOTAL EARNINGS ARE NOW $";J
570
580
       GOTO 720
590
      LET S = 1 + INT(5*RND)
      RETURN
600
610
       ON S GOTO 620, 640, 660, 680, 700
      LET S$ = "CHERRY"
620
630
      GOTO 710
      LET S$ = "APPLE"
640
650
      GOTO 710
      LET S$ = "LEMON"
660
670
      GOTO 710
      LET S$ = "ORANGE"
680
       GOTO 710
690
       LET S$ = "BANANA"
700
710
       RETURN
720
       PRINT
       PRINT "TO CONTINUE TYPE Y, IF NOT TYPE N"
730
740
       INPUT Z$
       IF Z$ = "Y" THEN 780
750
       PRINT "ONE-ARM BANDIT SAYS GOOD-BYE"
760
770
       STOP
       PRINT
780
       GOTO 190
790
800
       END
142
```

## PERMUTATIONS AND COMBINATIONS

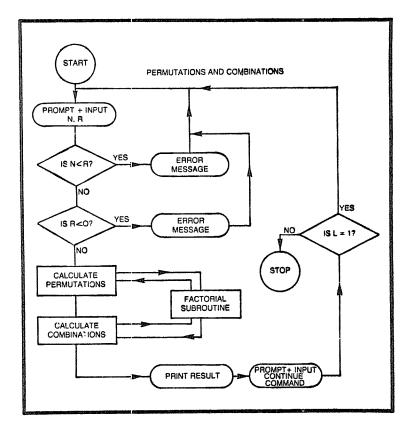
This program computes permutations and combinations, where N is the number of items available and R is the size of the groups under consideration.

## **FORMULAE**

$$P = \frac{N!}{(N-R)!} \qquad C = \frac{N!}{R!(N-R)!}$$

```
ENTER N,R

?
12,5
PERMUTATIONS = 95040
COMBINATIONS = 792
TYPE 1 TO CONTINUE, 0 TO STOP
?
1
ENTER N,R
?
23,21
PERMUTATIONS = 1.2926E22
COMBINATIONS = 253
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



### PERMUTATIONS AND COMBINATIONS

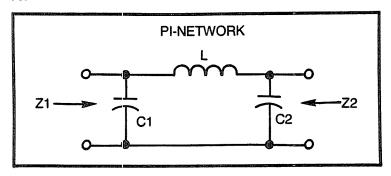
- 10 REM THIS PROGRAM COMPUTES PERMUTATIONS
- 20 REM AND COMBINATIONS, WHERE N = NUMBER OF
- 30 REM ITEMS AND R = SIZE OF GROUP SELECTED
- 40 PRINT "ENTER N.R":
- 50 INPUT N,R
- 60 IF N < R THEN 270
- 70 IF R < 0 THEN 290
- 80 LET T = N
- 90 GOSUB 310
- 100 LET A = T
- 110 LET T = N R
- 120 GOSUB 310
- 130 LET B = T
- 140 LET P = A/B
- 150 LET T = R

- 160 GOSUB 310
- 170 LET C = A/(T\*B)
- 180 PRINT "PERMUTATIONS = ":P
- 190 PRINT "COMBINATIONS = ";C
- 200 PRINT
- 210 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 220 INPUT L
- 230 IF L = 1 THEN 250
- 240 STOP
- 250 PRINT
- 260 GOTO 40
- 270 PRINT "N < R,INVALID INPUT"
- 280 GOTO 40
- 290 PRINT "R < 0, INVALID INPUT"
- 300 GOTO 40
- 310 IF T = 0 THEN 390
- 320 IF T = 1 THEN 390
- 330 LET I = 1
- 340 FOR I = 2 TO T
- 350 LET  $J = J^*I$
- 360 NEXT I
- 370 LET T = J
- 380 GOTO 400
- 390 LET T = 1
- 400 RETURN
- 410 END

#### PI-NETWORK IMPEDANCE MATCHING

Often between two resistive impedanced  $Z_1$  and  $Z_2$  a lossless network is desired. The computer expects the following information:  $Z_1 - Z_2$ , desired system Q and the operating frequency.

#### **FORMULAE**



 $Z_1 > Z_2$ , f = frequency and Q is desired system Q

$$C_1 = \frac{1}{2\pi f X_{C1}} \quad C_2 = \frac{1}{2\pi f X_{C2}} \quad L = \frac{X_1}{2\pi f} \frac{Z_2}{Z_1} (Q^2 + 1) > 1$$

and where

$$X_{C1} = \frac{Z_1}{Q_1} \qquad X_{C2} = \frac{Z_2}{\left(\frac{Z_2}{Z_1}(Q^2 + 1) - 1\right)^5}$$
$$X_L = \frac{QZ_1}{Q^2 + 1} \left(1 + \frac{Z_2}{QX_{C2}}\right)$$

#### **EXAMPLE**

**ENTER 1ST IMPEDANCE** 

?

345

**ENTER 2ND IMPEDANCE** 

?

300

ENTER DESIRED SYSTEM Q

2

20

```
ENTER OPERATING FREQUENCY?

500

COMPONENTS OF PI-NETWORK

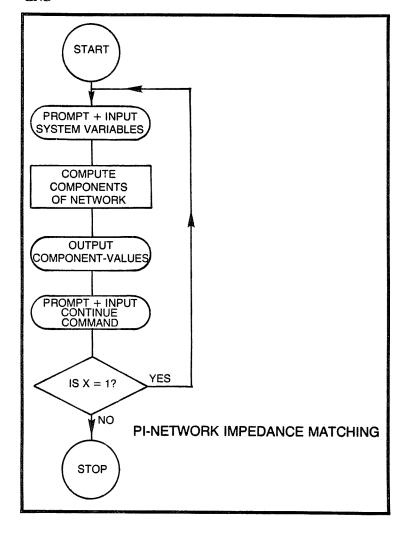
CAPACITOR 1 = 1.84527 E - 5

CAPACITOR 2 = 1.97846 E - 5

INDUCTOR = 1.05836 E - 2

TO CONTINUE TYPE 1, IF NOT 0

?
0
*END
```



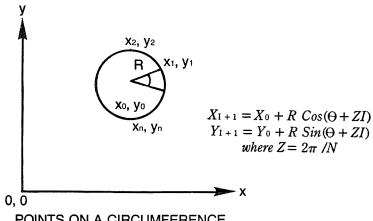
#### PI-NETWORK IMPEDANCE MATCHING

- 10 REM THIS PROGRAM COMPUTES THE COMPONENTS
- 20 REM OF A PI-NETWORK. TO MATCH TWO
- 30 REM IMPEDANCES
- 40 PRINT "ENTER 1ST IMPEDANCE"
- 50 INPUT Z1
- 60 PRINT "ENTER 2ND IMPEDANCE"
- 70 INPUT Z2
- 80 PRINT "ENTER DESIRED SYSTEM Q"
- 90 INPUT Q
- 100 PRINT "ENTER OPERATING FREQUENCY"
- 110 INPUT A
- 120 LET A = Z1/Q
- 130 LET C =  $((Z2/Z1)*((Q^2) + 1)) 1$
- 140 LET B = Z2/SQR(C)
- 150 LET E = (Z2/(Q\*B)) + 1
- 160 LET D = E\*((Q\*Z1)/((Q\(\gamma\)2) + 1))
- 170 LET P = 6.28319
- 180 LET C1 = 1/(P\*F\*A)
- 190 LET C2 = 1/(P\*F\*B)
- 200 LET L = D/(P\*F)
- 210 PRINT "COMPONENTS OF PI-NETWORK"
- 220 PRINT "CAPACITOR 1 = ";C1
- 230 PRINT "CAPACITOR 2 ="; C2
- 240 PRINT "INDUCTOR = ";L
- 250 PRINT
- 260 PRINT "TO CONTINUE TYPE 1, IF NOT 0"
- 270 INPUT X
- 280 IF X = 1 THEN 300
- 290 STOP
- 300 PRINT
- 310 GOTO 40
- 320 END

# POINTS ON THE CIRCUMFERENCE

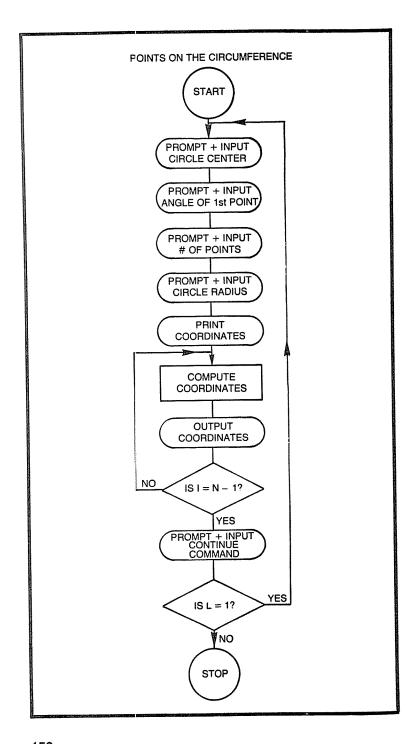
This program computes N equally spaced points on the circumference of a circle. Given radius and center of the circle, this program computes the rectangular coordinates of equally spaced points X<sub>1</sub>, Y<sub>1</sub>.

#### **FORMULAE**



POINTS ON A CIRCUMFERENCE

```
CENTER OF CIRCLE(X0, Y0) =
?
2.2
ANGLE IN DEGREES OF FIRST POINT =
90
NUMBER OF POINTS DESIRED =
?
2
RADIUS OF CIRCLE =
1
COORDINATES
POINT 1 X = 3 Y = 2
POINT 2 X = 2 Y = 1
```



#### POINTS ON THE CIRCUMFERENCE

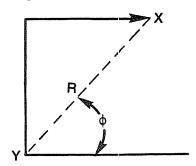
- 10 REM THIS PROGRAM COMPUTES N EQUALLY SPACED
- 20 REM POINTS ON THE CIRCUMFERENCE OF A CIRCLE
- 30 PRINT "CENTER OF CIRCLE (X0, Y0) = ";
- 40 INPUT X0, Y0
- 50 PRINT "ANGLE IN DEGREES OF 1ST POINT = ";
- 60 INPUT W
- 70 LET W = (W\*3.14159)/180
- 80 PRINT "NUMBER OF POINTS DESIRED = ":
- 90 INPUT N
- 100 PRINT "RADIUS OF A CIRCLE = ";
- 110 INPUT R
- 120 LET Z = 6.28319/N
- 130 PRINT
- 140 PRINT "COORDINATES"
- 150 FOR I = 0 TO N 1
- 160 LET X = X0 + (R\*COS(W + Z\*I))
- 170 LET Y = Y0 + (R\*SIN(W + (Z\*I)))
- 180 LET P = I + 1
- 190 PRINT "POINT;"; P, "X = "; X, "Y = "; Y
- 200 NEXT I
- 210 PRINT
- 220 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 230 INPUT L
- 240 IF L = 1 THEN 260
- 250 STOP
- 260 PRINT
- 270 GOTO 30
- 280 END

#### POLAR TO RECTANGULAR CONVERSION

This program converts given polar coordinates into rectangular coordinates.

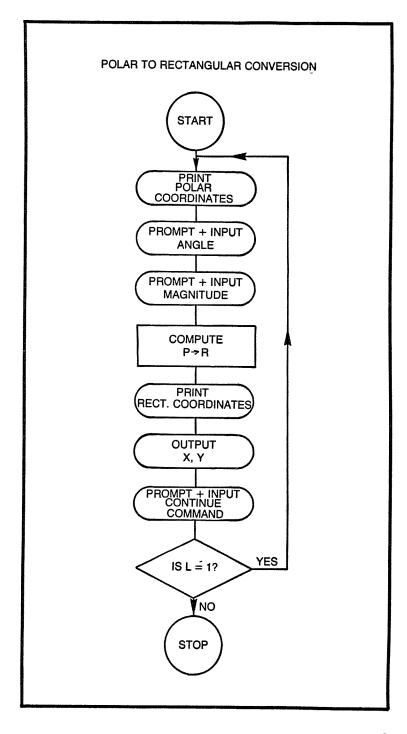
#### **FORMULAE**

#### POLAR TO RECTANGULAR



 $X = R \ Cos \ \Theta$  $Y = R \ Sin \ \Theta$ 

```
POLAR COORDINATES
ANGLE W IN DEGREES =
45
MAGNITUDE R ==
5
RECTANGULAR COORDINATES
X = 3.53553 Y = 3.53553
TYPE 1 TO CONTINUE, 0 TO STOP
POLAR COORDINATES
ANGLE W IN DEGREES =
20
MAGNITUDE R ==
?
1
RECTANGULAR COORDINATES
X = .939693 Y = .34202
TYPE 1 TO CONTINUE, 0 STOP
?
0
*END
```



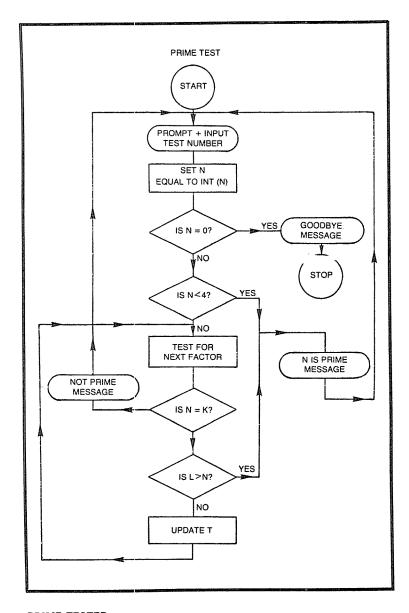
# POLAR TO RECTANGULAR CONVERSION

- 10 REM THIS PROGRAM CONVERTS GIVEN POLAR COORDINATES
- 20 REM INTO RECTANGULAR COORDINATES
- 30 PRINT "POLAR COORDINATES"
- 40 PRINT "ANGLE W IN DEGREES = ";
- 50 INPUT W
- 60 LET W = (W\*3.14159)/180
- 70 PRINT "MAGNITUDE R = ";
- 80 INPUT R
- 90 LET X = R\*COS(W)
- 100 LET Y = R\*SIN(W)
- 110 PRINT "RECTANGULAR COORDINATES"
- 120 PRINT "X = "; X, "Y = "; Y
- 130 PRINT
- 140 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 150 INPUT L
- 160 IF L = 1 THEN 180
- 170 STOP
- 180 PRINT
- 190 GOTO 30
- 200 END

#### PRIME TEST

This program tests a given number to see whether or not it is prime. If so, it is thus indicated and if not, the smallest factor returned. The program will continue to cycle until a zero is entered as a test number.

```
ENTER THE TEST NUMBER, ZERO TO STOP
45
45 IS NOT A PRIME 3 IS THE SMALLEST FACTOR
ENTER THE TEST NUMBER, ZERO TO STOP
120078
120078 IS NOT A PRIME 2 IS THE SMALLEST FACTOR
ENTER THE TEST NUMBER.ZERO TO STOP
121
121 IS NOT A PRIME 11 IS THE SMALLEST FACTOR
ENTER THE TEST NUMBER, ZERO TO STOP
?
179
179 IS A PRIME
ENTER THE TEST NUMBER, ZERO TO STOP
?
0
GOOD-BYE FROM THE PRIME TESTER
*END
```



#### PRIME TESTER

- 10 REM THIS PROGRAM TESTS IF A NUMBER IS PRIME
- 20 REM IT CONTINUES TO CYCLE UNTIL ZERO IS ENTERED
- 30 PRINT "ENTER THE TEST NUMBER, ZERO TO STOP"

- 40 INPUT N
- 50 LET N = INPUT(N)
- 60 IF N = 0 THEN 220
- 70 IF N < 4 THEN 180
- 10 = I T = 0
- 90 LET T = 2
- 100 LET J = INT(N/T)
- 110 LET K = J\*T
- 120 IF N = K THEN 200
- 130 LET I = I + 1
- 140 LET L = T\*T
- 150 IF L > N THEN 180
- 160 LET T = (I\*2) + 1
- 170 GOTO 100
- 180 PRINT N; "IS A PRIME"
- 190 GOTO 30
- 200 PRINT N; "IS NOT A PRIME"; T; "IS THE SMALLEST FACTOR"
- 210 GOTO 30
- 220 PRINT "GOOD-BYE FROM THE PRIME TESTER"
- 230 END

# **QUADRATIC EQUATIONS**

This program solves for x in a quadratic equation where a, b and c are given. Both real and complex roots are found.

#### **FORMULAE**

$$ax^{2} + bx + c = \phi$$

$$x_{1}, x_{2} = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

$$D = (b^2 - 4ac)/4a^2$$

 $D \ge \phi$  roots are real  $D < \phi$  roots are complex

$$D \ge \phi$$

$$IF - \frac{b}{2a} \ge \phi \quad X_1 = -\frac{b}{2a} + \sqrt{D}$$

$$IF - \frac{b}{2a} < \phi \qquad X_1 = -\frac{b}{2a} - \sqrt{D}$$

$$X_2 = \frac{C}{Y_{1,\sigma}}$$

$$D < O$$

$$U + Vi = \frac{-b}{2a} \pm \frac{\sqrt{4ac - b^2}}{2a} i$$

# **EXAMPLES**

ENTER VALUES FOR A,B AND C

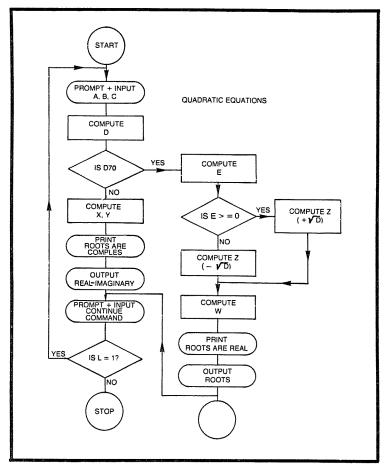
?

1,1,0

ROOTS ARE REAL

1ST ROOT = -1

2ND ROOT = 0



#### QUADRATIC EQUATION

- 10 REM THIS PROGRAM COMPUTES THE SOLUTION TO A
- 20 REM QUADRATIC EQUATION
- 30 PRINT "ENTER VALUES FOR A, B AND C"
- 40 INPUT A,B,C
- 50 LET D =  $((B^2) (4^*A^*C))/(4^*A^2)$
- 60 IF D > = 0 THEN 130
- 70 LET X = B/(2\*A)
- 80 LET Y = (SQR((4\*A\*C) B 2))/(2\*A)
- 90 PRINT "ROOTS ARE COMPLEX"
- 100 PRINT "REAL PART = ";X
- 110 PRINT "IMAGINARY PART = ";Y
- 120 GOTO 220
- 130 LET E = -B/(2\*A)
- 140 IF E > = 0 THEN 170
- 150 LET Z = E SQR(D)
- 160 GOTO 180
- 170 LET Z = E + SQR(D)
- 180 LET W =  $C/(Z^*A)$
- 190 PRINT "ROOTS ARE REAL"
- 200 PRINT 1ST ROOT = ";Z
- 210 PRINT "2ND ROOT = ";W
- 230 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 240 INPUT L
- 250 IF L = 1 THEN 270
- 260 STOP
- 270 PRINT
- 280 GOTO 30
- 290 END

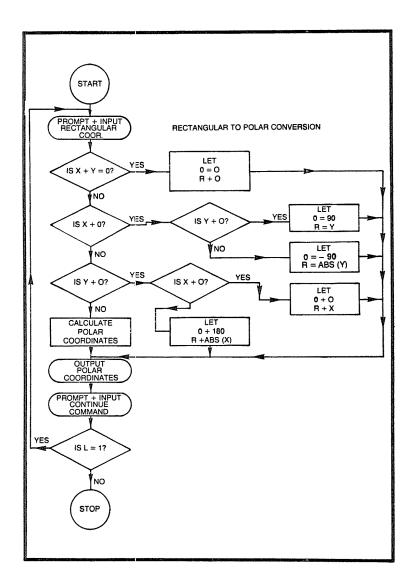
#### RECTANGULAR TO POLAR CONVERSION

This program computes rectangular coordinates that are supplied by the user into polar coordinates.

# **FORMULAE**

$$\phi = TAN^{-1} \frac{Y}{X} \quad R = \sqrt{X^2 + Y^2}$$

```
X =
10
Y =
10
POLAR COORDINATES
ANGLE IN DEGREES = 45.0000
MAGNITUDE = 14.1421
*******
TYPE 1 TO CONTINUE, 0 TO STOP
1
X =
34
Y =
32
POLAR COORDINATES
ANGLE IN DEGREES = 43.2643
MAGNITUDE = 46.6904
********
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



#### RECTANGULAR TO POLAR CONVERSION

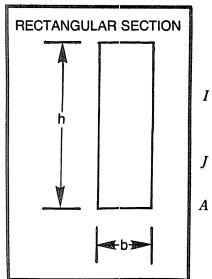
- 10 REM THIS PROGRAM CONVERTS GIVEN RECTAN-GULAR
- 20 REM COORDINATES INTO POLAR COORDINATES
- 30 PRINT "RECTANGULAR COORDINATES"
- 40 PRINT "X ="
- 50 INPUT X
- 60 PRINT "Y="

- 70 INPUT Y
- 80 IF X + Y = 0 THEN 150
- 90 IF X = 0 THEN 180
- 100 IF Y = 0 THEN 250
- 110 LET W = ATN(Y/X)
- 120 LET W = (W\*180)/3.14159
- 130 LET  $R = SQR(X\uparrow 2 + Y\uparrow 2)$
- 140 GOTO 310
- 150 LET W = 0
- 160 LET R = 0
- 170 GOTO 310
- 180 IF Y> 0 THEN 220
- 190 LET W = -90
- 200 LET R = ABS(Y)
- 210 GOTO 310
- 220 LET W = 90
- 230 LET R = Y
- 240 GOTO 310
- X > 0 THEN 290
- 260 LET W = 180
- 270 LET R = ABS(X)
- 280 GOTO 310
- 290 LET W = 0
- 300 LET R = X
- 310 PRINT "POLAR COORDINATES"
- 320 PRINT "ANGLE IN DEGREES = "; W
- 330 PRINT "MAGNITUDE = "; R
- 350 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 360 INPUT L
- 370 IF L = 1 THEN 390
- 380 STOP
- 390 PRINT
- 400 GOTO 40
- 410 END

### **RECTANGULAR SECTIONS**

This program computes various parameters: moment of inertia, polar moment of inertia, and area of section connected with a rectangular section.

#### FORMULAE

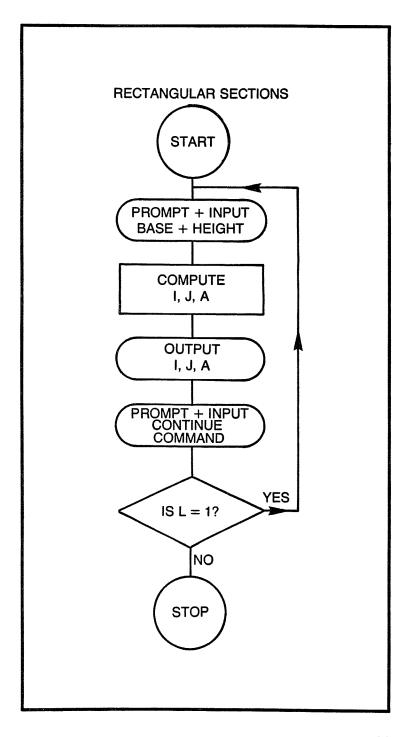


$$I = \frac{bh^3}{12} \quad I \text{ and } J \text{ is in (in 4)}$$

$$J = \frac{bh(b^2 + h^2)}{12}$$

$$A = bH$$

```
BASE =
?
3
HEIGHT =
?
5
MOMENT OF INERTIA = 31.25
POLAR MOMENT OF INERTIA = 42.50
AREA OF SECTION = 15
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



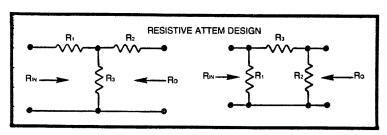
#### **RECTANGULAR SECTIONS**

- 10 REM THIS PROGRAM COMPUTES THE VARIOUS PARAMETERS
- 20 REM CONNECTED WITH A RECTANGULAR SECTION
- 30 PRINT "BASE =";
- 40 INPUT B
- 50 PRINT "HEIGHT = "
- 60 INPUT H
- 70 LET  $I = (B*(H\uparrow 3))/12$
- 80 LET  $J = (B*H*(B^2 + H^2))/12$
- 90 LET A = B\*H
- 100 PRINT "MOMENT OF INERTIA = ";I
- 110 PRINT "POLAR MOMENT OF INERTIA = ";J
- 120 PRINT "AREA OF SECTION = ";A
- 130 PRINT
- 140 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 150 INPUT L
- 160 IF L = 1 THEN 180
- 170 STOP
- 180 PRINT
- 190 GOTO 30
- 200 END

#### RESISTIVE ATTENUATOR DESIGN

This program computes the required three resistors to form either a Pi- or T-type resistive attenuator. This type of attenuator allows the user to choose a loss other than that of minimum.

#### **FORMULAE**



$$R_{IN} > Ro, \text{ and } N = \text{ desired loss } \geqslant \text{ minimum loss}$$

$$minimum \text{ loss } = 1\phi \log \left( \sqrt{\frac{R_{IN}}{R_O}} + \sqrt{\frac{R_{IN}}{R_O}} - 1 \right)^2$$

$$T - \text{type}$$

$$R_3 = \frac{2\sqrt{NR_{IN}R_O}}{N-1}$$

$$R_1 = R_{IN} \left( \frac{N+1}{N-1} - R_3 \right)$$

$$\pi - \text{type}$$

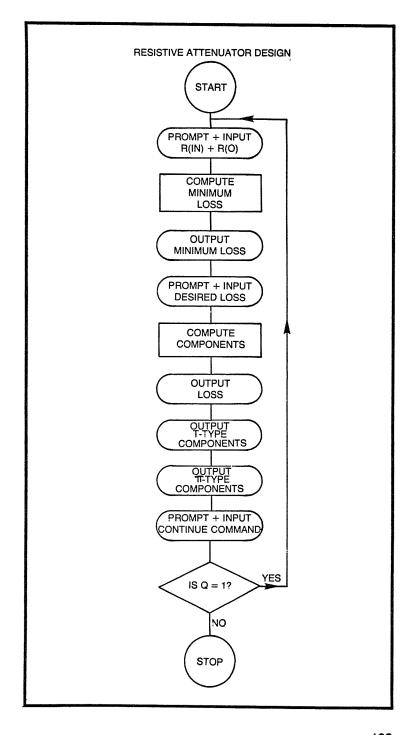
$$R_3 = \frac{1}{2} (N-1) \left( \frac{R_{IN}R_O}{N} \right)^{1/2}$$

$$R_1 = \frac{1}{R_{IN}} \left( \frac{N+1}{N-1} - \frac{1}{R_3} \right)$$

$$R_2 = \frac{1}{R_O} \left( \frac{N+1}{N-1} - \frac{1}{R_3} \right)$$

$$R_2 = \frac{1}{R_O} \left( \frac{N+1}{N-1} - \frac{1}{R_3} \right)$$

```
INPUT RESISTANCE R(IN) =
500
OUTPUT RESISTANCE R(0) =
?
100
MINIMUM SYSTEM LOSS IN DECIBELS = 12.54
ENTER DESIRED LOSS IN DECIBELS
20
R(IN) = 500 R(0) = 100
DESIRED LOSS = 20
T ATTENUATOR
RESISTOR 1 = 464.9
RESISTOR 2 = 56.85
RESISTOR 3 = 45.17
PI ATTENUATOR
RESISTOR 1 = 879.6
RESISTOR 2 = 107.5
RESISTOR 3 = 1107
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



```
RESISTIVE ATTENUATOR DESIGN
      REM THIS PROGRAM COMPUTES THE COMPO-
10
        NENTS
      REM REQUIRED FOR A PI OR T TYPE
20
      REM RESISTIVE ATTENUATOR
30
      PRINT "INPUT RESISTANCE R(IN) = ";
40
50
      INPUT X
60
      PRINT "OUTPUT RESISTANCE R(0) = ";
70
      INPUT Y
80
      LET Z = X/Y
90
      LET Q = (SQR(Z) + SQR(Z - 1))^2
      LET M = 10*(LOG(Q)/LOG(10))
100
      PRINT "MINIMUM SYSTEM LOSS IN DECIBELS
110
        = ":M
      PRINT "ENTER DESIRED LOSS IN DECIBELS";
120
130
      INPUT L
      LET N = 10 (L/10)
140
150
      LET W = N - 1
160
      LET U = N + 1
      LET A = 2*(SQR(X*Y*N))
170
180
      LET B = (X^*(U/W)) - A
190
      LET C = (Y^*(U/W)) - A
200
      LET D = (W*SQR((X*Y)/N))/2
210
      LET E = 1/((U/W)/X) - (1/D)
220
      LET F = 1/((U/W)/Y) - (1/D)
      PRINT "R(IN) = "; X, "R(0) = "; Y
230
      PRINT "DESIRED LOSS = ";L
240
250
      PRINT
260
      PRINT "T ATTENUATOR"
      PRINT "RESISTOR 1 = ":B
270
280
      PRINT "RESISTOR 2 =";C
290
      PRINT "RESISTOR 3 =":A
300
      PRINT
      PRINT "PI ATTENUATOR"
310
      PRINT "RESISTOR 1 = "; E
320
330
      PRINT "RESISTOR 2 = ":F
      PRINT "RESISTOR 3 =";D
340
350
      PRINT
      PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
360
370
      INPUT Q
380
      IF Q = 1 THEN 400
390
      STOP
      PRINT
400
      GOTO 40
410
```

420 170 END

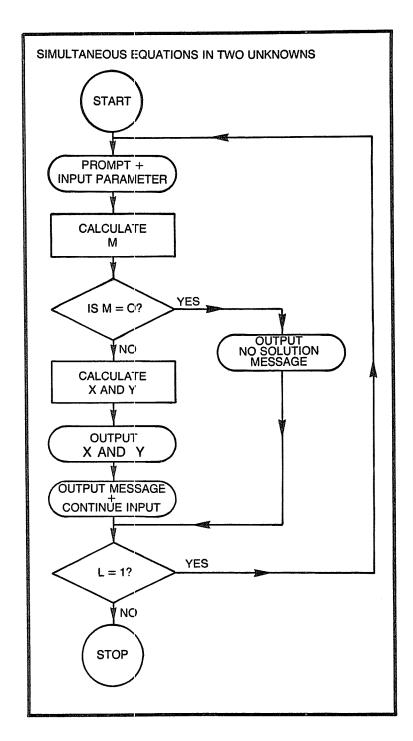
# SIMULTANEOUS EQUATIONS IN TWO UNKNOWNS

The user supplies the components of two AX + BY = C type equations, also giving the computer the opportunity to state if the solution is impossible.

#### FORMULAE

$$X = \frac{ED - BF}{AD - BC} = \begin{vmatrix} E & B \\ F & D \end{vmatrix} Y = \frac{AF - EC}{AD - BC} = \begin{vmatrix} A & E \\ C & F \end{vmatrix}$$

```
AX + BY = E
CX + DY = F
ENTER PARAMETERS, A,B,C,D,E,F
10,20,45,23,56,78
SOLUTION X = 9.6 Y = -2.55
TYPE 1 TO CONTINUE, 0 TO STOP
1
AX + BY = E
CX + DY = F
ENTER PARAMETERS A,B,C,D,E,F
10,10,789,2,2,6
NO SOLUTION. OR NO UNIQUE SOLUTION EXISTS
********
TYPE 1 TO CONTINUE, 0 TO STOP
0
*END
```



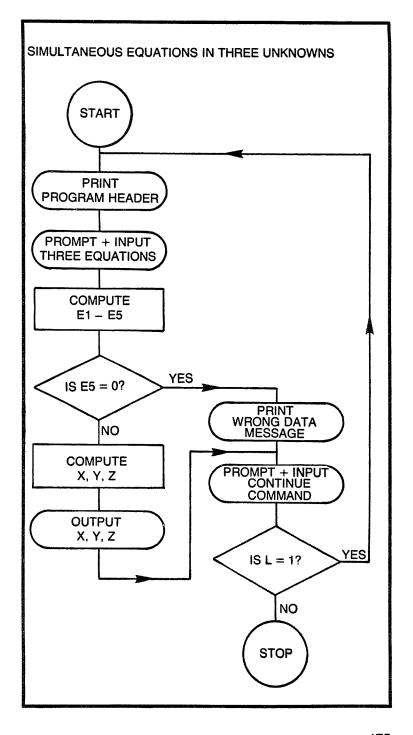
### SIMULTANEOUS EQUATIONS IN TWO UNKNOWNS

- 10 REM THIS PROGRAM COMPUTES SIMULTANEOUS EQUATIONS
- 20 REM IN TWO UNKNOWNS
- 30 PRINT "AX + BY = E"
- 40 PRINT "CX + DY = F"
- 50 PRINT "ENTER PARAMETERS A.B.C.D.E.F"
- 60 INPUT A.B.C.D.E.F
- 70 LET M = (A\*D) (B\*C)
- 80 IF M = 0 THEN 140
- 90 LET X = ((E\*D) (B\*F))/M
- 100 LET Y = ((A\*F) (E\*C))/M
- PRINT "SOLUTION", "X = "; X, "Y = "; Y
- 120 PRINT "\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*
- 130 GOTO 160
- 140 PRINT "NO SOLUTION, OR NO UNIQUE SOLUTION EXISTS"
- 150 PRINT "\*\*\*\*\*\*\*\*\*\*\*\*\*\*\*
- 160 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 170 INPUT L
- 180 IF L = 1 THEN 200
- 190 STOP
- 200 PRINT
- 210 GOTO 30
- 220 END

# SIMULTANEOUS EQUATIONS IN THREE UNKNOWNS

The computer solves a system of three equations in three unknowns with the parameters supplied by the user.

```
SOLVE FOR 3 EQUATIONS IN 3 UNKNOWNS
OF THE TYPE AX + BY + CZ = D
ENTER FIRST EQUATION(A,B,C,D)
?
1,4,6,3
ENTER SECOND EQUATION(A,B,C,D)
?
- 3,8,0, - 2
ENTER THIRD EQUATION(A,B,C,D)
?
4, - 5,2,6
SOLUTION
X = 2.65516 Y = .741935 Z = - .435483
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



# SIMULTANEOUS EQUATIONS IN THREE UNKNOWNS

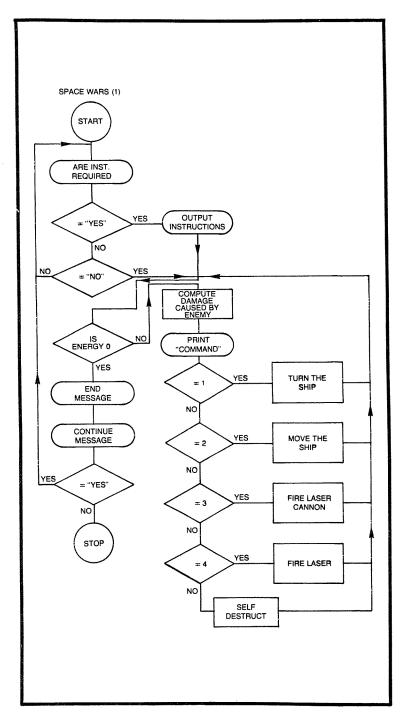
- 10 REM THIS PROGRAM COMPUTES THE SOLUTION TO
- 20 REM A SYSTEM OF 3 EQUATIONS IN 3 UNKNOWNS
- 30 PRINT "SOLVE FOR 3 EQUATIONS IN 3 UNKNOWNS"
- 40 PRINT "OF THE TYPE AX + BY + CZ = D"
- 50 PRINT "ENTER 1ST EQUATION (A,B,C,D)"
- 60 INPUT A1, B1, C1, D1
- 70 PRINT "ENTER 2ND EQUATION (A,B,C,D)"
- 80 INPUT A2.B2.C2.D2
- 90 PRINT "ENTER 3RD EQUATION (A,B,C,D)
- 100 INPUT A3, B3, C3, D3
- 110 LET E1 = ((B1\*A2)/A1) B2
- 120 LET E2 = ((C1\*A2)/A1) C2
- 130 LET E3 = ((B1\*A3)/A1) B3
- 140 LET E4 = ((C1\*A3)/A1) C3
- 150 LET E5 = ((E1\*E4) (E2\*E3))
- 160 IF E5 = 0 THEN 250
- 170 LET E6 = ((D1\*A2)/A1) D2
- 180 LET E7 = ((D1\*A3)/A1) D3
- 190 LET Y = ((E6\*E4) (E2\*E7))/E5
- 200 LET Z = ((E1\*E7) (E6\*E3))/E5
- 210 LET X = (D1/A1) ((B1/A1\*Y) ((C1/A1)\*Z)
- 220 PRINT "SOLUTION"
- 230 PRINT "X = "; X, "Y = "; Y, "Z = "; Z
- 240 GOTO 260
- 250 PRINT "INSUFFICIENT OR ERRONEOUS DATA ENTERED"
- 260 PRINT
- 270 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 280 INPUT L
- 290 IF L = 1 THEN 310
- 300 STOP
- 310 PRINT
- 320 GOTO 30
- 330 END

## SPACE WARS (1)

The game of Space Wars, as simulated by this program, is a battle between two ships, one the enemy, the other the player. The player has the following options: rotate the ship, move the ship, fire the laser cannon, fire the laser, or self-destruct. The object of this game is to destroy the enemy. The enemy, also being armed with a laser cannon and a laser, fires on you, so be careful.

```
RUN
ARE INSTRUCTIONS REQUIRED? TYPE EITHER
YES OR NO
YES
THERE ARE 5 EXECUTIVE COMMANDS: TURN THE
SHIP(1), MOVE(2), FIRE LASER CANNON(3),
FIRE LASER(4) AND SELF-DESTRUCT(5)
THE CANNON MUST BE FIRED WITHIN 10 DEGREES
OF 90 TO BE EFFECTIVE. NEGATIVE DEG TURNS TO-
   WARDS
0 AND POSITIVE DEG TOWARDS 180. ENTERING NEGATIVE
   KM
MOVES YOU TOWARDS THE ENEMY, WHILE POSITIVE
   MOVES
YOU AWAY. LASER EFFECTIVENESS IS RANDOM, DUE TO
SHIELDING, DISTANCE AND INTERSTELLAR DEBRIS
MAY THE FORCE BE WITH YOU
DISTANCE TO ENEMY 3.7 E0 3KM
BEARING IS 87 DEGREES
THE SKY FIGHTER HAS FIRED HIS LASER
YOUR TOTAL ENERGY IS NOW 9.75E03 UNITS
THE ENEMY HAS 9.5E03 UNITS OF ENERGY LETS
WHICH COMMAND DO YOU WISH TO EXECUTE
?
HOW MANY KM TO TRANSVERSE
- 3.3E03
DISTANCE TO ENEMY 400KM
BEARING IS 87 DEGREES
THE SKY FIGHTER HAS FIRED HIS LASER
```

YOUR TOTAL ENERGY IS NOW 9.32E03 UNITS THE ENEMY HAS 9.0E03 UNITS OF ENERGY LEFT WHICH COMMAND DO YOU WISH TO EXECUTE 5 YOU HAVE INSTRUCTED THE ON-BOARD COMPUTER TO SELF-DESTRUCT, THE REACTOR HAS GONE CRITICAL, YOU HAVE GONE TO MEET THE FORCE YOUR DESTRUCTION HAS ALSO DESTROYED THE SKY FIGHTER, YOU WILL BE REMEMBERED AS A HERO SPACE WARS IS OVER TO PLAY SPACE WARS AGAIN TYPE GO, OTHERWISE TYPE NO ? NO SPACE WARS SAYS GOOD-BYE \*END



#### SPACE WARS (1)

- 10 REM THIS PROGRAM IS THE GAME OF SPACE WARS
- 20 REM TWO SHIPS BATTLE, YOU MUST DESTROY THE
- 30 REM ENEMY TO SAVE THE REPUBLIC
- 40 RANDOMIZE
- 50 PRINT "ARE INSTRUCTIONS REQUIRED? TYPE EITHER"
- 60 PRINT "YES OR NO"
- 70 INPUT A\$
- 80 IF A\$ = "YES" THEN 120
- 90 IF A\$ = "NO" THEN 250
- 100 PRINT "INVALID RESPONSE"
- 110 GOTO 50
- 120 PRINT
- 130 PRINT "THERE ARE 5 EXECUTIVE COMMANDS; TURN THE"
- 140 PRINT "SHIP(1), MOVE(2), FIRE LASER CANNON(3),"
- 150 PRINT "FIRE LASER(4) AND SELF-DESTRUCT(5)"
- 160 PRINT "THE CANNON MUST BE FIRED WITHIN 10 DEGREES"
- 170 PRINT "OF 90 TO BE EFFECTIVE. NEGATIVE DEG TURNS TOWARDS"
- 180 PRINT "0 AND POSITIVE DEG TOWARDS 180. ENTERING NEGATIVE KM"
- 190 PRINT "MOVES YOU TOWARDS THE ENEMY, WHILE POSITIVE MOVES"
- 200 PRINT "YOU AWAY. LASER EFFECTIVENESS IS RANDOM. DUE TO"
- 210 PRINT "SHIELDING, DISTANCE AND INTERSTEL-LAR DEBRIS"
- 220 PRINT
- 230 PRINT "\*\*\*\*\*\*\*\*\*\*\*\*\*GOOD-LUCK\*\*\*\*\*\*\*\*\*\*\*\*\*\*
- 240 PRINT "MAY THE FORCE BE WITH YOU"
- 250 LET E1 = 1E04
- 260 LET E2 = E1
- 270 LET D = 1E03 + INT(5E05\*RND)
- 280 LET B = 1 + INT(180\*RND)
- 290 GOSUB 34:0
- 300 GOSUB 390
- 310 LET E1 = E1 D1
- 320 GOSUB 500

```
330 GOTO 690
```

- 340 IF D > = 1E05 THEN 370
- $350 \quad LET L = 1$
- 360 GOTO 380
- 370 LET L = 0
- 380 RETURN
- 390 IF L = 0 THEN 440
- 400 LET H2 = (1 + INT(100\*RND))/100
- 410 LET D1 = 500\*H2
- 420 LET E2 = E2 500
- 430 GOTO 490
- 440 LET M1 = 1 + INT(2\*RND)
- 450 IF M1 = 1 THEN 470
- 455 LET D1 = 1000
- 460 GOTO 480
- 470 LET D1 = 0
- 480 LET E2 = E2 1000
- 490 RETURN
- 500 PRINT
- 510 PRINT "DISTANCE TO ENEMY ";D;"KM"
- 520 PRINT "BEARING IS ";B;" DEGREES"
- 530 IF L = 1 THEN 560
- 540 PRINT "THE SKY FIGHTER HAS FIRED THE LASER CANNON"
- 550 GOTO 570
- 560 PRINT "THE SKY FIGHTER HAS FIRED HIS LASER"
- 570 PRINT "YOUR TOTAL ENERGY IS NOW";E1;"
  UNITS"
- 580 PRINT "THE ENEMY HAS ";E2;" UNITS OF ENERGY LEFT"
- 590 IF E1 < = 0 THEN 620
- 600 IF E2 < = 0 THEN 650
- 610 GOTO 680
- 620 PRINT "YOUR ENERGY LEVEL IS ZERO, THE ENEMY"
- 630 PRINT "HAS WON, YOU HAVE BECOME ONE WITH THE FORCE!"
- 640 GOTO 1180
- 650 PRINT "THE ENEMY HAS RUN OUT OF ENERGY, YOU"
- 660 PRINT "HAVE WON"
- 670 GOTO 1180
- 680 RETURN

- 690 PRINT
- 700 PRINT "WHICH COMMAND DO YOU WISH TO EXE-CUTE"
- 710 INPUT C
- 720 ON C GOTO 730, 840, 1010, 1100, 1140
- 730 PRINT "HOW MANY DEGREES OF ROTATION"
- 740 INPUT B1
- 750 IF B + B1 = 0 THEN 800
- 760 IF B + B1 > 180 THEN 820
- 770 LET B = B + B1
- 780 LET E1 = E1 (10\*ABS(B1))
- 790 GOTO 290
- 800 PRINT "YOUR ANGLE MUST BE GREATER THAN 0 DEGREES"
- 810 GOTO 730
- PRINT "YOUR ANGLE MUST BE LESS THAN 181 DE-GREES"
- 830 GOTO 730
- 840 PRINT "HOW MANY KM TO TRANSVERSE"
- 850 INPUT K
- 860 IF D + K = 0 THEN 910
- 870 IF D + K > 1E06 THEN 960
- 880 LET D = D + K (1000)
- 890 LET E1 = E1 (ABS)
- 900 GOTO 290
- 910 PRINT "YOU HAVE TRIED TO CLOSE THE DISTANCE TO ZERO"
- 920 PRINT "BETWEEN YOU AND THE ENEMY, THE ON-BOARD"
- 930 PRINT "COMMAND COMPUTER WILL NOT EXE-CUTE THIS MANEUVER"
- 940 PRINT
- 950 GOTO 840
- 960 PRINT "YOU HAVE TRIED TO EXCEED THE DISTANCE WHERE"
- 970 PRINT "ANY OF YOUR WEAPONS ARE EFFECTIVE"
- 980 PRINT "THE ON-BOARD COMPUTER WILL NOT"
- 990 PRINT "EXECUTE THIS MANEUVER"
- 1000 GOTO 840
- 1010 LET E1 = E1 1000
- 1020 IF B > = 80 THEN 1050
- 1030 PRINT "YOUR ANGLE IS TOO SMALL, YOU HAVE MISSED"

- 1040 GOTO 290
- 1050 IF B < = 100 THEN 1080
- 1060 PRINT "YOUR ANGLE IS TOO GREAT, YOU HAVE MISSED"
- 1070 GOTO 290
- 1080 LET E2 = E2 1000
- 1090 GOTO 290
- 1100 LET E1 = E1 500
- 1110 LET D2 = (1 + INT(100\*RND))/100
- 1120 LET E2 = E2 (D2\*500)
- 1130 GOTO 290
- 1140 PRINT "YOU HAVE INSTRUCTED THE ON-BOARD COMPUTER"
- 1150 PRINT "TO SELF-DESTRUCT, THE REACTOR HAS GONE"
- 1160 PRINT "CRITICAL, YOU HAVE GONE TO MEET THE FORCE"
- 1170 IF D < = 500 THEN 1200
- 1180 PRINT "SPACE WARS IS OVER"
- 1190 GOTO 1240
- 1200 PRINT "YOUR DESTRUCTION HAS ALSO DESTROYED"
- 1210 PRINT "THE SKY FIGHTER, YOU WILL BE REMEMBERED"
- 1220 PRINT "AS A HERO"
- 1230 GOTO 1180
- 1240 PRINT
- 1250 PRINT "TO PLAY SPACE WARS AGAIN TYPE GO,"
- 1260 PRINT "OTHERWISE TYPE NO"
- 1270 INPUT Z\$
- 1280 IF Z\$ = "GO" THEN 1310
- 1290 PRINT "SPACE WARS SAYS GOOD-BYE"
- 1300 STOP
- 1310 PRINT
- 1320 GOTO 50
- 1330 END

# SPACE WARS (2)

This computer simulation requires considerably more memory than any other program in the book. For the user who is memory limited, the following may be done. Deleting the REM statements, removing the instructions, and reducing the string lengths in the messages will reduce the memory requirement by about 50 percent.

#### **EXAMPLE**

RUN

ARE INSTRUCTIONS FOR SPACE WARS REQUIRED? TYPE EITHER YES OR NO

?

YES

THE DEATH STAR SPACE STATION, YOUR GOAL, IS HEAVILY

SHIELDED AND MOUNTS MORE FIREPOWER THAN HALF THE IMPERIAL FLEET. BUT, ITS DEFENSES WERE PRIMARILY DESIGNED TO FEND OFF LARGE-SCALE CAPI-TAL

SPACE-SHIP ASSAULTS. A SMALL, ONE- OR TWO-MAN X-WING FIGHTER SHOULD BE ABLE TO SLIP THROUGH ITS DEFENSIVE SCREENS. YOUR MISSION IS TO DESTROY THE DEATH STAR!!! ON ITS SURFACE THERE IS A SMALL THERMAL EXHAUST PORT. ITS SIZE BELIES ITS IMPORTANCE

AS IT APPEARS TO BE AN UNSHIELDED SHAFT THAT RUNS DIRECTLY INTO THE MAIN REACTOR SYSTEM POWERING THE DEATH STAR SPACE STATION. SINCE THIS SERVES AS AN EMERGENCY OUTLET FOR WASTE HEAT IN THE EVENT OF REACTOR OVERPRODUCTION, ITS USEFULNESS

WOULD BE ELIMINATED BY ENERGY-PARTICLE SHIELD-ING.

A DIRECT HIT WOULD INITIATE A CHAIN REACTION THAT WOULD DESTROY THE STATION, THUS PROTECTING THE REPUBLIC

\*\*\*\*\*\*EXECUTIVE COMMANDS ARE\*\*\*\*\*\*

- (1) FIRE HIGH-ENERGY TORPEDO
- (2) FIRE LASER CANNON
- (3) FIRE LASER
- (4) PROPULSION OF X-WING

THE BATTLE COMPUTER OPTION MAY BE USED WITH COMMANDS

2 AND 3. THE ENERGY TORPEDO IS USED TO DESTROY THE DEATH STAR WITH, EACH TORPEDO EXPENDS 20,000 UNITS OF ENERGY. THE LASER CANNON MAY BE USED AGAINST THE SKY FIGHTERS, IT REQUIRES 5,000 UNITS THE LASER USES 1,000 ENERGY UNITS PER SHOT AND IT IS ALSO USED AGAINST THE SKY FIGHTERS.

THE BATTLE COMPUTER REQUIRES 500 ENERGY UNITS, BUT,

GUARANTEES A DIRECT HIT ON A SKY FIGHTER. TO DESTROY A SKY FIGHTER YOU MUST DEPLETE IT OF ENERGY.

MOVING THE X-WING SPACE CRAFT IS IMPERATIVE AS THE ENERGY TORPEDO MUST BE FIRED WITHIN 1000KM OF THE DEATH STAR. X-WING PROPULSION REQUIRES 1 ENERGY UNIT PER KM

# GOOD-LUCK MAY THE FORCE BE WITH YOU

DISTANCE TO DEATH STAR IS NOW 1E05KM
THE SKY FIGHTER HAS FIRED HIS LASER CANNON
THE DARK LORD IS EXTREMELY DANGEROUS!!!
THE SMITH LORD HAS USED A LASER CANNON ENERGY
BEAM

YOUR TOTAL ENERGY IS NOW 4.98E05 WHICH COMMAND DO YOU WISH TO EXECUTE ?

. 4

HOW MANY UNITS OF ENERGY DO YOU WISH TO FEED TO THE HYPER-ATOMIC DRIVE UNIT, (1 UNIT/1KM)

\*\*CAUTION\*\* TOO MUCH ENERGY WILL OVER-HEAT THE REACTOR, INPUT NO MORE THAN 22,500 UNITS AT ANY ONE TIME

?

30,000

IN WHICH DIRECTION, AWAY (A) OR TOWARDS (T) THE DEATH STAR

?

T

YOU HAVE WASTED 3.0E04 UNITS OF ENERGY THE REACTOR IS CRITICALLY OVERHEATED

```
DISTANCE TO DEATH STAR IS NOW 1E05KM
THE SKY FIGHTER HAS FIRED HIS LASER CANNON
RADER'S ON-BOARD ATTACK COMPUTER HAS MATCHED
YOUR COURSE, HIS WEAPONS ARE READY
THE SMITH LORD HAS USED A LASER CANNON ENERGY
 BEAM
YOUR TOTAL ENERGY IS NOW 4.39E05 UNITS
WHICH COMMAND DO YOU WISH TO EXECUTE
4
HOW MANY UNITS OF ENERGY DO YOU WISH TO FEED TO
THE HYPER-ATOMIC DRIVE UNIT, (1 UNIT/1KM)
**CAUTION** TOO MUCH ENERGY WILL OVER-HEAT
THE REACTOR, INPUT NO MORE THAN 22,500 UNITS
AT ANY ONE TIME
20,000
IN WHICH DIRECTION, AWAY (A) OR TOWARDS (T)
THE DEATH STAR
?
T
DISTANCE TO DEATH STAR IS NOW 8.0E04KM
THE SKY FIGHTER HAS FIRED HIS LASER CANNON
*CAUTION* GARTH RADER IS THE BEST SHOT IN THE
IMPERIAL FLEET, PLUS HE USES THE BAD SIDE OF THE
  FORCE
THE SMITH LORD HAS USED A LASER CANNON ENERGY
  BEAM
YOUR TOTAL ENERGY IS NOW 4.1E05 UNITS
WHICH COMMAND DO YOU WISH TO EXECUTE
TO PLAY SPACE WARS AGAIN TYPE GO, IF
NOT TYPE NO
?
NO
SPACE WARS SAY GOOD-BYE AND MAY THE FORCE
  BE WITH YOU
*END
The ///// indicate where the program was terminated, this simula-
tion may be played for a considerable length of time. In the interest of
saving space and leaving the unexpected to the user only a portion of
a typical run has been shown.
```

- GOAL, IS HEAVILY"

  160 PRINT "SHIELDED AND MOUNTS MORE
- FIREPOWER THAN HALF"
  170 PRINT "THE IMPERIAL FLEET. BUT, ITS DE-
- FENSES WERE"

  180 PRINT "PRIMARILY DESIGNED TO FEND OFF
  LARGE-SCALE CAPITAL"
- 190 PRINT "SPACE-SHIP ASSAULTS. A SMALL, ONE-OR TWO-MAN"
- 200 PRINT "X-WING FIGHTER SHOULD BE ABLE TO SLIP THROUGH"
- 210 PRINT "ITS DEFENSIVE SCREENS. YOUR MISSION, IS TO DESTROY"
- 220 PRINT "THE DEATH STAR!!! ON ITS SURFACE THERE IS A SMALL"
- 230 PRINT "THERMAL EXHAUST PORT. ITS SIZE BE-LIES ITS IMPORTANCE"
- 240 PRINT "AS IT APPEARS TO BE AN UNSHIELDED SHAFT THAT RUNS"
- 250 PRINT "DIRECTLY INTO THE MAIN REACTOR SYSTEM, POWERING"

260	PRINT "THE DEATH STAR SPACE STATION. SINCE THIS SERVES"
270	PRINT "AS AN EMERGENCY OUTLET FOR WASTI
280	HEAT IN THE" PRINT "EVENT OF REACTOR OVERPRODUCTION
	ITS USEFULNESS'
290	PRINT "WOULD BE ELIMINATED BY ENERGY- PARTICLE SHIELDING"
300	PRINT "A DIRECT HIT WOULD INITIATE A CHAIN
300	REACTION THAT"
210	PRINT "WOULD DESTROY THE STATION, THUS
310	PROTECTING THE"
320	PRINT "REPUBLIC"
330	PRINT "******EXECUTIVE COMMANDS
	ARE******
340	PRINT "(1) FIRE HIGH-ENERGY TORPEDO"
350	PRINT "(2) FIRE LASER CANNON"
360	PRINT "(3) FIRE LASER"
370	PRINT "(4) PROPULSION OF X-WING"
380	PRINT "THE BATTLE COMPUTER OPTION MAY BE
	USED WITH COMMANDS"
390	PRINT "2 AND 3. THE ENERGY TORPEDO IS USE
	TO DESTROY"
400	PRINT "THE DEATH STAR WITH, EACH TORPEDO
	EXPENDS 20,000"
410	PRINT "UNITS OF ENERGY. THE LASER CANNON
	MAY BE USED"
420	PRINT "AGAINST THE SKY FIGHTERS, IT RE
	QUIRES 5,000 UNITS"
430	PRINT "THE LASER USES 1,000 ENERGY UNITS
	PER SHOT AND IT"
440	PRINT "IS ALSO USED AGAINST THE SKY FIGHT
	ERS."
450	PRINT "THE BATTLE COMPUTER REQUIRES 500
	ENERGY UNITS, BUT,"
460	PRINT "GUARANTEES A DIRECT HIT ON A SKY
	FIGHTER. TO DESTROY"
465	PRINT "A SKY FIGHTER YOU MUST DEPLETE IT OF
	ENERGY."
470	PRINT "MOVING THE X-WING SPACE CRAFT IS IM
	PERATIVE AS"
480	PRINT "THE ENERGY TORPEDO MUST BE FIRED
	WITHIN 1000KM"

```
PRINT "OF THE DEATH STAR. X-WING PROPUL-
490
        SION REQUIRES"
500
      PRINT "1 ENERGY UNIT PER KM"
      PRINT"*******************
510
520
      PRINT" GOOD-LUCK "
530
      PRINT "MAY THE FORCE BE WITH YOU"
      PRINT"**********************
535
536
      REM X-WING ENERGY AND SKY ENERGY
540
      LET X1 = 5E05
550
      LET T1 = 1E04
      LET T2 = 5E04
560
570
      LET D = 1E05
580
      GOSUB 630
590
      GOSUB 730
600
      GOSUB 830
610
      GOSUB 1040
620
      GOSUB 1500
625
      GOTO 580
630
      IF D > 1E04 THEN 660
      LET L = 1
640
      GOTO 700
650
660
      LET L = 0
670
      LET H = (1 + INT(100*RND))/100
680
      LET E1 = 5000*H
690
      GOTO 720
700
      LET H = (1 + INT(100*RND))/100
710
      LET E1 = 1000*H
      RETURN
720
730
      IF D > 5E03 THEN 760
740
      LET K = 1
750
      GOTO 800
760
      LET K = 0
770
      LET H = (1 + INT(100*RND))/100
780
      LET E2 = 8000*H
790
      GOTO 820
      LET H = (1 + INT(100*RND))/100
800
810
      LET E2 = 3000*H
820
      RETURN
830
      IF D < 3E03 THEN 860
      LET E3 = 0
840
      GOTO 880
850
860
      LET H = (1 = INT(100*RND))/100
870
      LET E3 = 2E04*H
```

```
880
       LET T1 = T1 - E1
      LET T2 = T2 - E2
890
      IF T1 < = 0 THEN 920
900
910
       GOTO 950
920
       LET E1 = 0
930
      LET Y = 1
940
       GOTO 960
       LET Y = 0
950
960
       IF T2 < = 0 THEN 980
       GOTO 1010
970
980
       LET E2 = 0
990
       LET Z = 1
       GOTO 1020
1000
1010
       LET Z = 0
       LET X1 = X1 - E1 - E2 - E3
1020
1030
       RETURN
       PRINT "DISTANCE TO DEATH STAR IS NOW";
1040
         D:"KM"
       IF Y = 1 THEN 1100
1045
       IF L = 0 THEN 1080
1050
       PRINT "THE SKY FIGHTER HAS FIRED HIS LASER"
1060
       GOTO 1110
1070
       PRINT "THE SKY FIGHTER HAS FIRED HIS LASER
1080
         CANNON"
       GOTO 111.0
1090
       PRINT "THE SKY FIGHTER IS OUT OF ACTION!!!"
1100
       IF Z = 1 THEN 1180
1110
       GOTO 1220
1120
       IF K = 0 THEN 1160
1130
       PRINT"THE DARK LORD HAS FIRED HIS HIGH
1140
         ENERGY LASER"
       GOTO 1360
1150
       PRINT "THE SMITH LORD HAS USED A LASER CAN-
1160
         NON ENERGY BEAM"
       GOTO 1360
1170
       PRINT "GARTH RADER HAS EXPENDED ALL HIS
1180
         WEAPON'S ENERGY"
       PRINT "SUPPLY. HE IS CURRENTLY ESCAPING TO
1190
         THE ENDS OF"
       PRINT "THE GALAXY. ***THE FORCE IS WITH
1200
         YOU***"
       GOTO 1360
1210
```

1220	LET C = 1 + (5*RND)
1230	ON C GOTO 1240, 1270, 1290, 1310, 1330
1240	PRINT "*CAUTION*GARTH RADER IS THE BEST SHOT IN THE"
1250	PRINT "IMPERIAL FLEET, PLUS HE USES THE BAD
1000	SIDE OF THE FORCE"
1260	GOTO 1130
1270	PRINT "THE DARK LORD IS EXTREMELY DANGEROUS!!!"
1280	GOTO 1130
1290	PRINT "**CAUTION RADER IS INHUMANLY ACCURATE CAUTION**"
1300	GOTO 1130
1310	PRINT "THE SMITH LORD'S PRECISION IS AWE- SOME"
1320	GOTO 1130
1330	PRINT "RADER'S ON-BOARD ATTACK COMPUTER HAS MATCHED"
1340	PRINT "YOUR COURSE, HIS WEAPONS ARE READY"
1350	GOTO 1130
1360	IF D $<$ = 3E03 THEN 1380
1370	GOTO 1410
1380	PRINT "***YOU ARE CLOSER THAN 3000KM TO
	THE SPACE STATION"
1390	PRINT "THE DEATH STAR'S AUTOMATIC DE- FENSE NETWORK HAS BEEN"
1400	PRINT "ACTIVATED. ***USE EXTREME CAUTION***"
1410	PRINT
1415	PRINT "YOUR TOTAL ENERGY IS NOW ";X1;" UNITS"
1420	IF X1 < 2E04 THEN 1140
1430	GOTO 1490
1440	PRINT "YOU HAVE DEPLETED YOUR ENERGY SUPPLY, THE DEATH"
1450	PRINT "STAR WILL NOW DESTROY YOUR HOME PLANET"
1460	PRINT "YOU WILL BE A HERO NOWHERE AND RE- MEMBERED BY NONE"
1470	PRINT "*****YOU HAVE MISUSED THE FORCE*****"
1480	GOTO 2690

1400	DOMIDN
1490	RETURN
1500	PRINT PRINT "WHICH COMMAND DO YOU WISH TO EXE-
1510	CUTE"
1520	INPUT B
1530	ON B GOTO 1540, 1690, 2030, 2320
1540	IF D $<$ = 1000 THEN 1590
1550	PRINT "YOU HAVE WASTED A TORPEDO, YOU ARE FARTHER"
1560	PRINT "AWAY THAN 1000KM"
1570	LET X1 = X1 - 2E04
1580	GOTO 2680
1590	LET H = 1 + (INT(100*RND))
1600	IF $H > = 50$ THEN 1640
1610	PRINT "YOU SHOULD HAVE USED THE FORCE,
	YOU HAVE MISSED"
1620	LET X1 = X1 - 2E04
1630	GOTO 2680
1640	PRINT "THE FORCE WAS WITH YOU, YOU HAVE
	SINGLE-HANDED"
1650	PRINT "DESTROYED THE DEATH STAR. YOU
	HAVE SAVED THE"
1660	PRINT "REPUBLIC AND PRINCESS LEAH ARGONA
	WILL LOVE"
1670	PRINT "YOU FOREVER."
1680	GOTO 2740
1690	PRINT "THE CANNON IS READY, DO YOU WISH
	COMPUTER ASSISTANCE"
1700	PRINT "ENTER EITHER YES OR NO"
1710	INPUT C\$
1720	IF $C$ \$ = "YES" THEN 1820
1730	IF $C$ \$ = "NO" THEN 1880
1740	PRINT "INVALID RESPONSE"
1750	GOTO 1700
1760	PRINT "WHICH FIGHTER THE SKY "S" OR RADER
	"R"
1770	INPUT C\$
1780	IF $C$ \$ = "T" THEN 1840
1790	IF $C$ \$ = "V" THEN 1860
1800	PRINT "WHICH????"
1810	GOTO 1760
1820	LET Q = 5000
1830	GOTO 1760

```
1840
        LET T1 = T1 - Q
 1850
        GOTO 1960
 1860
        LET T2 = T2 - Q
1870
        GOTO 1960
        PRINT "DO YOU WISH TO FIRE ON GARTH RADER
 1880
          (R) OR"
        PRINT "ON THE SKY FIGHTER (S)"
1890
1900
        INPUT C$
1910
        LET Q = 5000*((1 + INT(100*RND))/100)
        IF C$ = "S" THEN 1980
1920
        IF C$ = "R" THEN 2000
1930
1940
        PRINT "WHICH ENEMY????"
1950
        GOTO 1880
        LET X1 = X1 - 5500
1960
1970
        GOTO 2660
1980
        LET T1 = T1 - Q
1990
        GOTO 2010
        LET T2 = T2 - Q
2000
2010
        LET X1 = X1 - 5000
2020
        GOTO 2660
       PRINT "YOU HAVE DECIDED ON USING THE
2030
         LASER"
        PRINT "DO YOU WISH COMPUTER ASSISTANCE,
2040
         YES OR NO"
2050
       INPUT C$
2060
       IF C$ = "YES" THEN 2100
       IF C$ = "NO" THEN 2120
2070
2080
       PRINT "THE COMPUTER RESPONSES ONLY TO A
         YES OR A NO"
2090
       GOTO 2040
2100
       LET I = 1
2110
       GOTO 2130
2120
       LETI = 0
       PRINT "WHICH FIGHTER THE SKY (S) OR RADER
2130
2140
       PRINT "DO YOU WISH TO FIRE ON"
2150
       INPUT C$
2160
       IF J = 1 THEN 2190
       LET Q = 1000*((1 + INT(100*RND))/100)
2170
2180
       GOTO 2200
2190
       LET Q = 1000
2200
       IF C$ = "S" THEN 2240
       IF C$ = "R" THEN 2260
2210
```

```
PRINT "WHICH TARGET????"
2220
2230
       GOTO 2130
       LET T1 = T1 - Q
2240
       GOTO 2270
2250
       LET T2 = T2 - Q
2260
       IF J = 1 THEN 2300
2270
       LET X1 = X1 - 1000
2280
       GOTO 2660
2290
       LET X1 = X1 - 1500
2300
       GOTO 2660
2310
       PRINT "HOW MANY UNITS OF ENERGY DO YOU
2320
         WISH TO FEED TO"
       PRINT "THE HYPER-ATOMIC DRIVE UNIT, (1
2330
         UNIT/1KM)"
       PRINT "**CAUTION** TOO MUCH ENERGY WILL
2340
         OVER-HEAT"
       PRINT "THE REACTOR. INPUT NO MORE THAN
2350
         22.500 UNITS"
       PRINT "AT ANY ONE TIME"
2360
2370
       INPUT F
       PRINT "IN WHICH DIRECTION, AWAY (A) OR TO-
2380
         WARDS (T)"
       PRINT "THE DEATH STAR"
2390
       INPUT C$
2400
       IF F > 2.25E04 THEN 2470
2410
       IF C$ = "A" THEN 2500
2420
       IF C$ = "T" THEN 2620
2430
        PRINT "DON'T YOU KNOW WHICH DIRECTION YOU
2440
          WANT TO GO TO"
        GOTO 2380
2450
        REM OVERHEATING THE REACTOR
2460
        PRINT "YOU HAVE WASTED ":F:" UNITS OF
 2470
          ENERGY"
        PRINT "THE REACTOR IS CRITICALLY OVER-
 2480
          HEATED"
        GOTO 2640
 2490
        LET D = D + F
 2500
        IF D > = 1.5E05 THEN 2540
 2510
        GOTO 2640
 2520
        REM WENT TOO FAR
 2530
        PRINT "WHERE ARE YOU GOING?? THE BATTLE IS
 2540
          IN THE"
        PRINT "OPPOSITE DIRECTION"
 2550
```

2560	GOTO 2640
2570	PRINT "YOU HAVE SMASHED INTO THE DARK STAR******"
2580	PRINT "WHERE DID YOU LEARN TO FLY, GARTH RADER"
2590	PRINT "IS LAUGHING AT YOU;; OH!! BY THE WAY"
2600	PRINT "* * * * * * YOU HAVE LOST * * * * * * "
2610	GOTO 2690
2620	LET D = D - F
2630	IF D < = 0 THEN 2570
2640	LET X1 = X1 - F
2650	GOTO 2680
2660	PRINT "THE SKY FIGHTER'S ENERGY IS NOW ";T1;"UNITS"
2670	PRINT "THE DARK LORD'S ENERGY IS" ;T2;" UNITS"
2680	RETURN
2690	PRINT "YOU ARE AN INCOMPETENT GOOD KNIGHT"
2700	PRINT "YOU HAVE DISGRACED THE MEMORY OF"
2710	PRINT "OBI- SAN COYOTE! WHOSE SIDE ARE YOU ON??"
2720	PRINT "WHY DON'T YOU PROVE YOUR WORTH AND TRY AGAIN"
2730	GOTO 2760
2740	PRINT "OBI- SAN COYOTE WOULD BE PROUD OF YOU"
2750	PRINT "YOU ARE INDEED A **GOOD KNIGHT**"
2760	PRINT
2770	PRINT "TO PLAY SPACE WARS AGAIN TYPE GO, IF"
2780	PRINT "NOT TYPE NO"
2790	INPUT L\$
<b>2800</b>	IF L\$ = "GO" THEN 2840
2810	IF L\$ = "NO" THEN 2860
2820	PRINT "DO YOU WANT TO STOP OR PLAY AGAIN?????"
2830	GOTO 2770
2840	PRINT
2850	GOTO 50
2860	PRINT "SPACE WARS SAY GOOD-BYE AND MAY THE FORCE BE WITH YOU"
2870	END

# STRAIGHT LINE DEPRECIATION

This program computes the value depreciation of an item by the straight line method.

# **FORMULA**

```
X_C = last \ current \ value, \ D = depreciation \ per \ year,
X_I = new \ current \ value
X_C - D = X_I
```

```
EXAMPLE
```

```
ORIGINAL VALUE =
?
10000
LIFETIME IN YEARS =
?
12
```

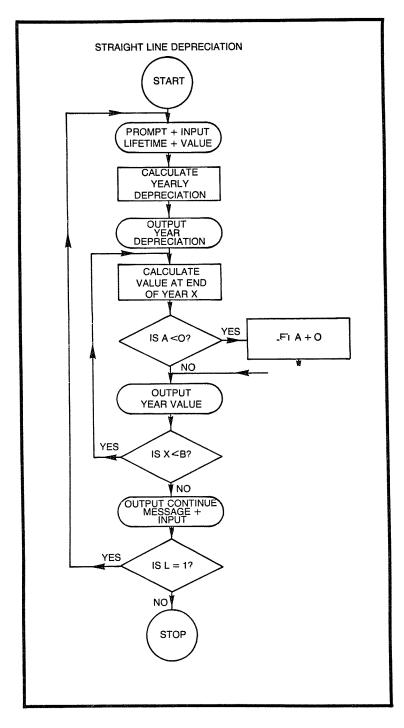
YEARLY DEPRECIATION = 833.333

YEAR	VALUE			
1	9166.66			
2	8333.33			
3	7500.			
4	6666.66			
5	5833.33			
6	5000.			
7	4166.66			
8	3333.33			
9	2500.			
10	1666.66			
11	333.333			
12	0			
**********				

TYPE 1 TO CONTINUE, 0 TO STOP

?

\*END



#### STRAIGHT LINE DEPRECIATION

- 10 REM THIS PROGRAM COMPUTES VALUE DEPRE-CIATION
- 20 REM BY THE STRAIGHT LINE METHOD
- 30 PRINT "ORIGINAL VALUE = ";
- 40 INPUT A
- 50 PRINT "LIFETIME IN YEARS = ";
- 60 INPUT B
- 70 LET C = A/B
- 80 PRINT "YEARLY DEPRECIATION = ":C
- 90 PRINT
- 100 PRINT "YEAR", "VALUE"
- 110 LET X = 0
- 120 LET X = X + 1
- 130 LET A = A C
- 140 IF A < 0 THEN 160
- 150 GOTO 170
- 160 LET A = 0
- 170 PRINT X.A
- 180 IF X < B THEN 120
- 200 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 210 INPUT L
- 220 IF L = 1 THEN 240
- 230 STOP
- 240 PRINT
- 250 GOTO 30
- 260 END

## **VECTOR CROSS PRODUCT**

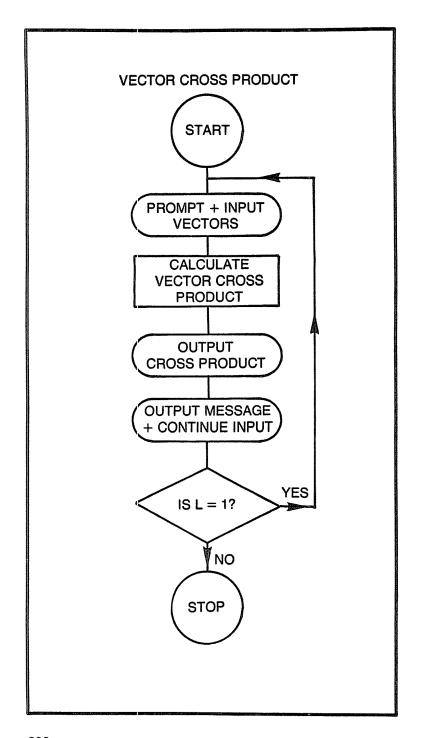
If  $A(A_1,A_2,A_3)$  and  $B(B_1,B_2,B_3)$  are two three-dimensional vectors then the cross product of A and B is denoted by AxB. The program responds with a solution represented by X,Y and Z.

#### **FORMULAE**

$$A \times B = \begin{vmatrix} A_2 A_3 \\ B_2 B_3 \end{vmatrix}, - \begin{vmatrix} A_1 A_3 \\ B_1 B_3 \end{vmatrix}, \begin{vmatrix} A_1 A_2 \\ B_1 B_2 \end{vmatrix}$$
$$= (A_2 B_3 - A_3 B_2, A_3 B_1 - A_1 B_3, A_1 B_2 - A_2 B_1)$$

#### **EXAMPLES**

```
ENTER 1ST VECTOR (A1, A2, A3)
5
10.11.10
ENTER 2ND VECTOR (B1, B2, B3)
4,3,4
VECTOR CROSS PRODUCT
X = 14 Y = 0 Z = -14
++++++++++++++++++++++++
TYPE 1 TO CONTINUE, 0 TO STOP
1
ENTER 1ST VECTOR (A1, A2, A3)
12,23,34
ENTER 2ND VECTOR (B1,B2,B3)
23.41.67
VECTOR CROSS PRODUCT
X = 147 Y = -22 Z = -37
TYPE 1 TO CONTINUE, 0 TO STOP
?
0
*END
```



## **VECTOR CROSS PRODUCT**

- 10 REM THIS PRODUCT COMPUTES THE CROSS PRODUCT
- 20 REM OF TWO VECTORS
- 30 PRINT "ENTER 1ST VECTOR (A1,A2,A3)"
- 40 INPUT A1.A2.A3
- 50 PRINT "ENTER 2ND VECTOR (B1,B2,B3)
- 60 INPUT B1,B2,B3
- 70 LET X = (A2\*B3) (A3\*B2)
- 80 LET Y = (A3\*B1) (A1\*B3)
- 90 LET Z = (A1\*B2) (A2\*B1)
- 100 PRINT "VECTOR CROSS PRODUCT"
- 110 PRINT "X = "; X, "Y = "; Y, "Z = "; Z
- 120 PRINT "++++++++++++ "
- 130 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 140 INPUT L
- 150 IF L = 1 THEN 170
- 160 STOP
- 170 PRINT
- 180 GOTO 30
- 190 END

# **VECTOR DOT PRODUCT AND NORM**

This program computes the vector dot product, also known as the scalar product and the norms of two vectors.

#### **FORMULAE**

$$\overrightarrow{A} = (A_1, A_2, A_3)$$
 and  $\overrightarrow{B}$   $(B_1, B_2, B_3)$  are two vectors

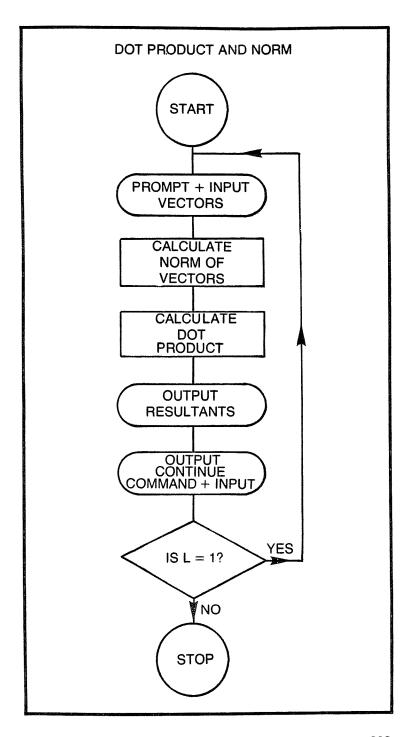
NORM of  $\overrightarrow{A}$  is denoted  $|\overrightarrow{A}|$  and  $\overrightarrow{B}$  is denoted  $|\overrightarrow{B}|$ 

$$|\overrightarrow{A}| = \sqrt{A_1^2 + A_2^2 = A_3^2}$$

$$|\overrightarrow{B}| = \sqrt{B_1^2 + B_2^2 + B_3^2}$$

$$|\overrightarrow{A} \circ \overrightarrow{B} = A_1 B_1 + A_2 B_2 + A_3 B_3$$

# EXAMPLE



## **VECTOR DOT PRODUCT AND NORM**

- 10 REM THIS PROGRAM COMPUTES DOT PRODUCT AND
- 20 REM THE NORMS OF TWO VECTORS
- 30 PRINT "ENTER 1ST VECTOR (A1,A2,A3)"
- 40 INPUT A1, A2, A3
- 50 PRINT "ENTER 2ND VECTOR (B1,B2,B3)"
- 60 INPUT B1,B2,B3
- 70 REM CALCULATE NORM OF A VECTOR
- 80 LET  $X = SQR((A1^2) + (A2^2) + (A3^2))$
- 90 REM CALCULATE NORM OF B VECTOR
- 100 LET  $Y = SQR((B1^{1}2) + (B2^{1}2) + (B3^{1}2))$
- 110 REM CALCULATE DOT PRODUCT
- 120 LET Z = (A1\*B1) + (A2\*B2) + (A3\*B3)
- 130 PRINT "DOT PRODUCT = ":Z
- 140 PRINT "NORM OF 1ST VECTOR = ";X
- 150 PRINT "NORM OF 2ND VECTOR = ";Y
- 170 PRINT "TYPE 1 TO CONTINUE, 0 TO STOP"
- 180 INPUT L
- 190 IF L = 1 THEN 210
- 200 STOP
- 210 PRINT
- 220 GOTO 30
- 230 END

# FROCRAMS & CAMES IN BASIC

From arithmetic progression to statistical permutations to onearm bandits, here are 57 practical, useful and fun programs designed to help you really put your minicomputer to work!

Game programs include blackjack, one-arm bandit, craps, and two space war games. Math and accounting programs include compounding, straight-line depreciation, statistical permutations, instant derivatives, and solutions for integrals—even a whole section of geometric solutions for modern-day Euclids. For history buffs, there is a Day-of-the-Week program for any date back through 1753.

Each program begins with an introductory paragraph describing its capabilities, and continues with a typical program sequence and flowchart. All programs will run on any floating point BASIC.

The author is a veteran computer programmer with extensive experience in developing software in various languages for a wide range of hardware systems.



